

# Towards Bidirectional Ratcheted Key Exchange

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Information Security Group

Royal Holloway, University of London

Bertram Poettering

Horst Görtz Institute for IT Security  
Chair for Network and Data Security  
Ruhr University Bochum

Paul Rösler

RUB

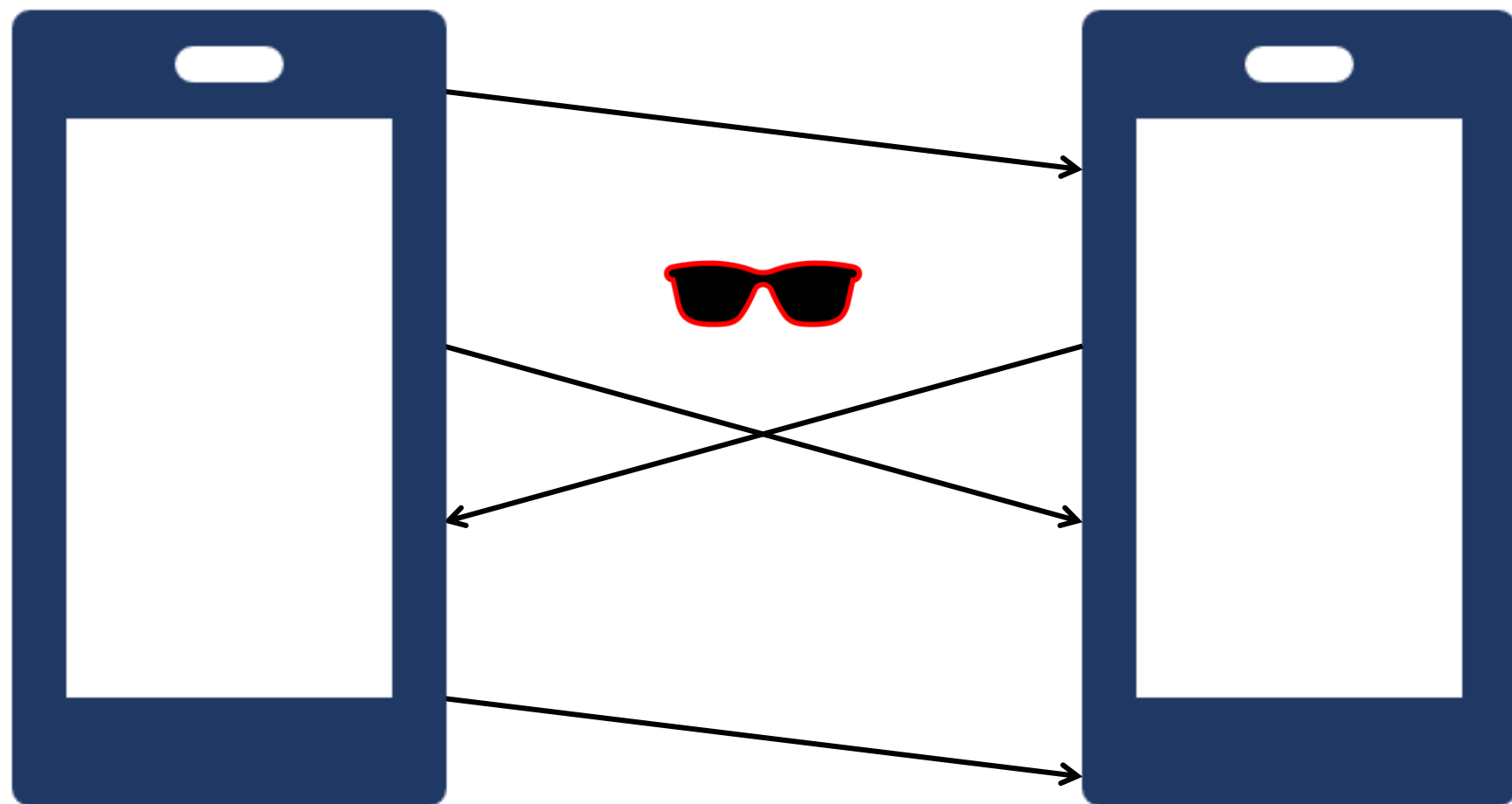


ROYAL  
HOLLOWAY  
UNIVERSITY  
OF LONDON

- What is Ratcheting?  
Modeling RKE  
Construction Intuition  
Results

# Introduction

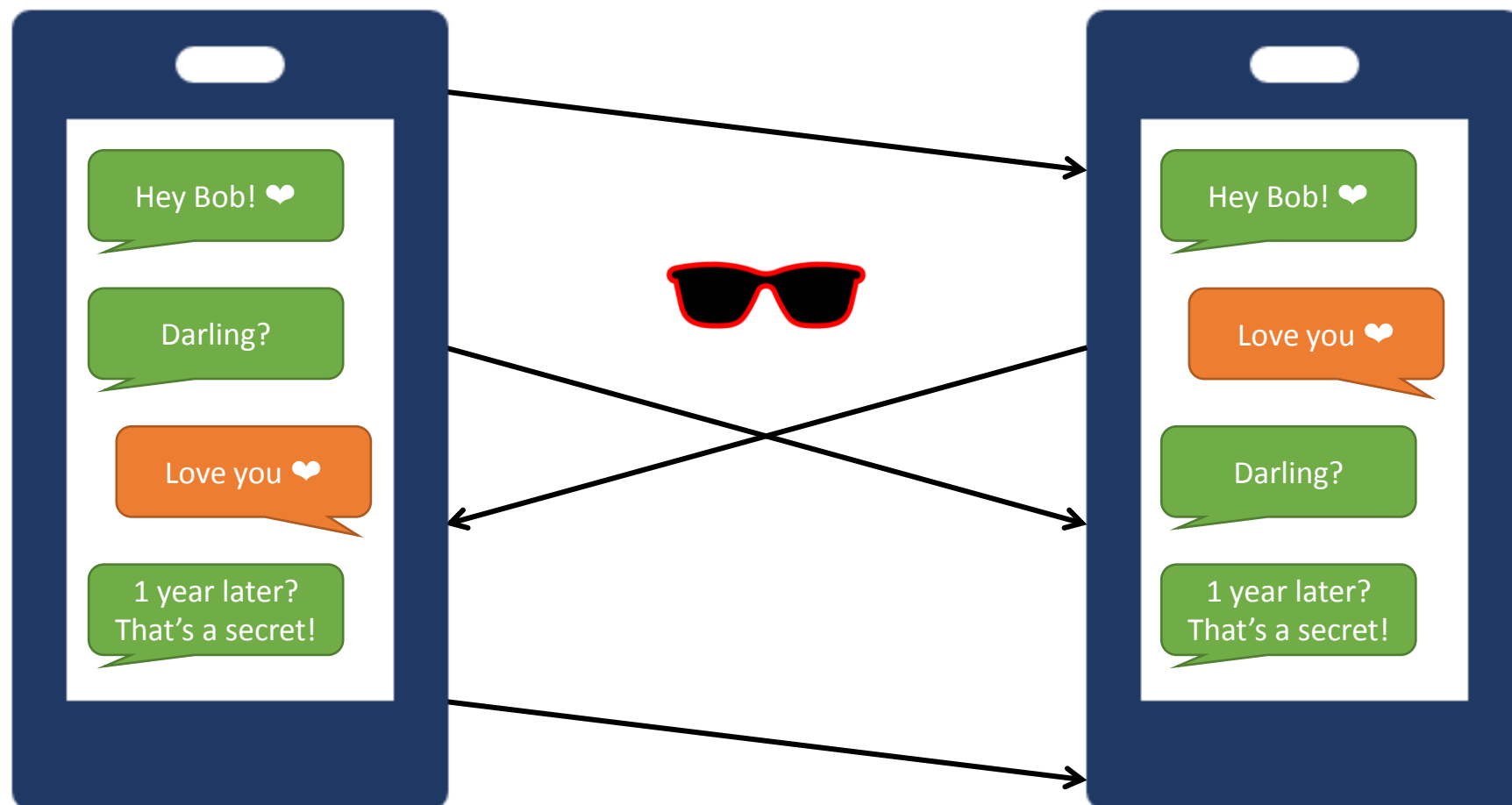
- Alice and Bob communicate
- Active adversary



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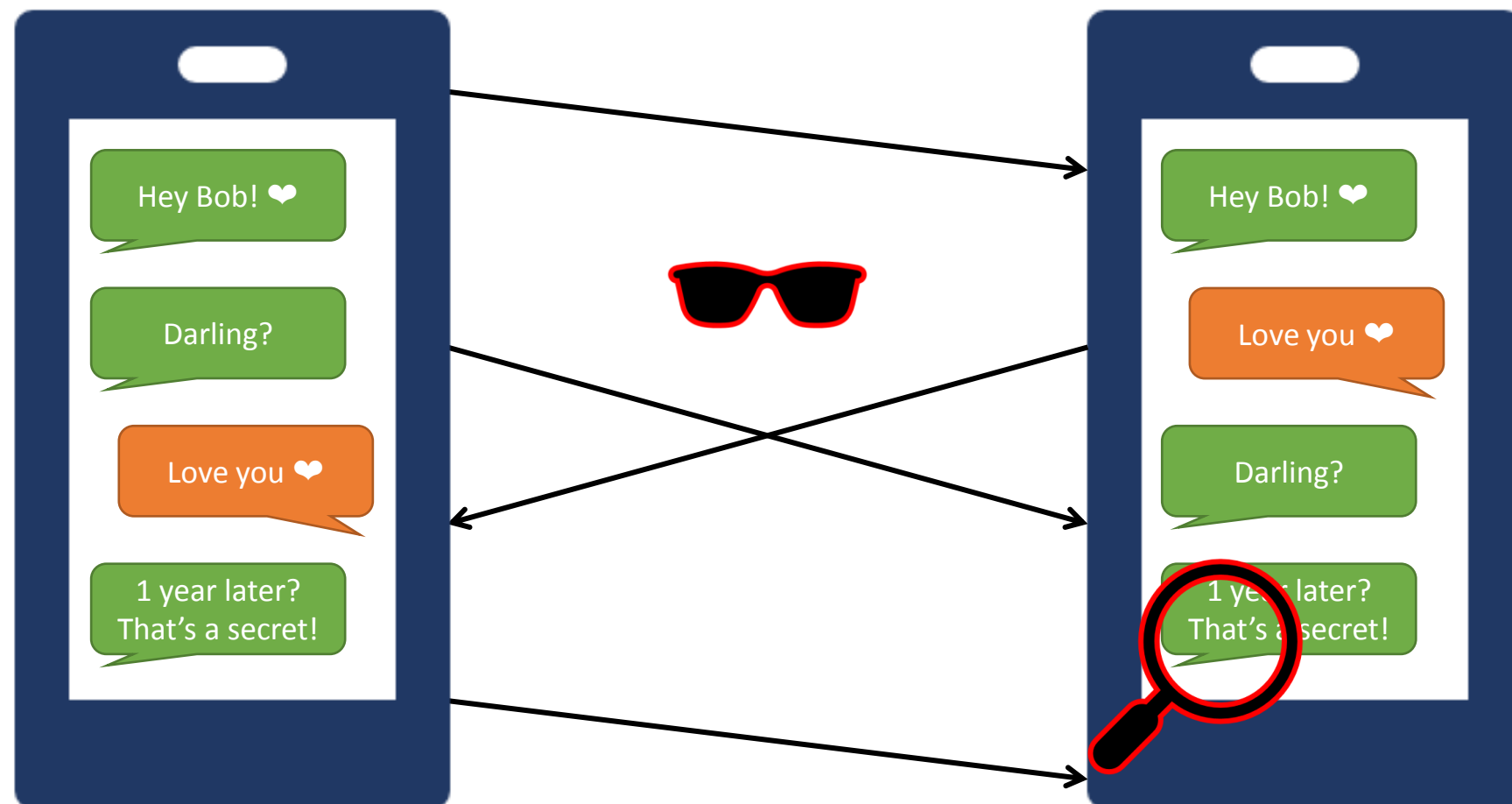
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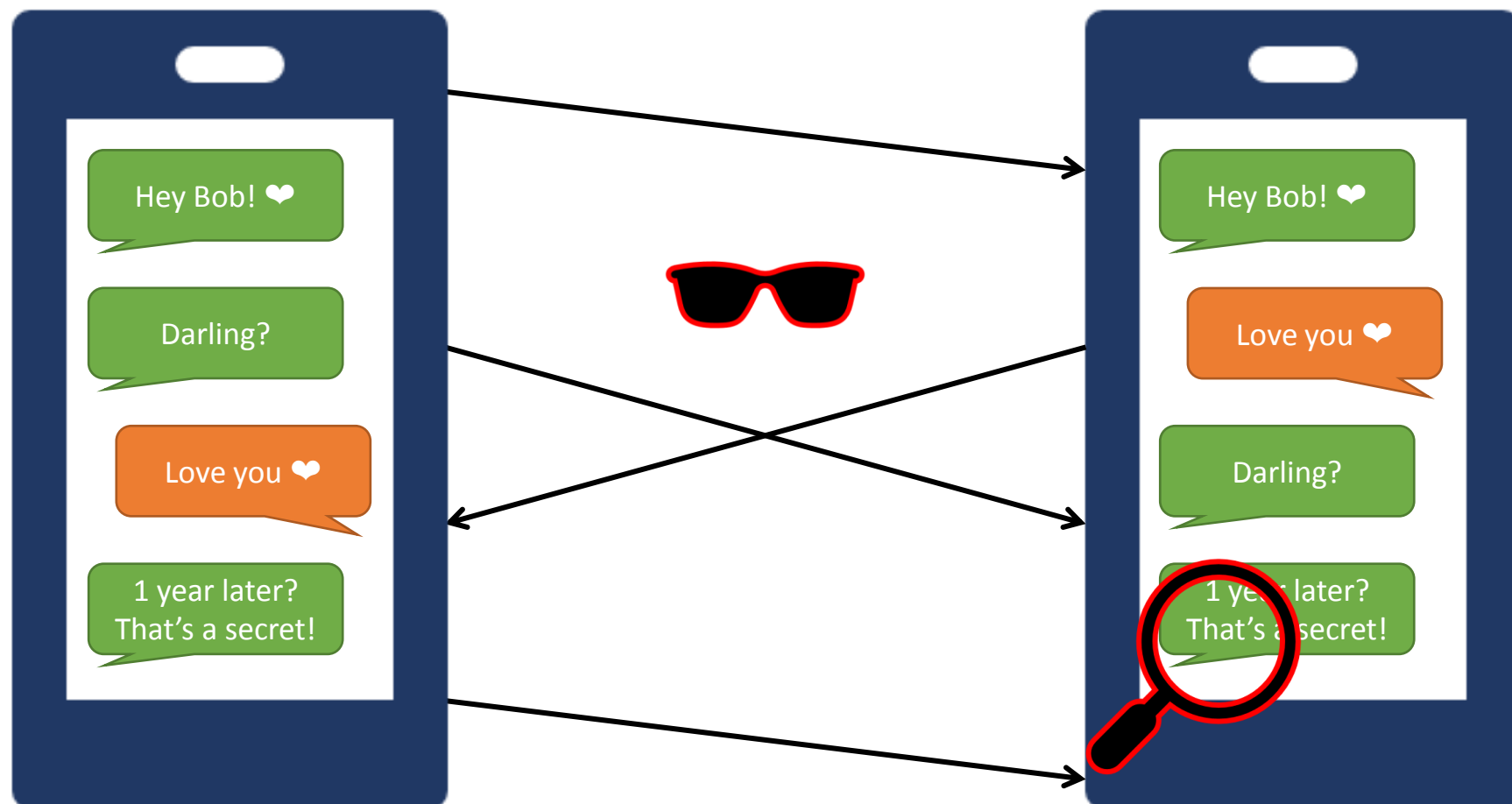
- Alice and Bob communicate
- Active adversary
- Long term communication
  - Local (full) state temporarily exposed



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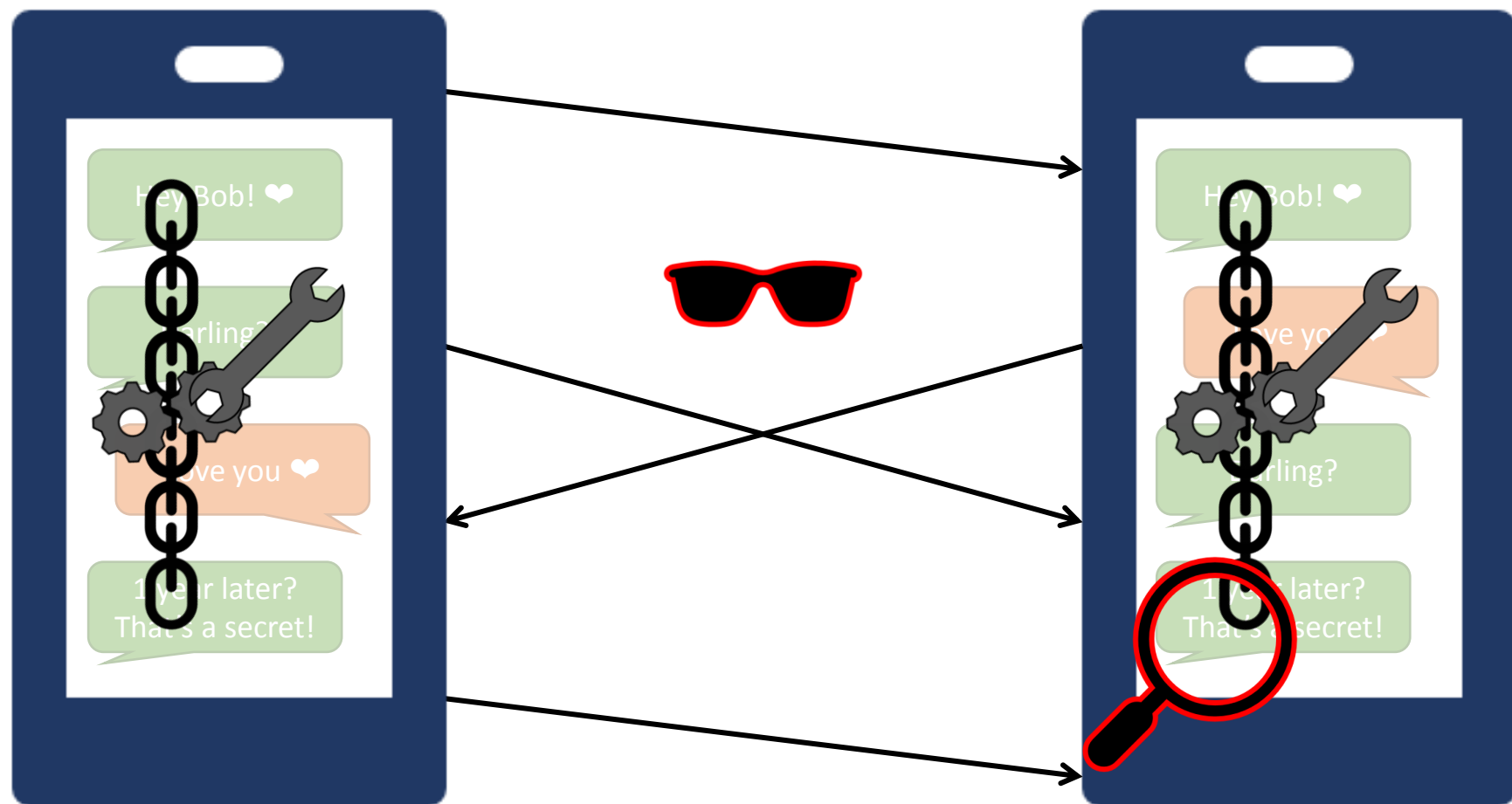
- Alice and Bob communicate
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  - Local (full) state temporarily exposed
- Practical protocols w/o precise security definition
  - E.g., Signal 



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# What is Ratcheting?

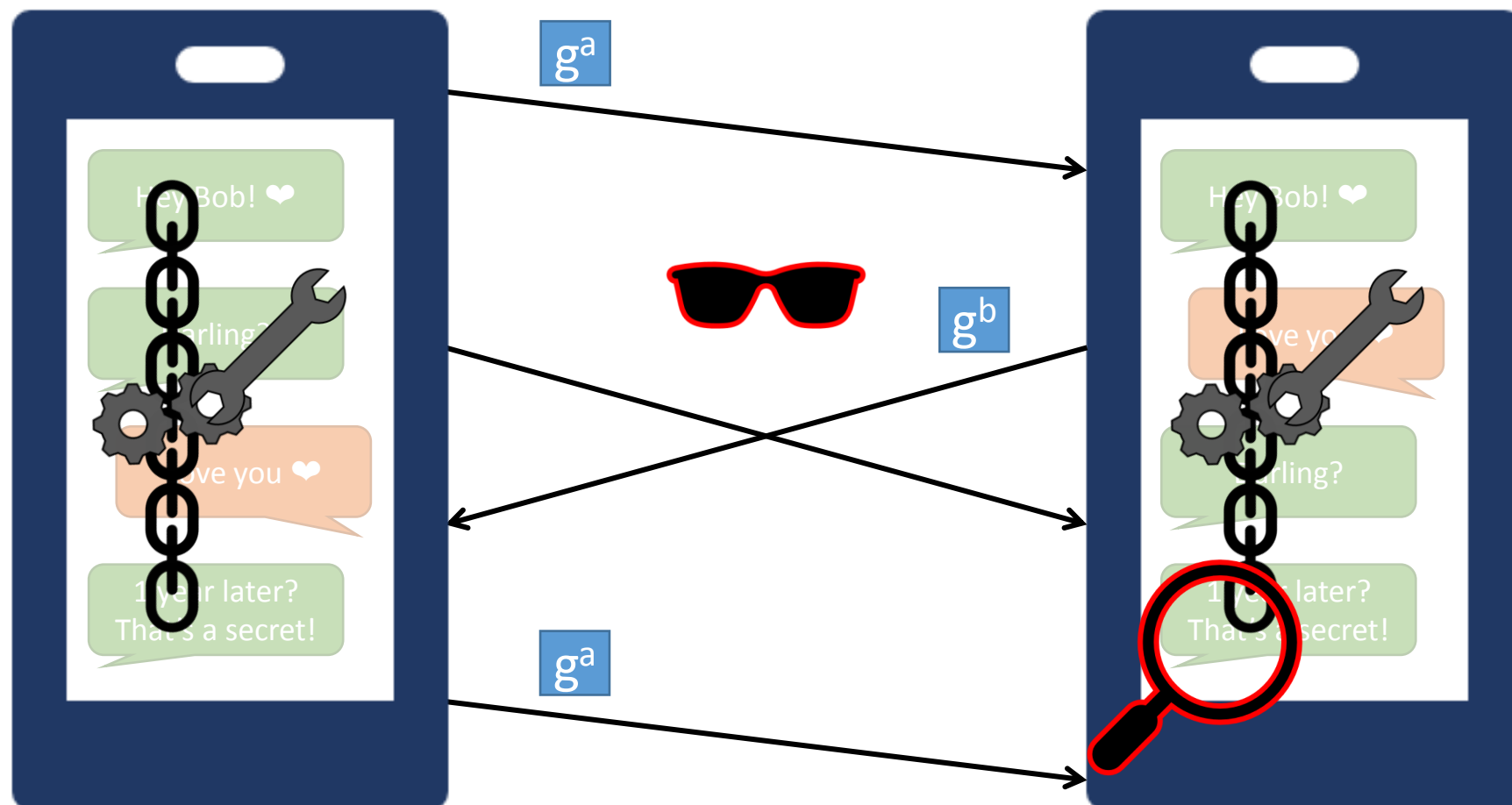
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Modeling RKE  
Construction Intuition  
Results

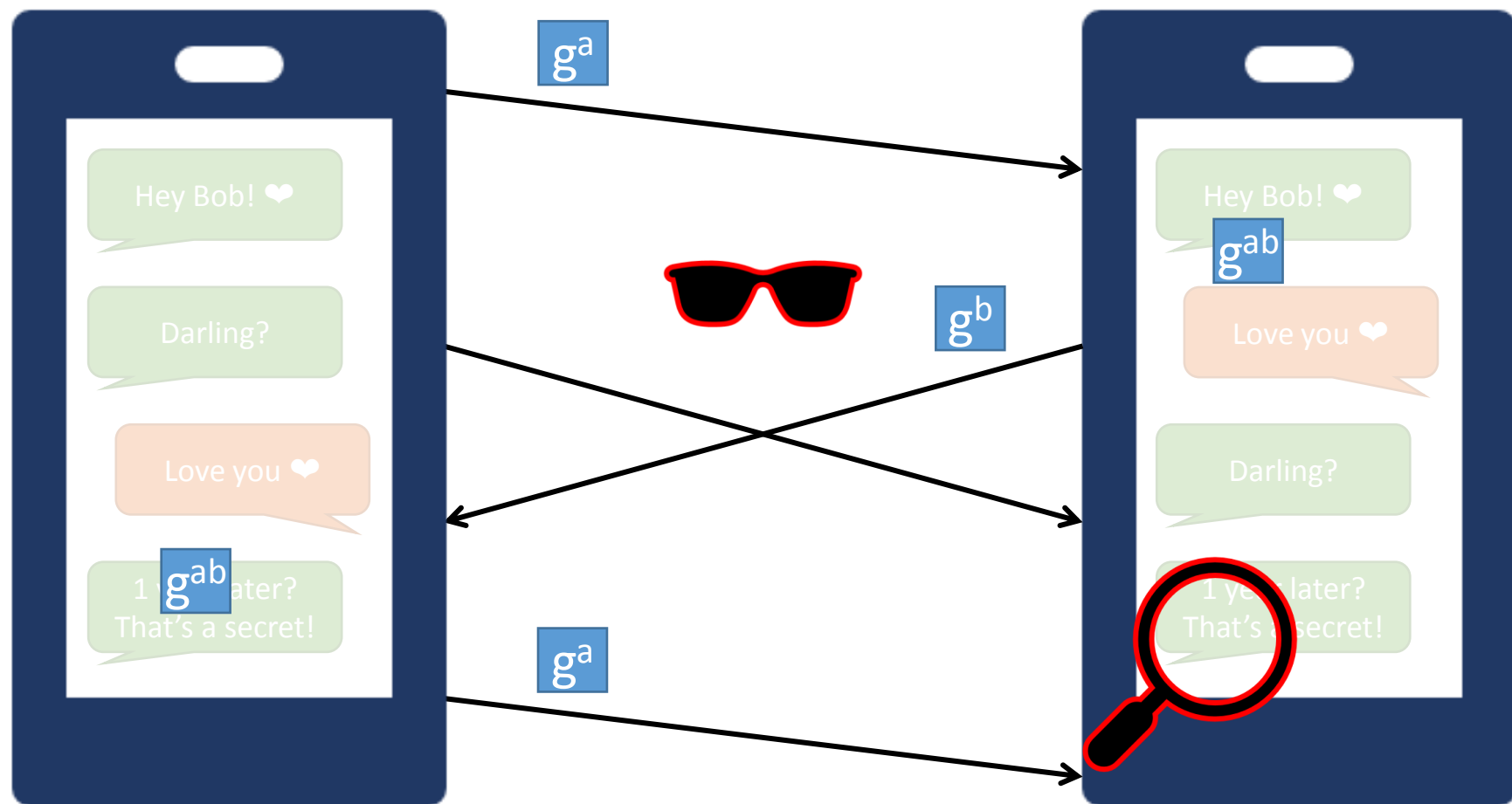
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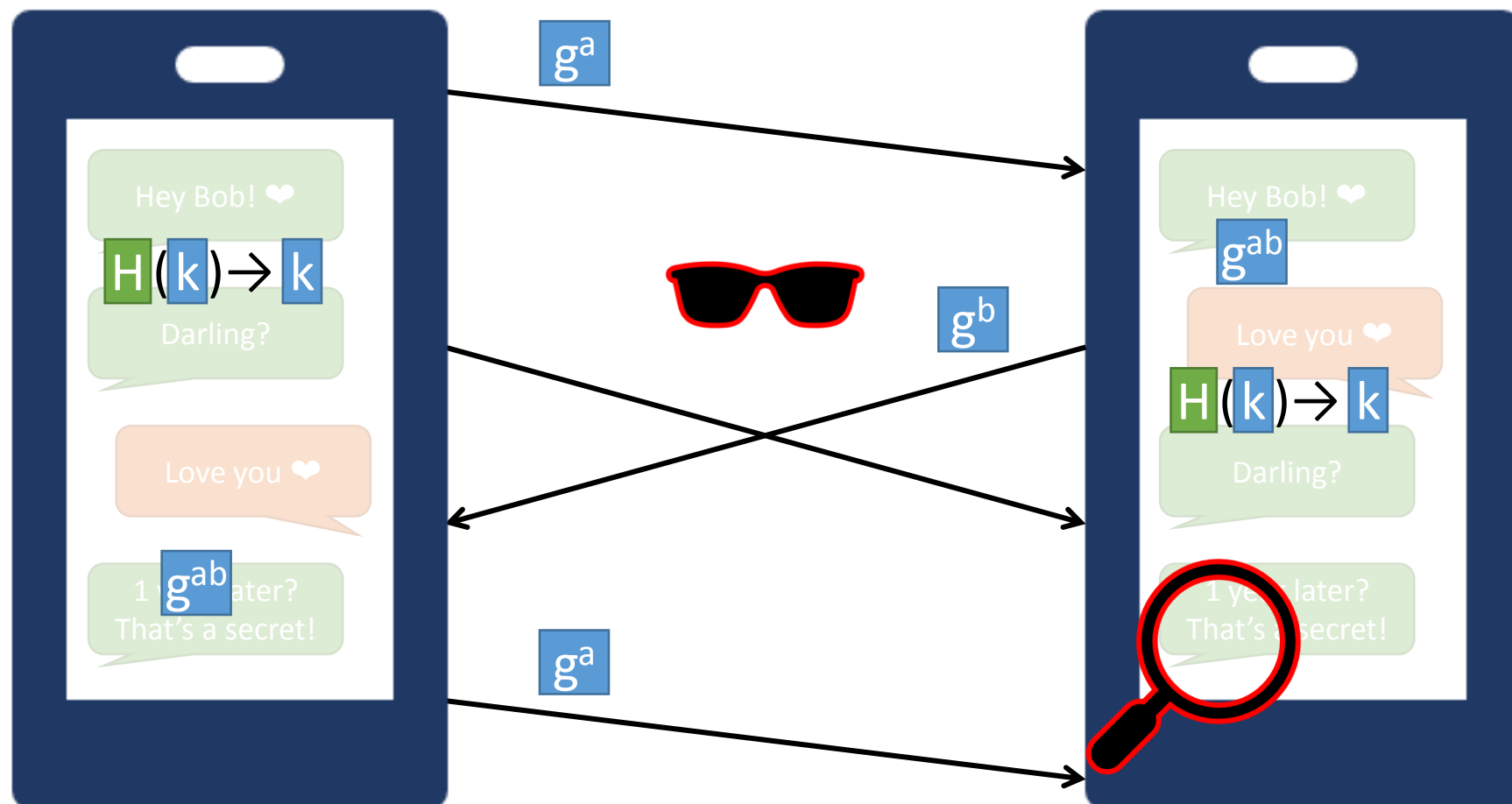




# What is Ratcheting?

- What is Ratcheting?  
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Construction Intuition  
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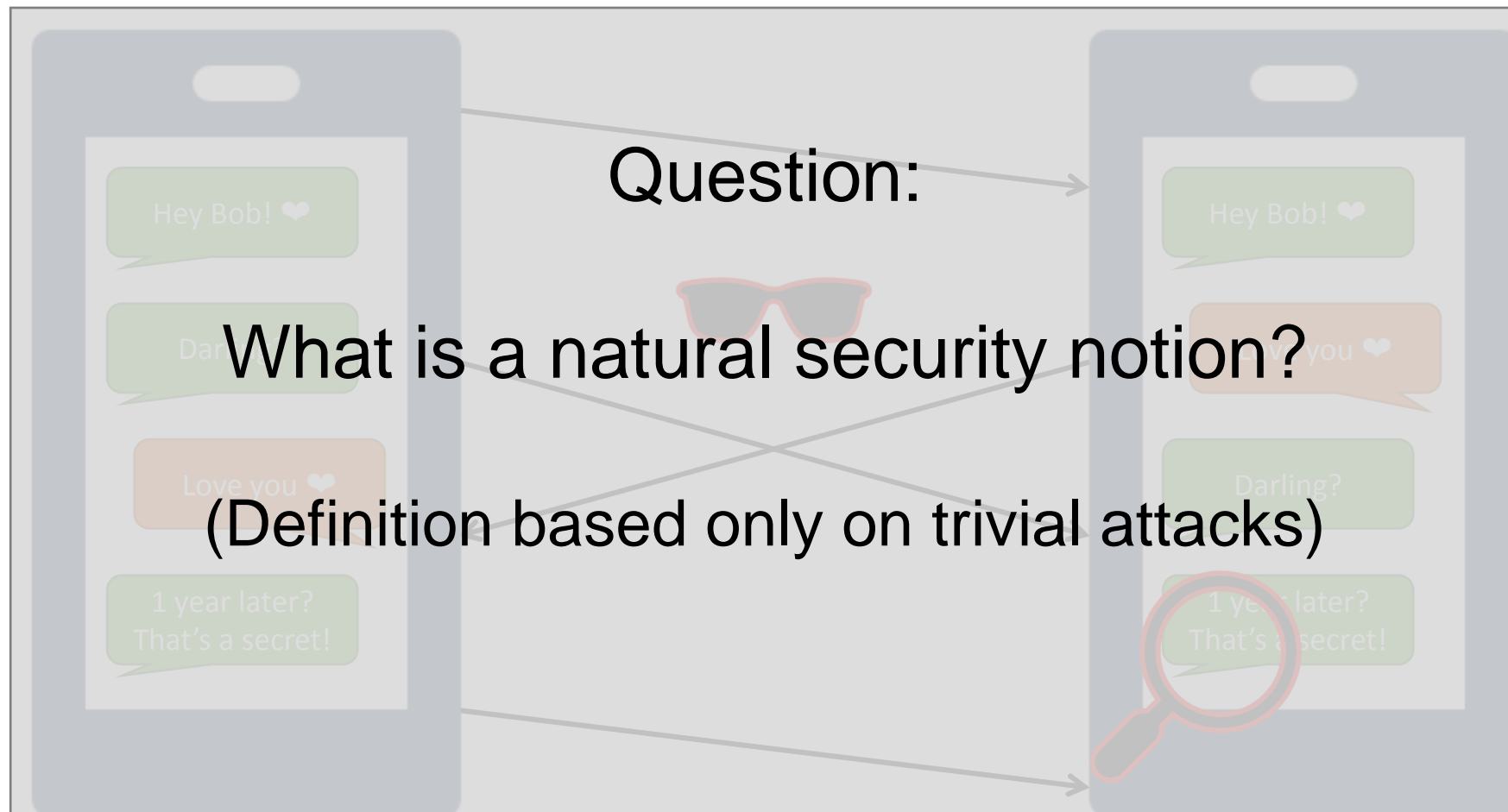
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- What is Ratcheting?  
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# Natural Security Notion for Ratcheting?

- Alice and Bob communicate
- Active adversary
- Long term communication
  - Local (full) state temporarily exposed

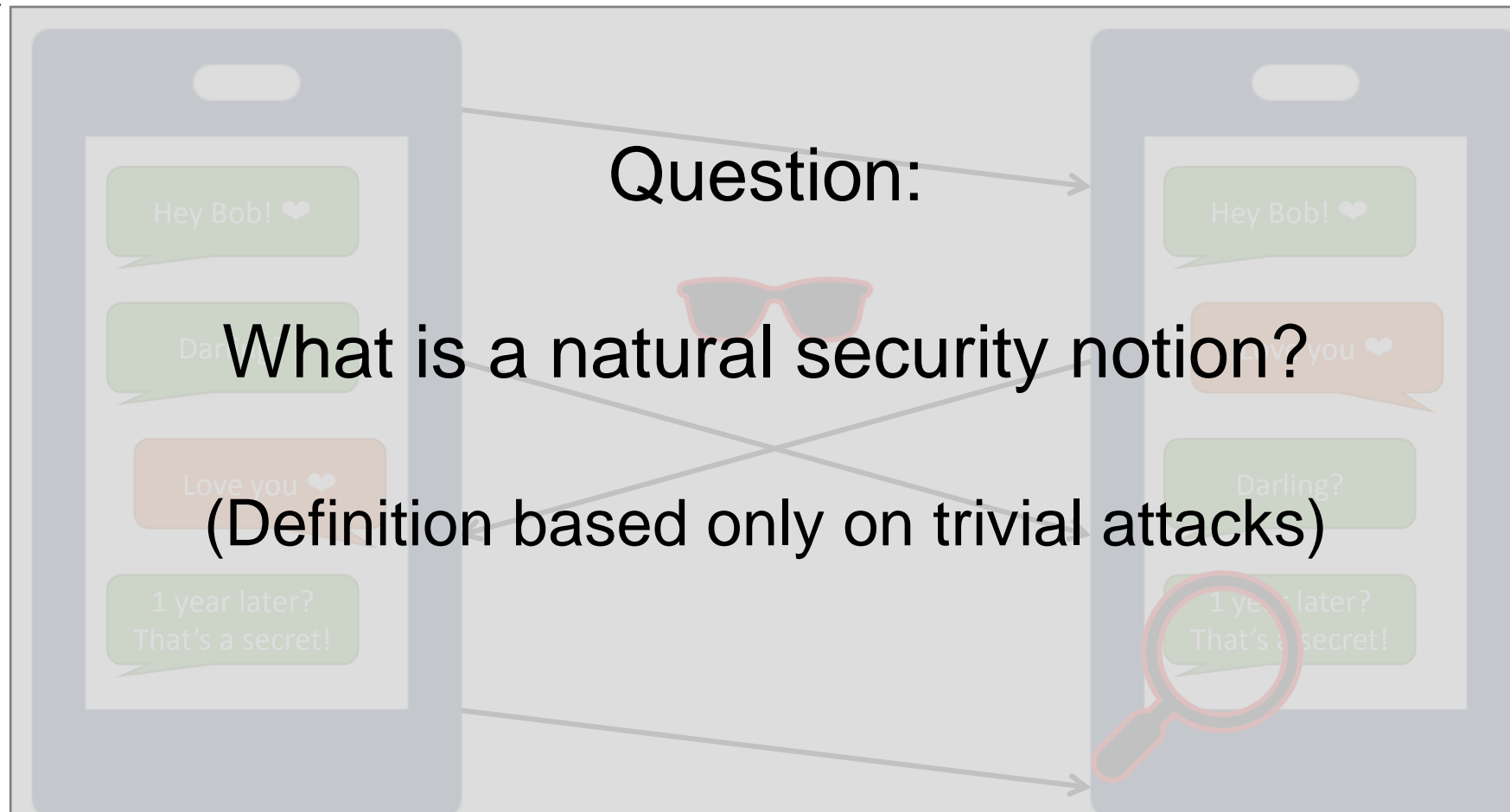


- What is Ratcheting?  
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# Natural Security Notion for Ratcheting?

- Natural security notion

- Definition based only on trivial attacks
- Bellare et al. on unidirectional communication C'17
  - Bob cannot be exposed



- What is Ratcheting?  
Modeling RKE  
Construction Intuition  
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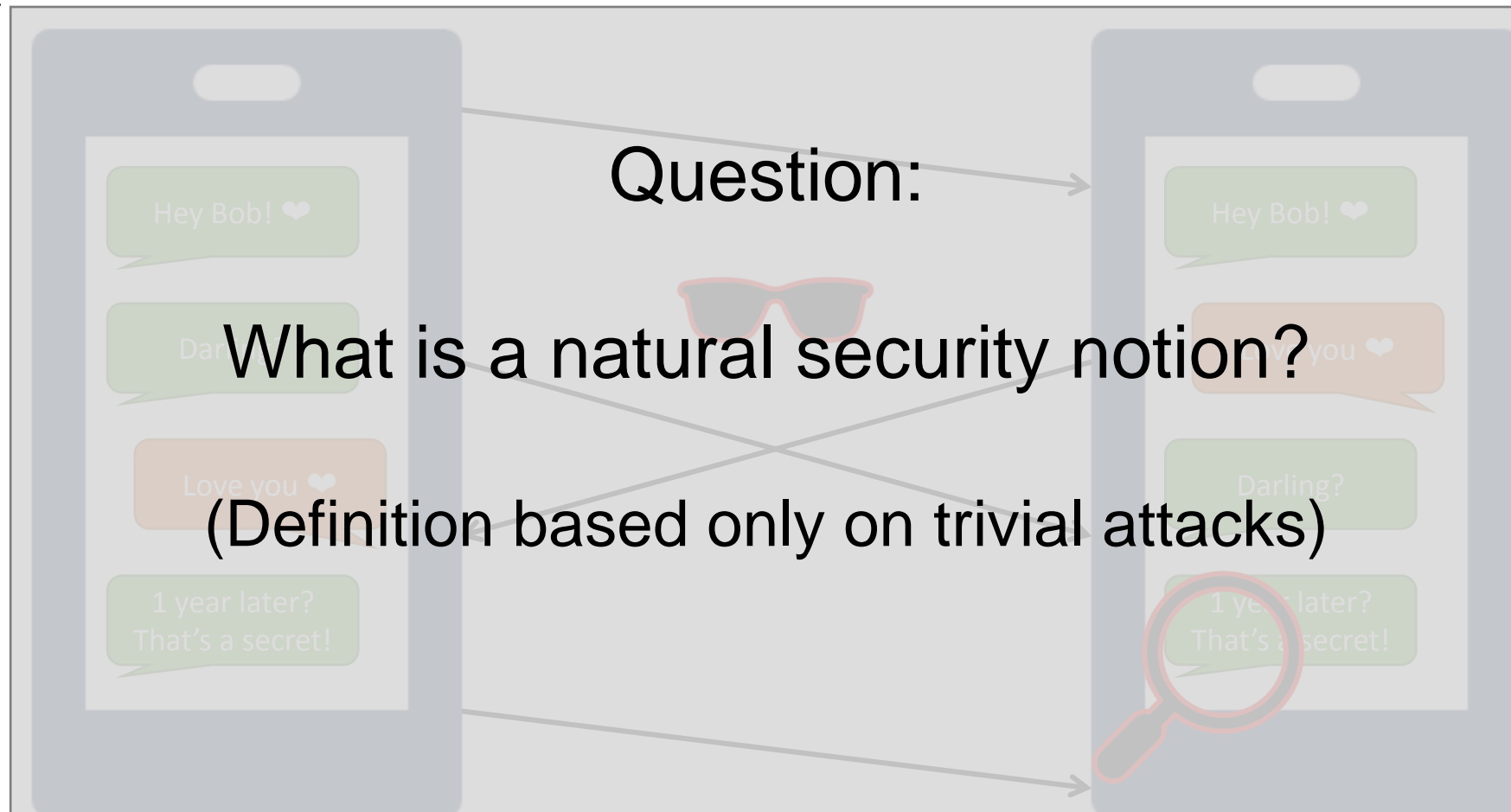
# Natural Security Notion for Ratcheting?

- Natural security notion

- Definition based only on trivial attacks
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  - Bob cannot be exposed

Our models require and constructions provide *full* security under:

- Asynchronous communication
- Exposure of both parties



# Agenda

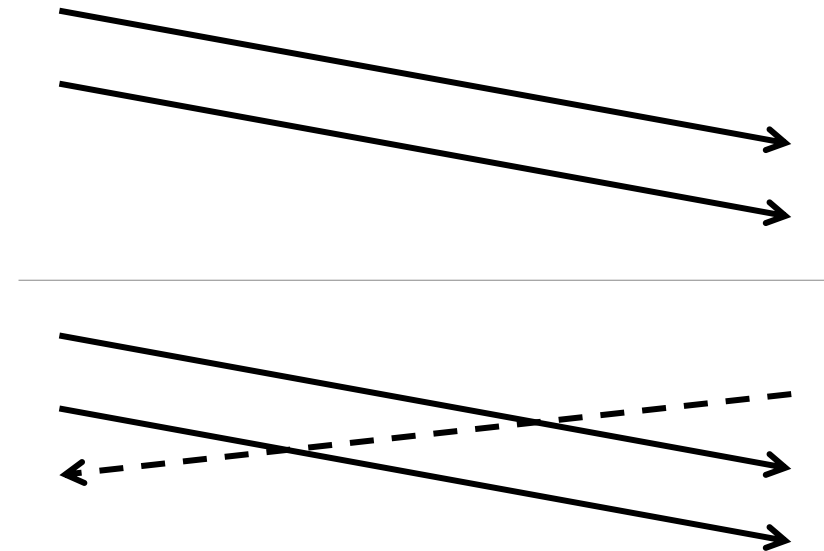
## 1. The Primitive Ratcheted Key Exchange

## 2. General Adversary Model

## 3. Unidirectional Ratcheting → Model and Construction

## 4. Sesquidirectional Ratcheting → Model and Construction

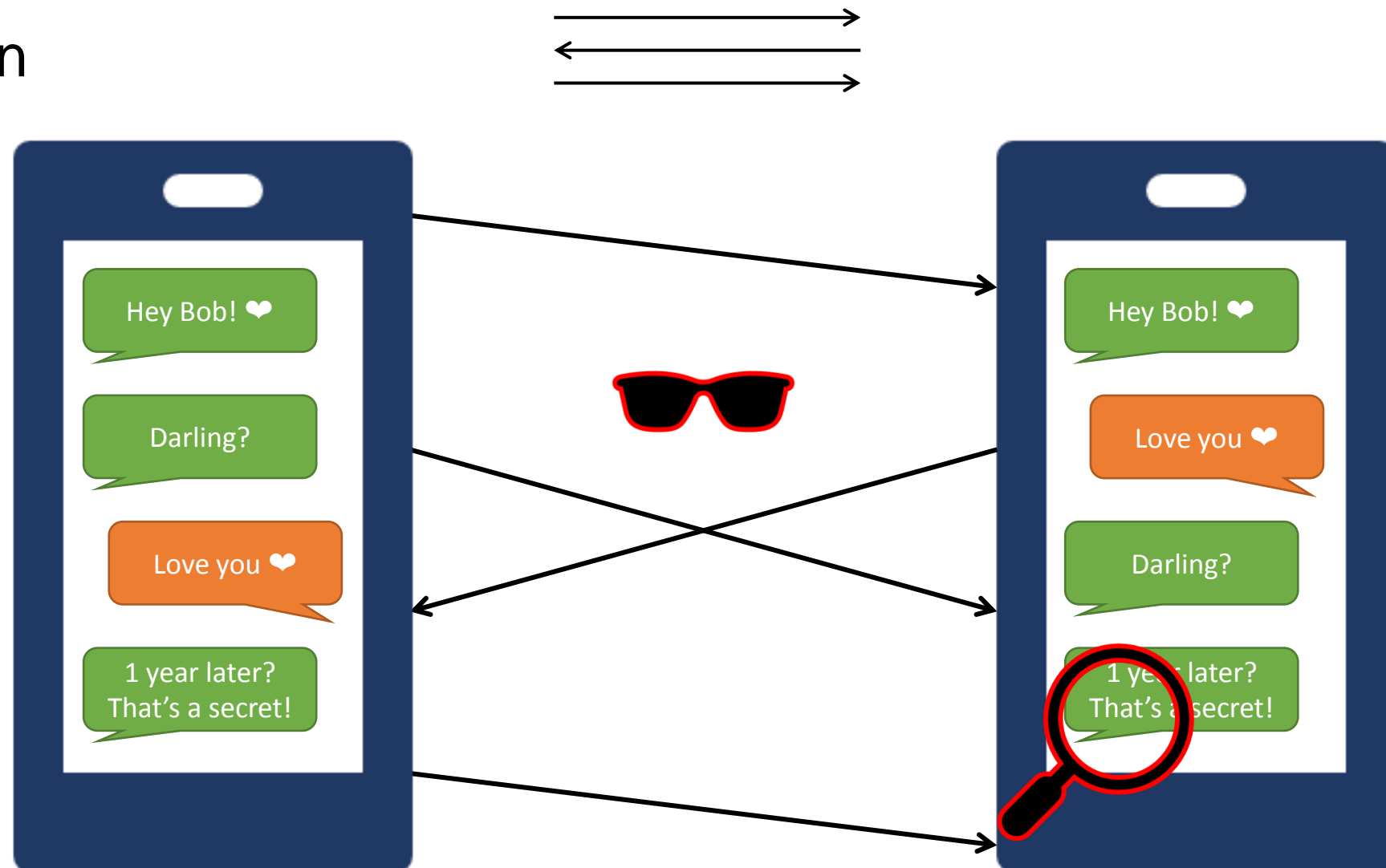
## 5. Results



- What is Ratcheting?  
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# Natural Security Notion for Ratcheting?

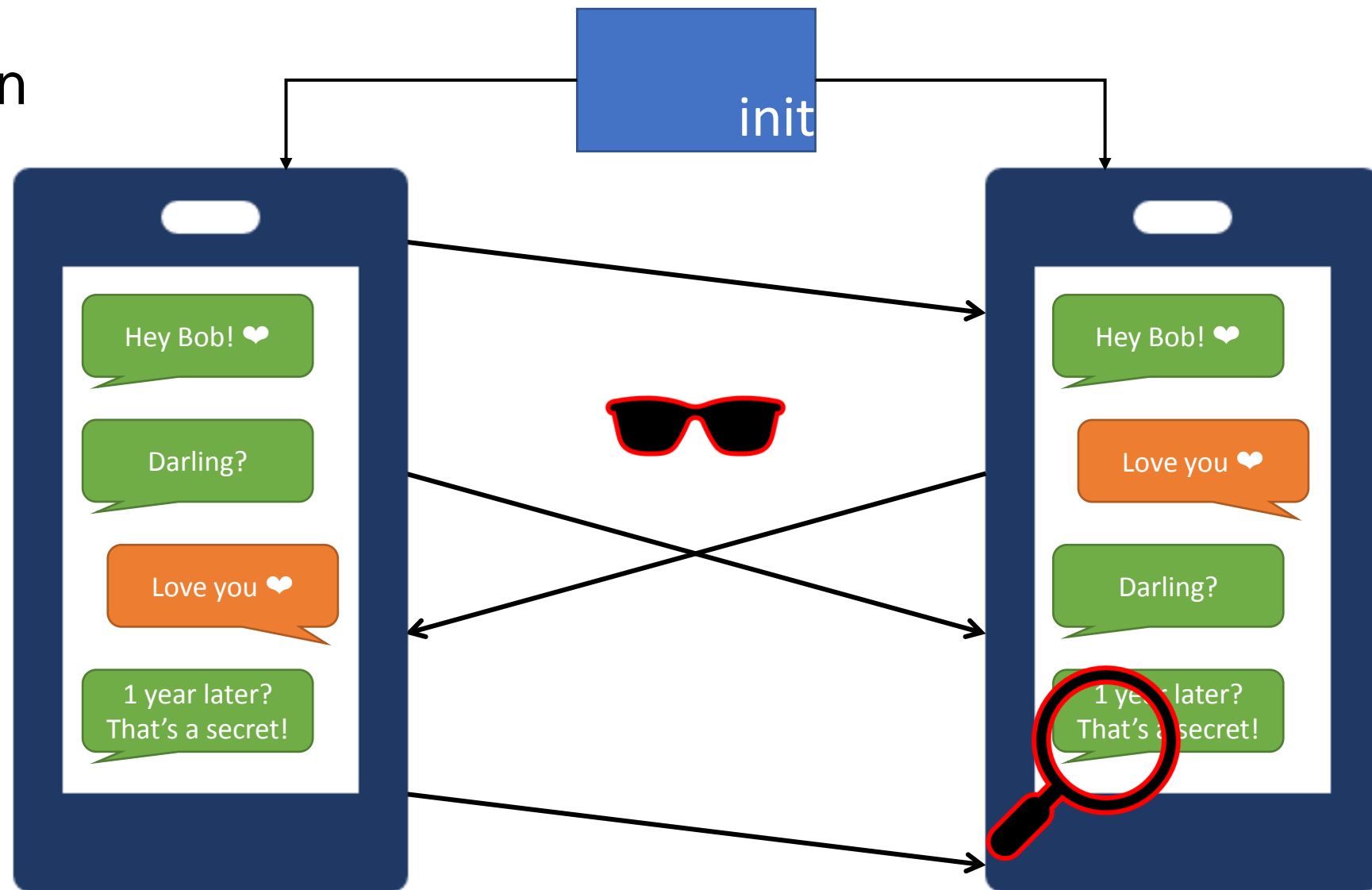
- Natural security notion
  - Definition based only on trivial attacks
- Syntax:
  - Initialization



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# Natural Security Notion for Ratcheting?

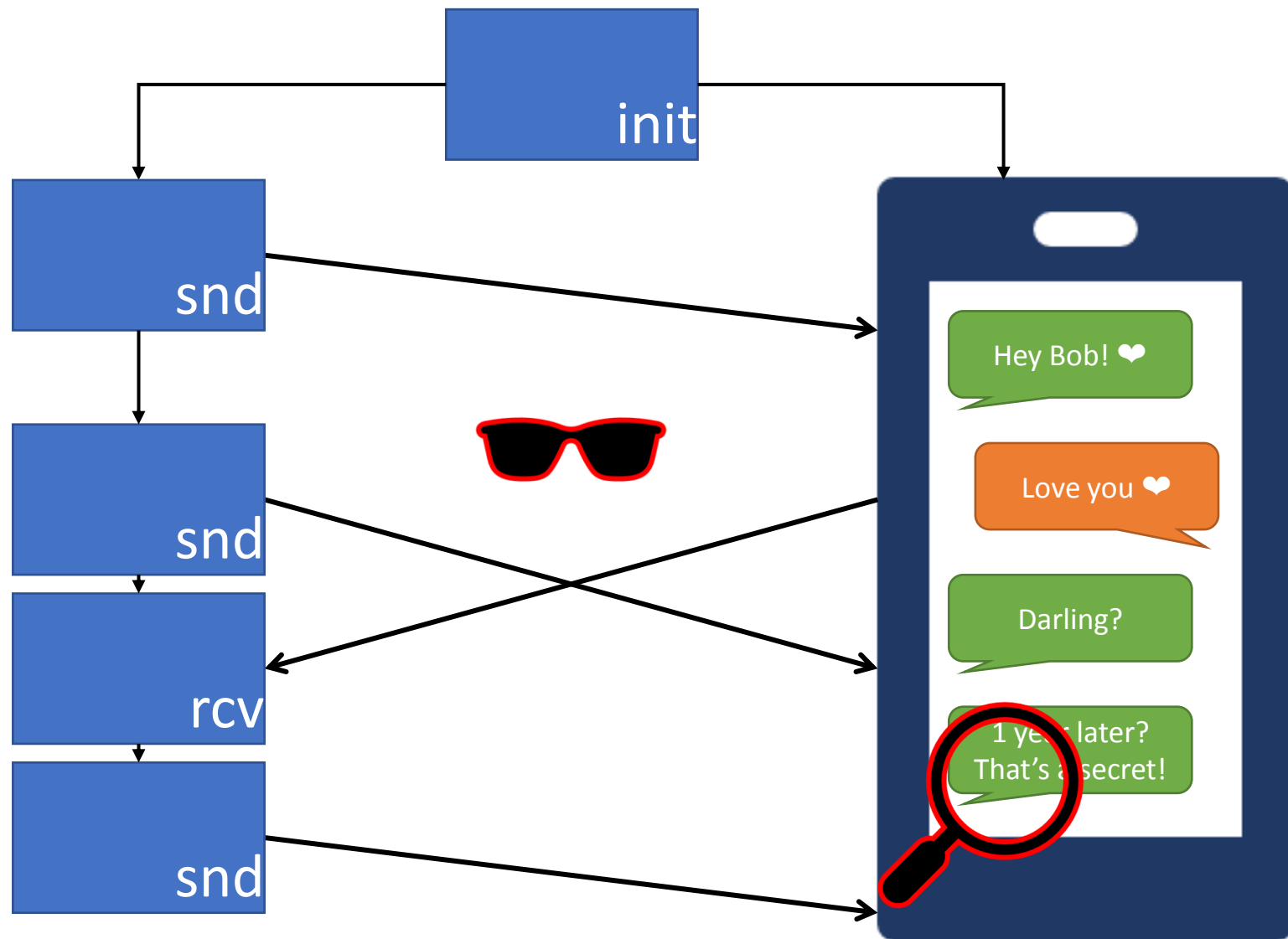
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# Natural Security Notion for Ratcheting?

- Natural security notion
  - Definition based only on trivial attacks
- Syntax:
  - Initialization
  - Sending & receiving

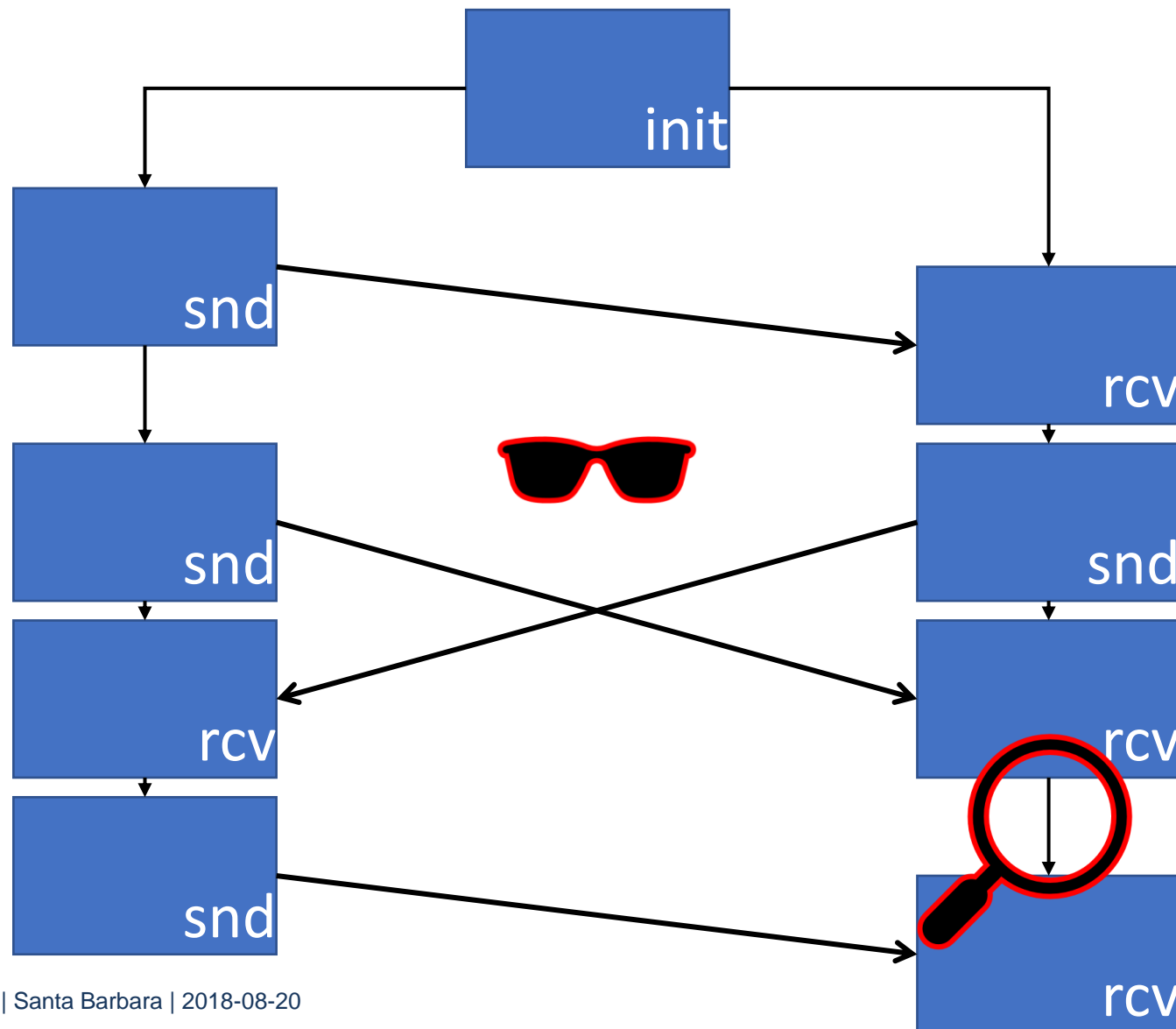




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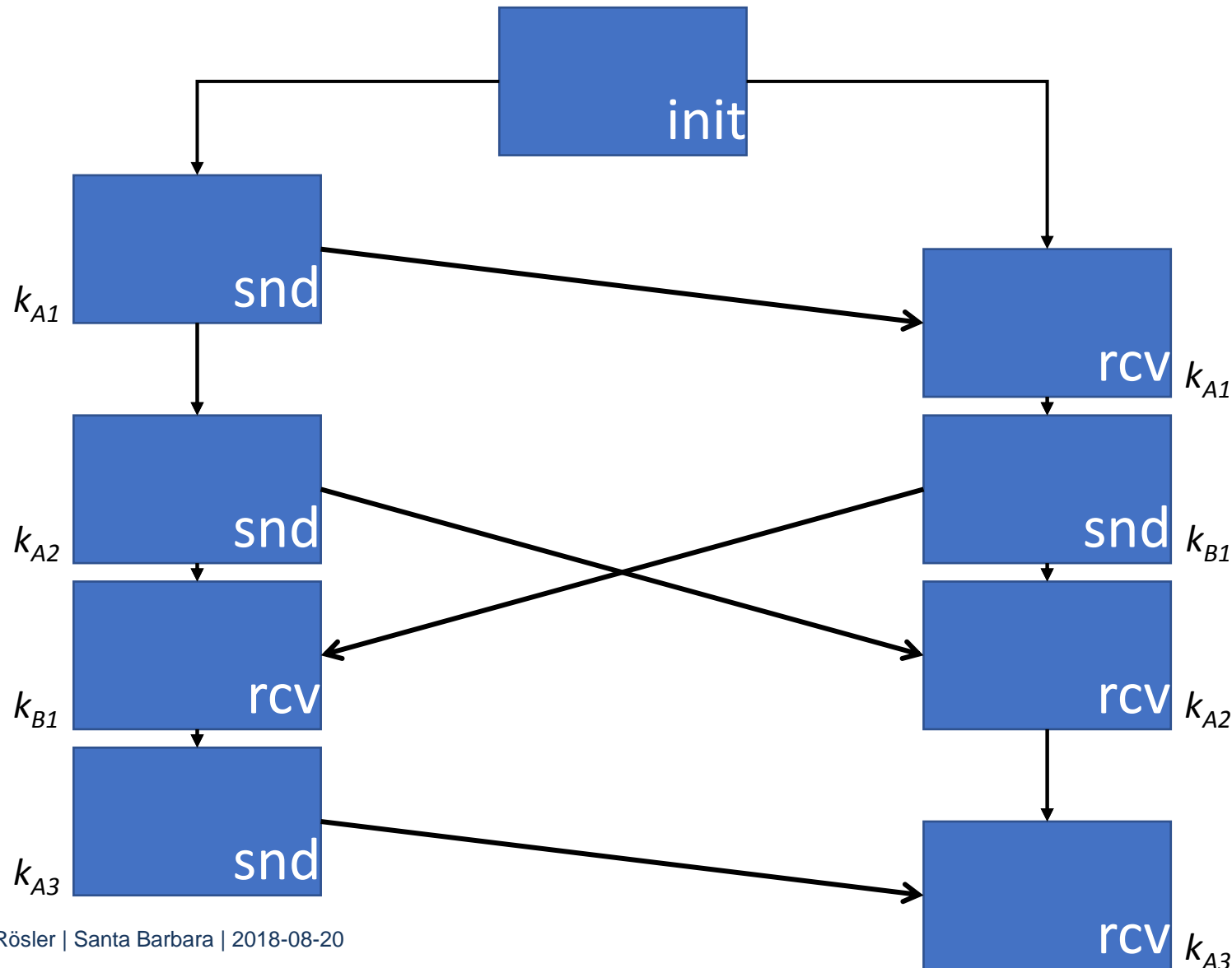


# Natural Security Notion for Ratcheting?

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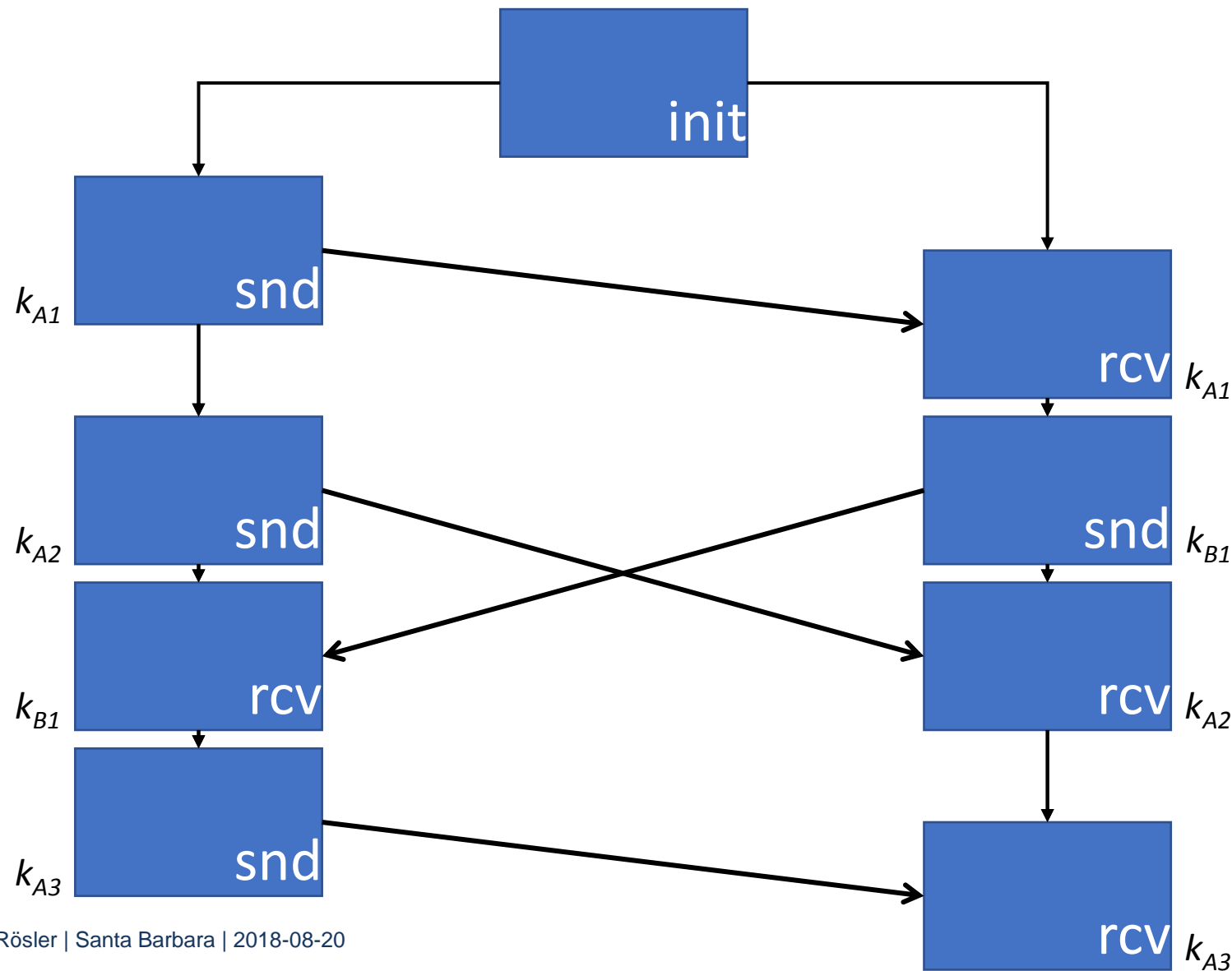
- Natural security notion
  - Definition based only on trivial attacks
- Syntax:
  - Initialization
  - Sending & receiving
  - Key exchange
    - Consecutive establishment of keys in session

≠ *Authenticated key exchange!*



# Natural Security Notion for Ratcheting?

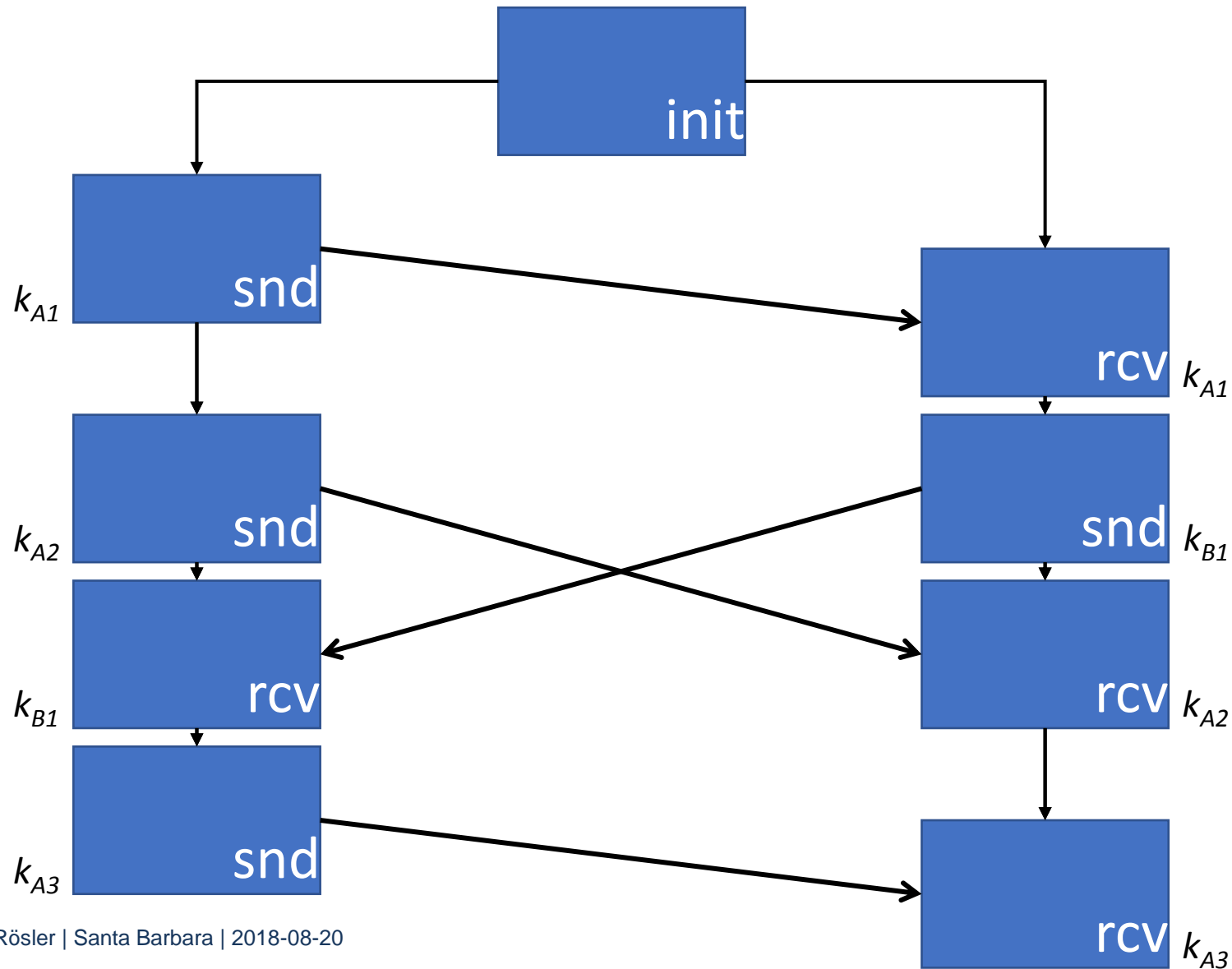
- Natural security notion
  - Definition based only on trivial attacks
- Syntax:
  - Initialization
  - Sending & receiving
  - Key exchange
    - Composition in Bellare et al. C'17



# Three Variants of Ratcheting

- What is Ratcheting?  
Modeling RKE  
Construction Intuition  
Results

- Bidirectional ratcheting is complicated  
→ Understand its components



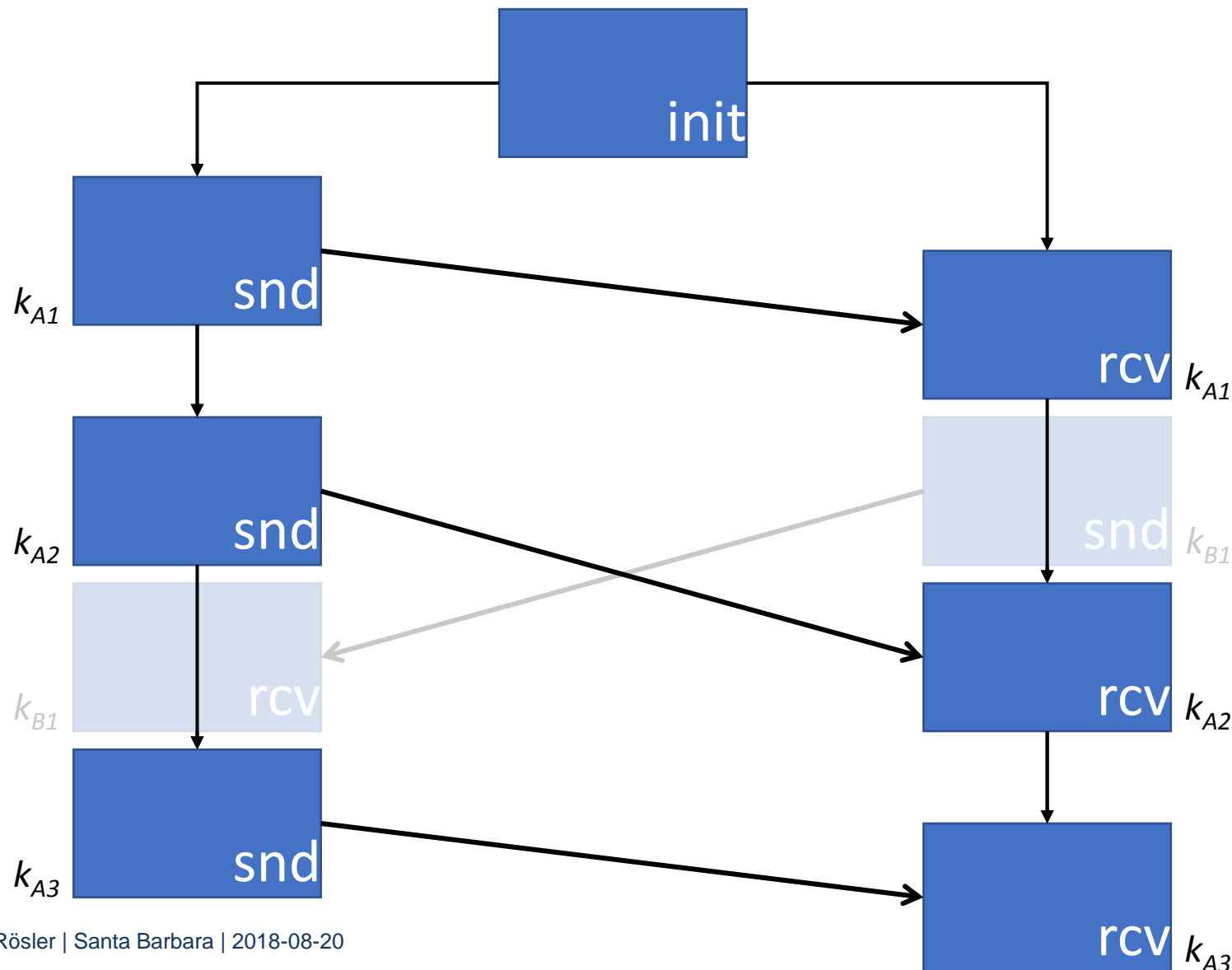
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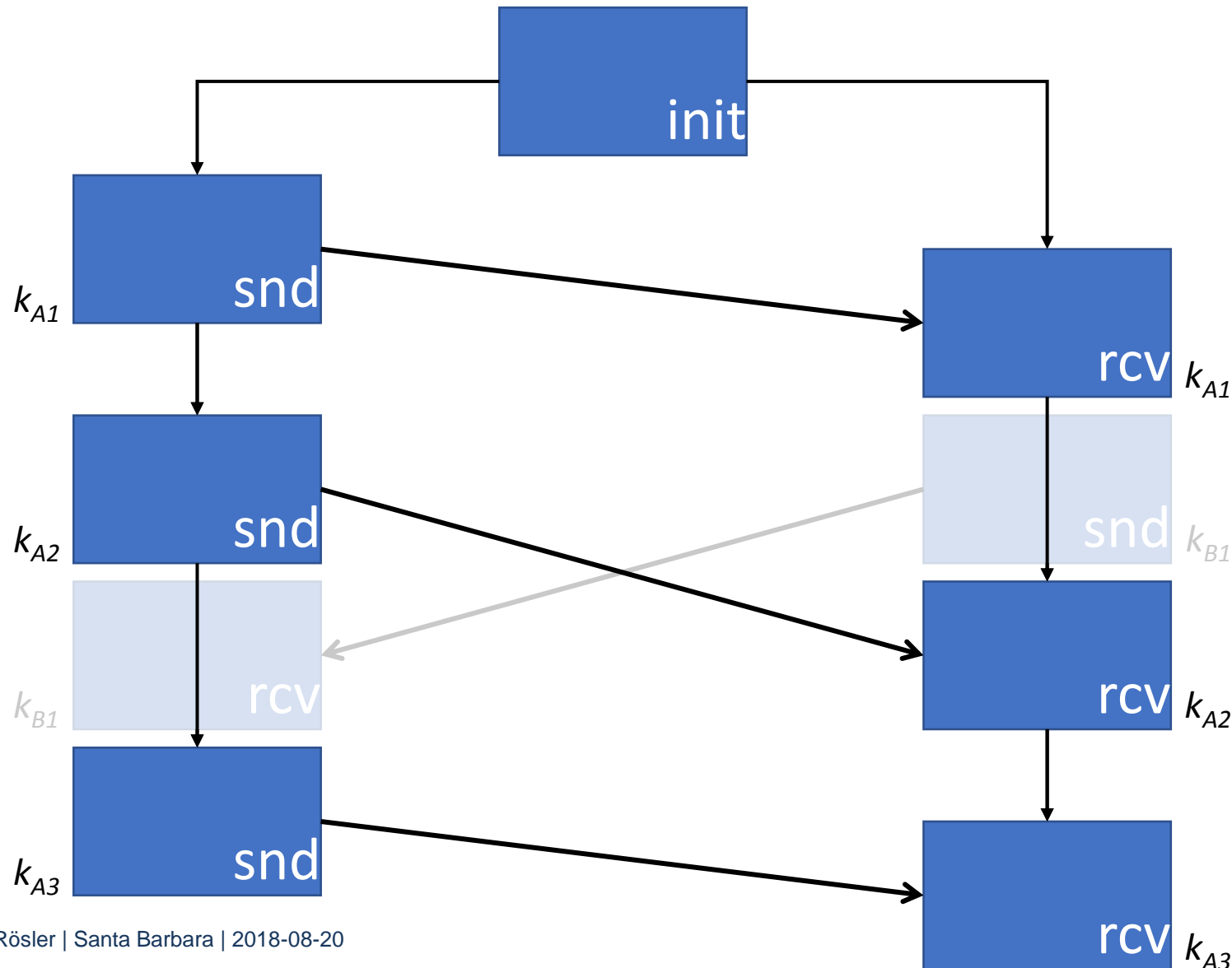
- Unidirectional key establishment



# Three Variants of Ratcheting

- What is Ratcheting?  
Modeling RKE  
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Results

- Bidirectional ratcheting is complicated
- Understand its components:
  - Unidirectional key establishment
  - Alice initiates computation of new key
  - Bob does not respond



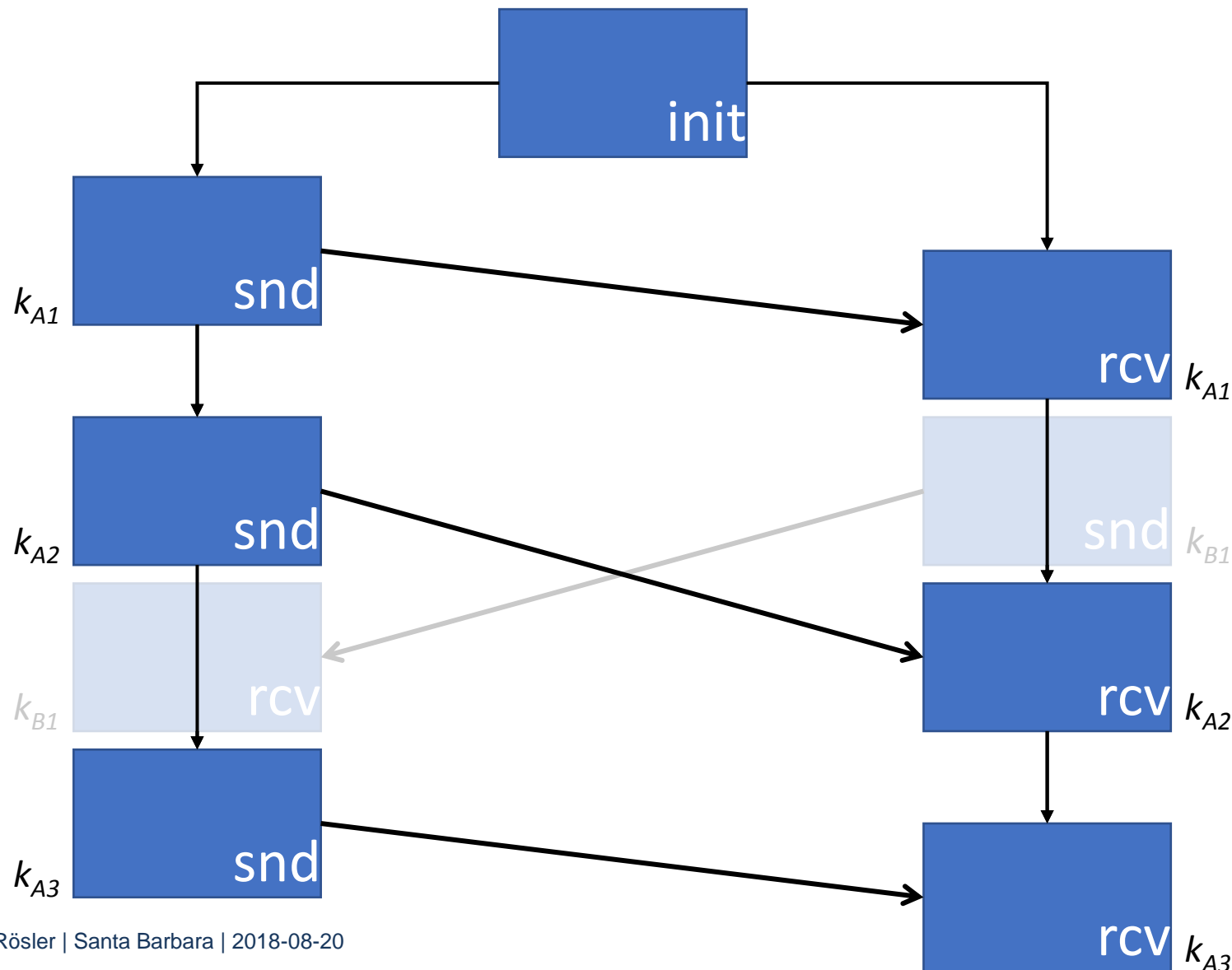
# Three Variants of Ratcheting

- What is Ratcheting?  
Modeling RKE  
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Results

- Bidirectional ratcheting is complicated

→ Understand its components:

- Unidirectional ratcheted key exchange (RKE)



# Three Variants of Ratcheting

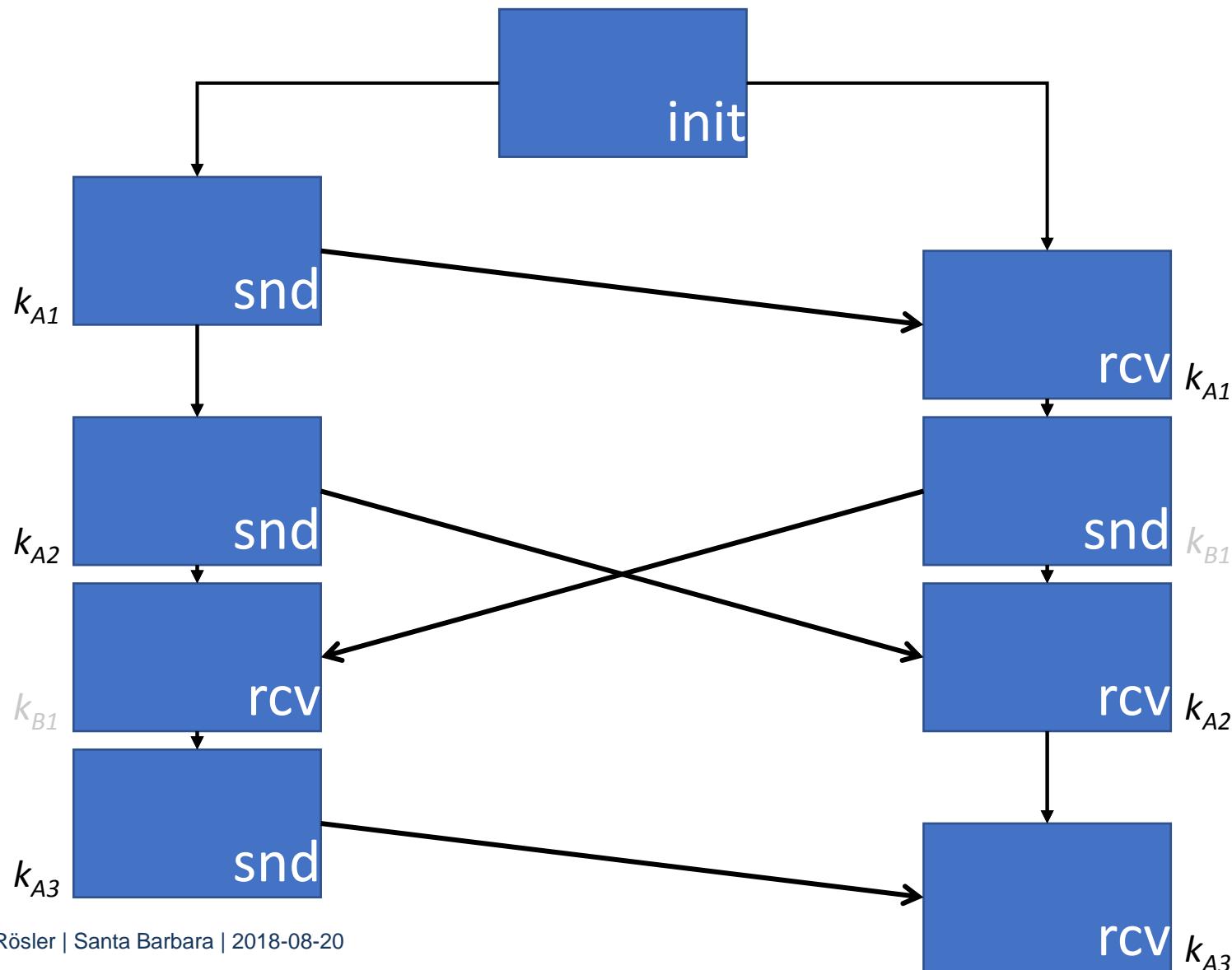
- What is Ratcheting?  
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Results

• Bidirectional ratcheting is complicated

→ Understand its components:

- Unidirectional RKE
- Sesquidirectional RKE
- Bob contributes (but cannot establish keys)
- Adds security

(sesqui = 1.5)





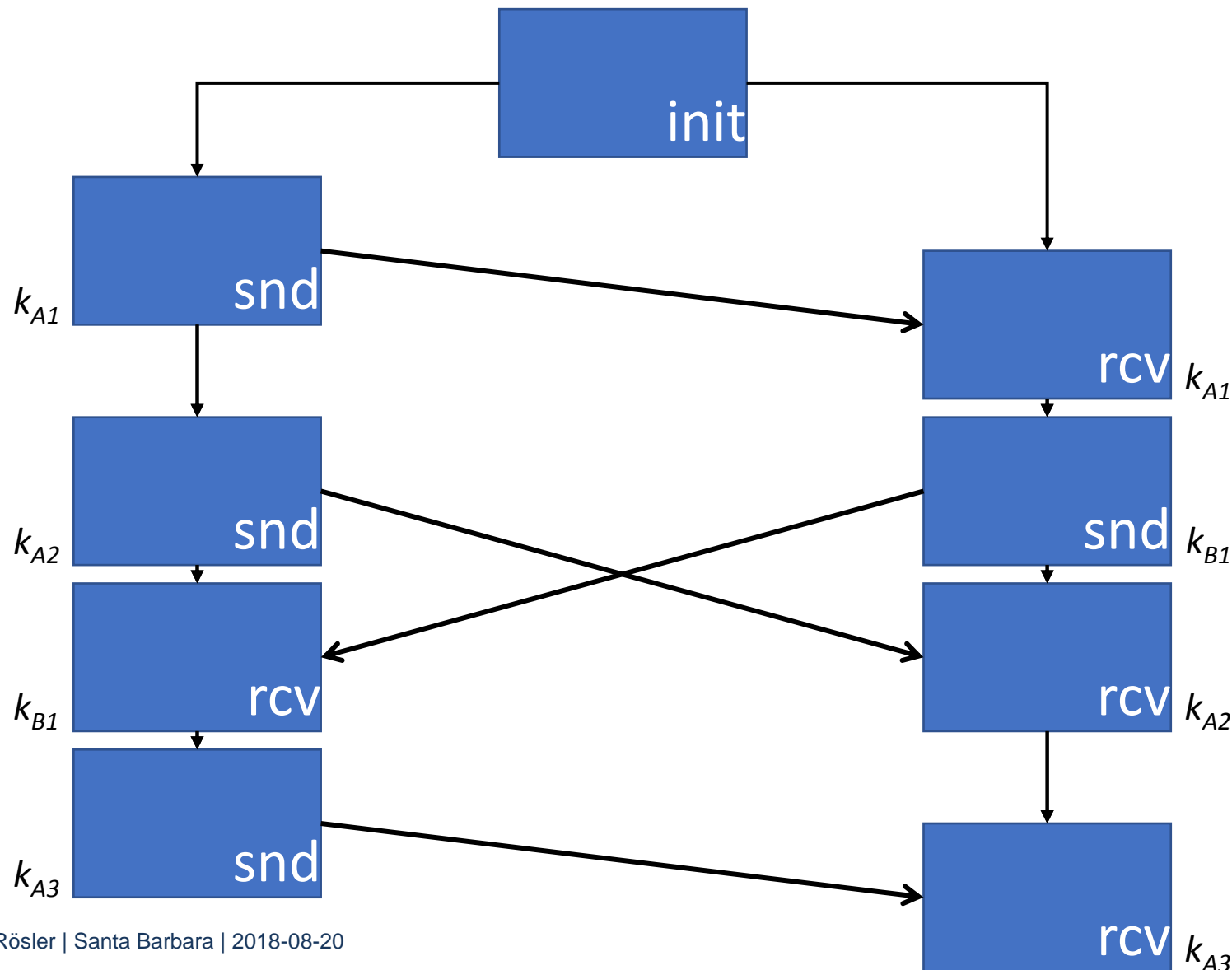
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• Bidirectional ratcheting is complicated

→ Understand its components:

- Unidirectional RKE
- Sesquidirectional RKE
- Symmetric roles



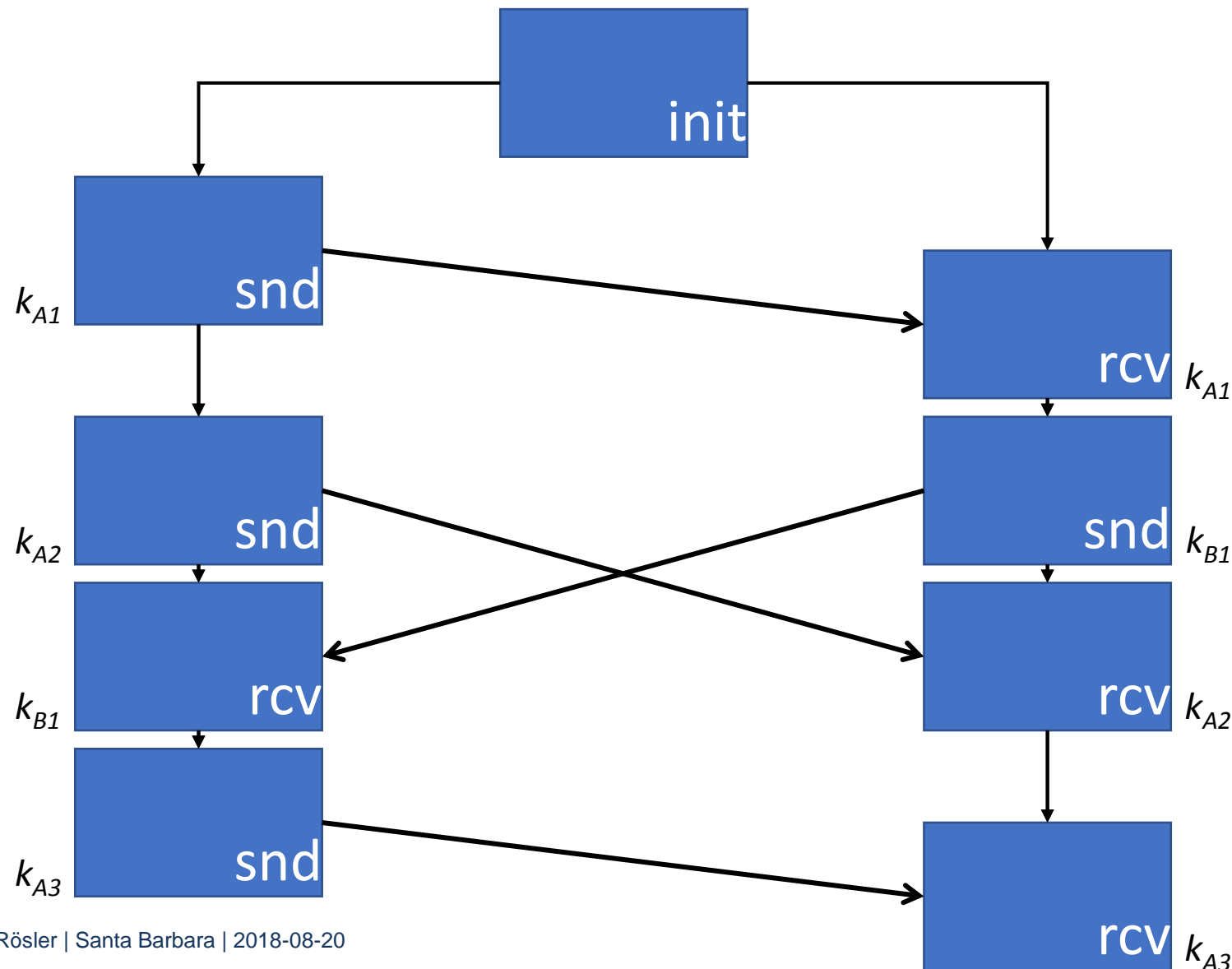
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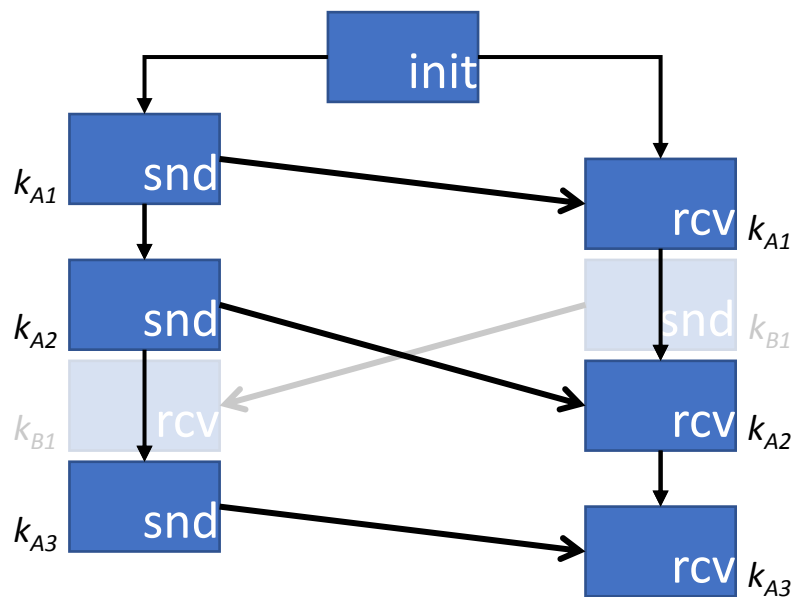
- Unidirectional RKE
- Sesquidirectional RKE
- Symmetric roles
- Bidirectional RKE = 2x Sesquid. RKE (extended version)



- What is Ratcheting?  
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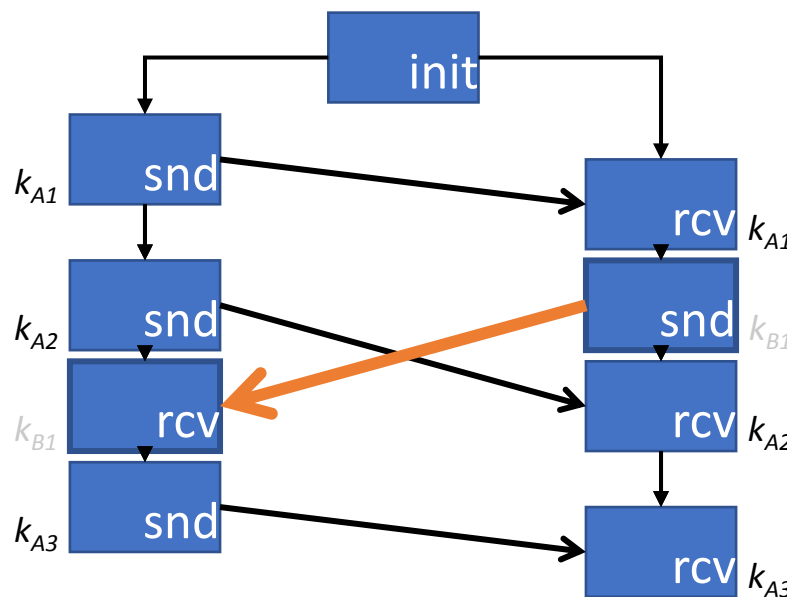
# Three Variants of Ratcheting

## Unidirectional RKE (+ Exposure of Bob)



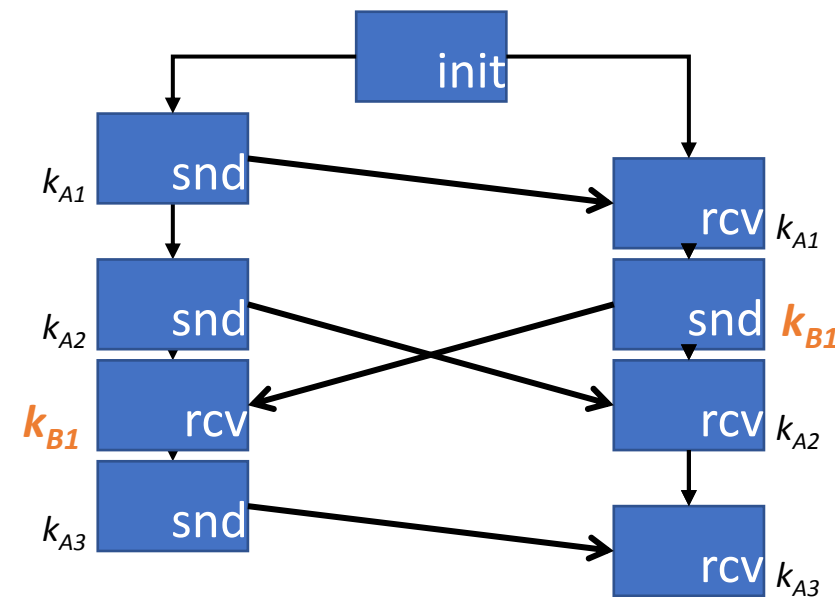
No responses  
from Bob

## Sesquidirectional RKE



Bob's responses  
only help to recover

## Bidirectional RKE



Symmetric roles  
(extended version)

# Agenda

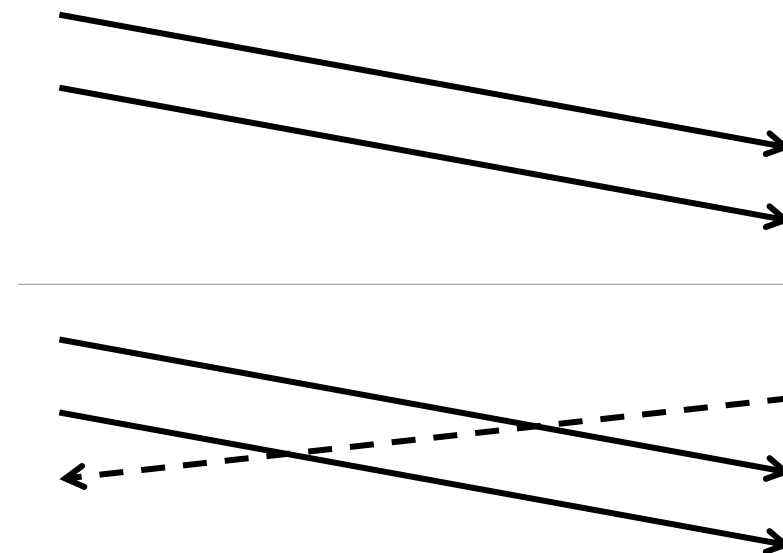
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**2. General Adversary Model**

3. Unidirectional Ratcheting  
→ Model and Construction

4. Sesquidirectional Ratcheting  
→ Model and Construction

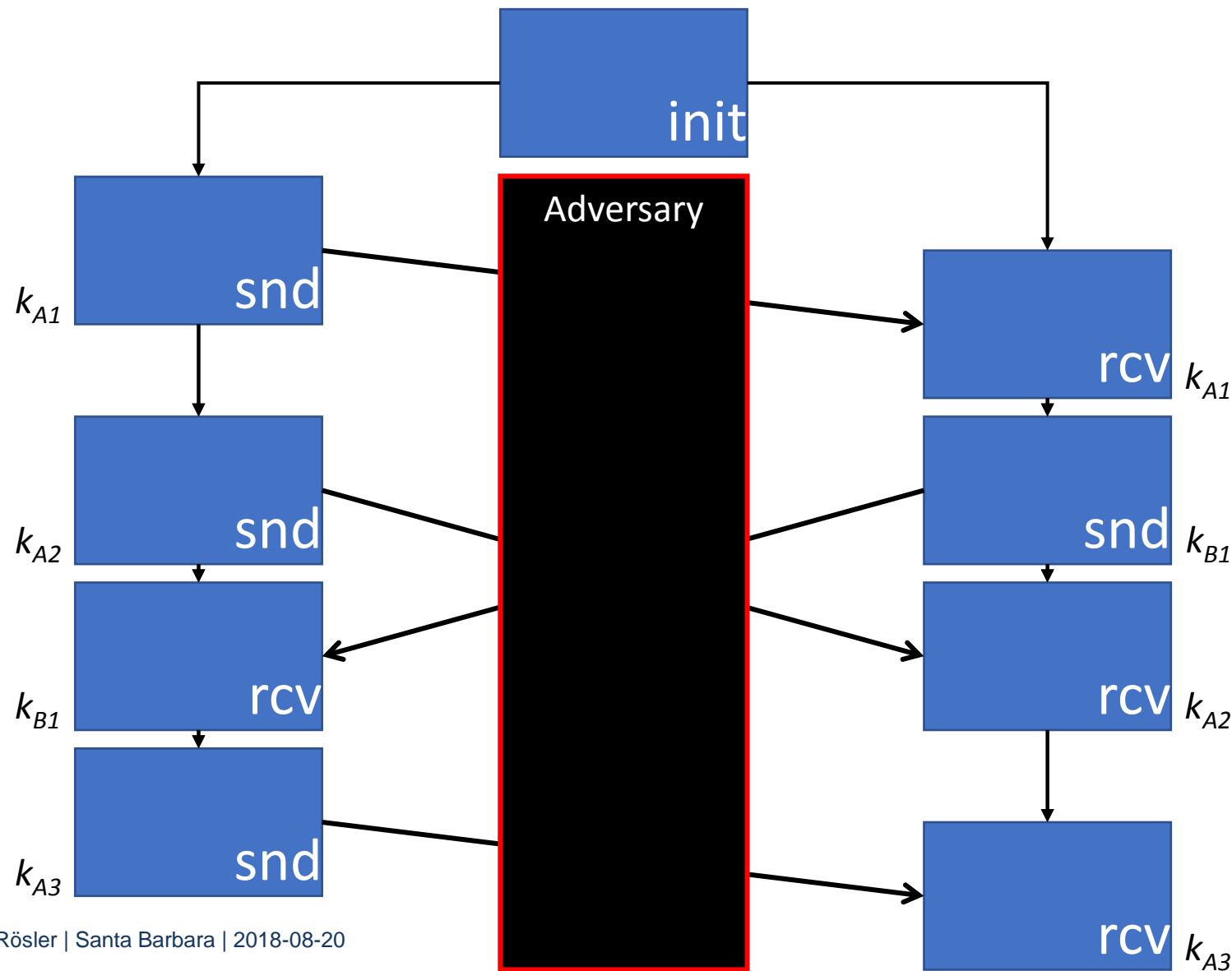
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# Modeling Ratcheted Key Exchange

- What is Ratcheting?
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- Construction Intuition
- Results

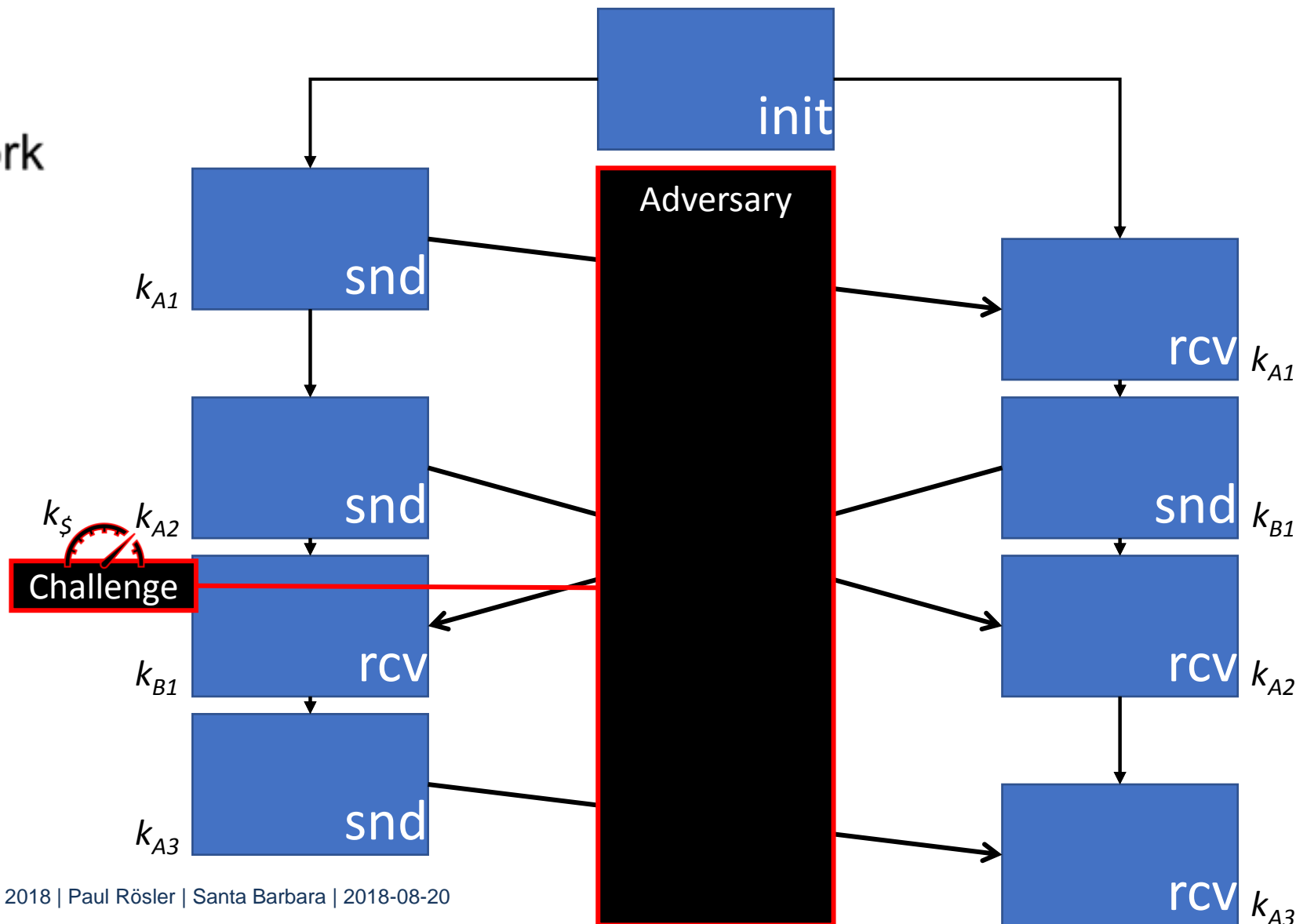
- Active adversary
  - Control whole network traffic



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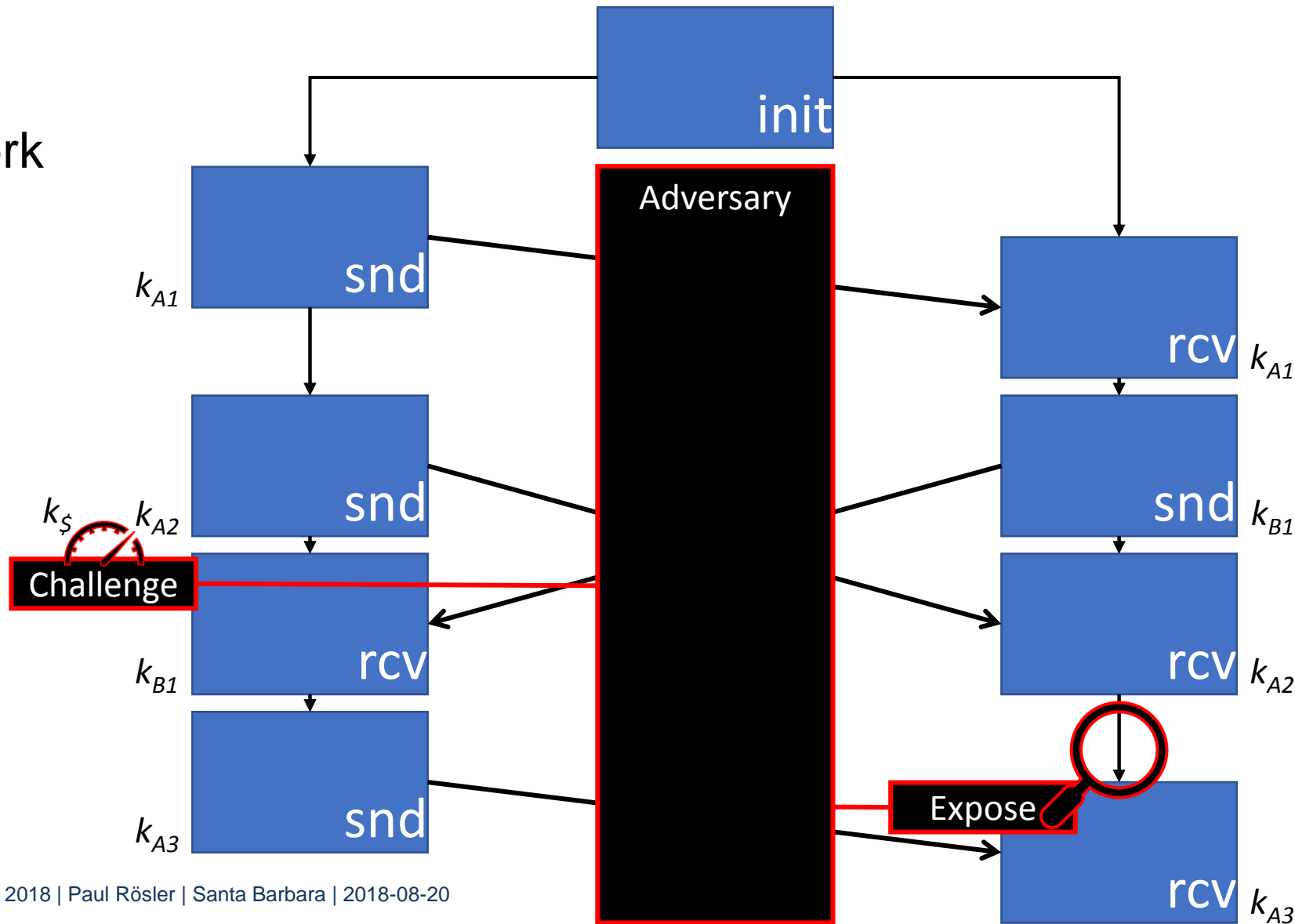
- Active adversary
    - Control whole network traffic
  - Analyze key indistinguishability
    - Multi-challenge real or random key
- Guess bit  $b \in \{0,1\}$



# Modeling Ratcheted Key Exchange

What is Ratcheting?  
 Modeling RKE  
 Construction Intuition  
 Results

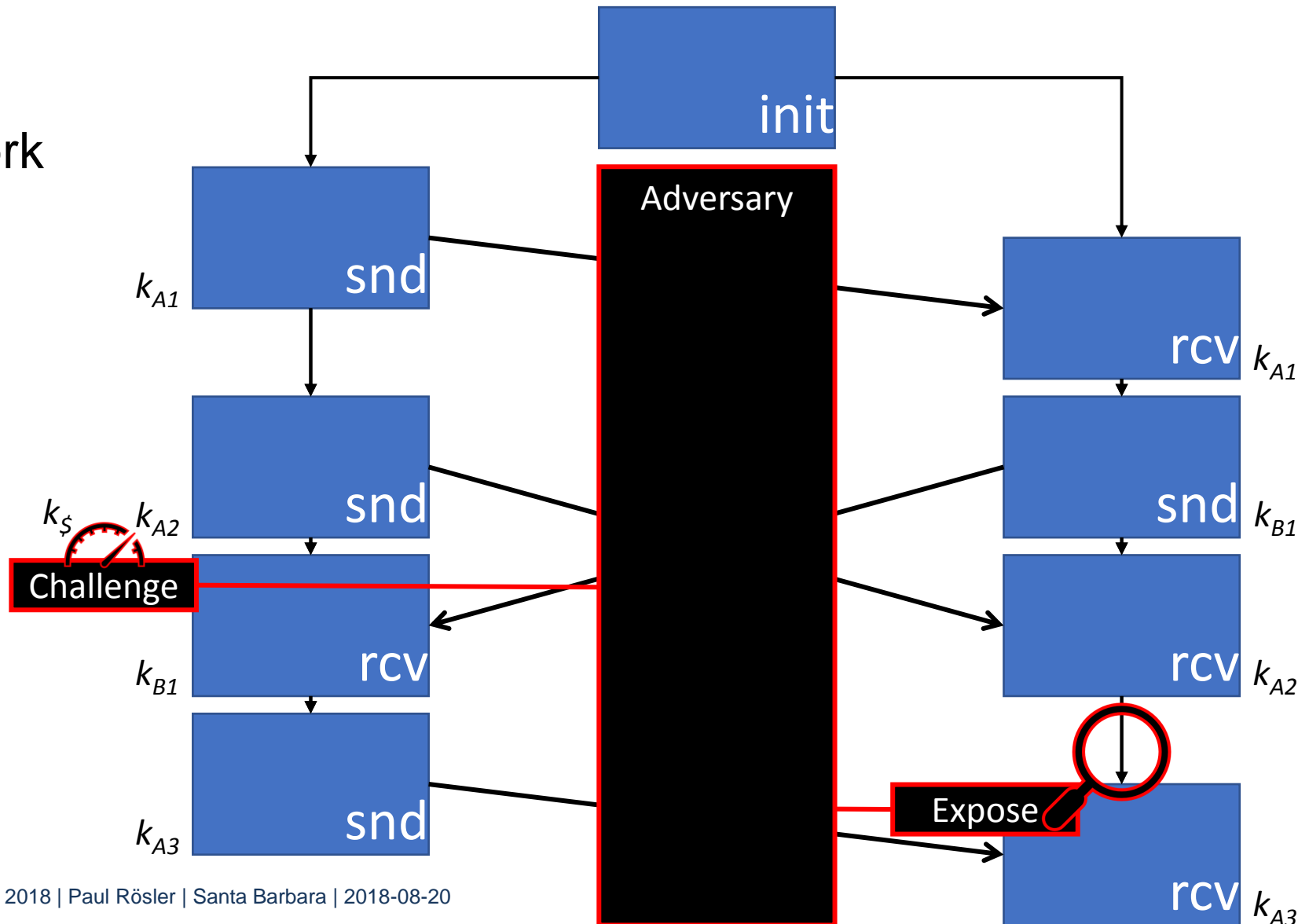
- Active adversary
  - Control whole network traffic
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  - Multi-challenge real or random key
- Model exposures of local state



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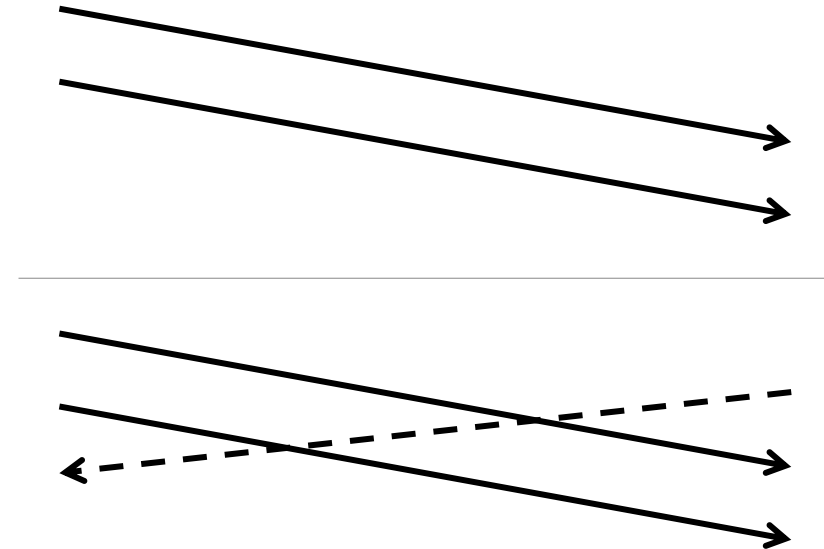
- Active adversary
  - Control whole network traffic
- Analyze key indistinguishability
  - Multi-challenge real or random key
- Model exposures of local state
- Single session
- Init abstracted





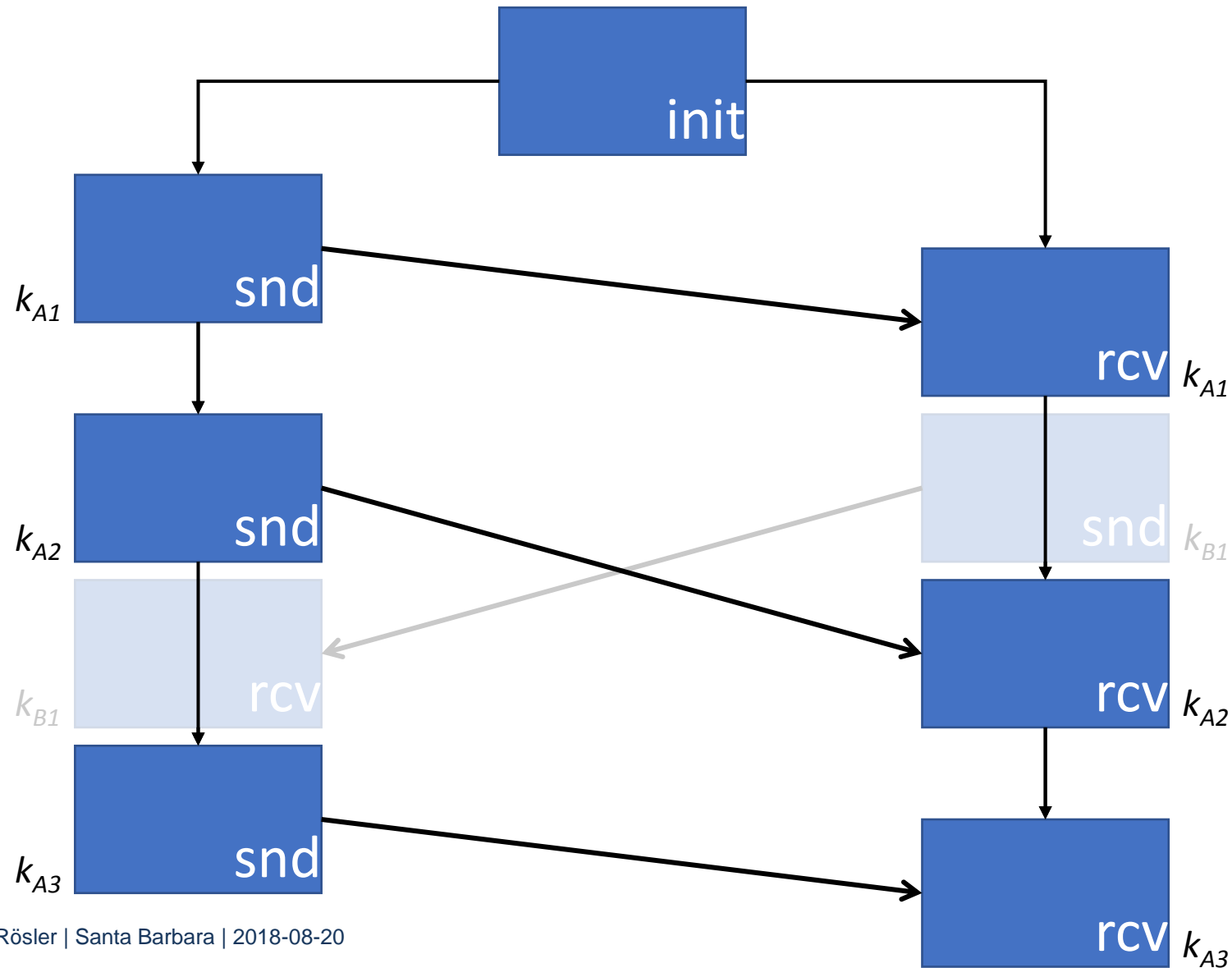
# Agenda

1. The Primitive Ratcheted Key Exchange
2. General Adversary Model
3. **Unidirectional Ratcheting**  
→ **Model** and Construction
4. Sesquidirectional Ratcheting  
→ Model and Construction
5. Results



# Modeling Unidirectional RKE

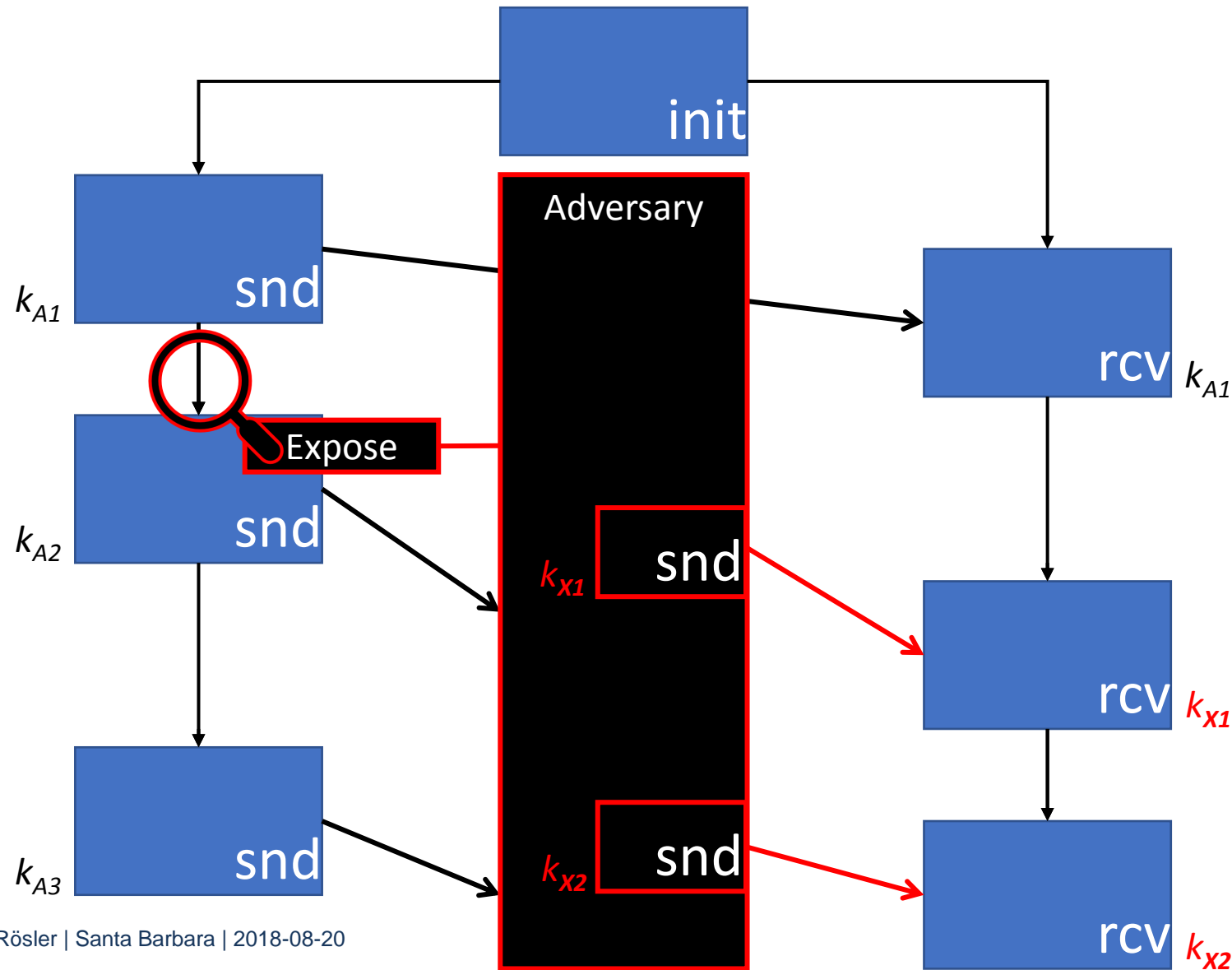
- What is Ratcheting?
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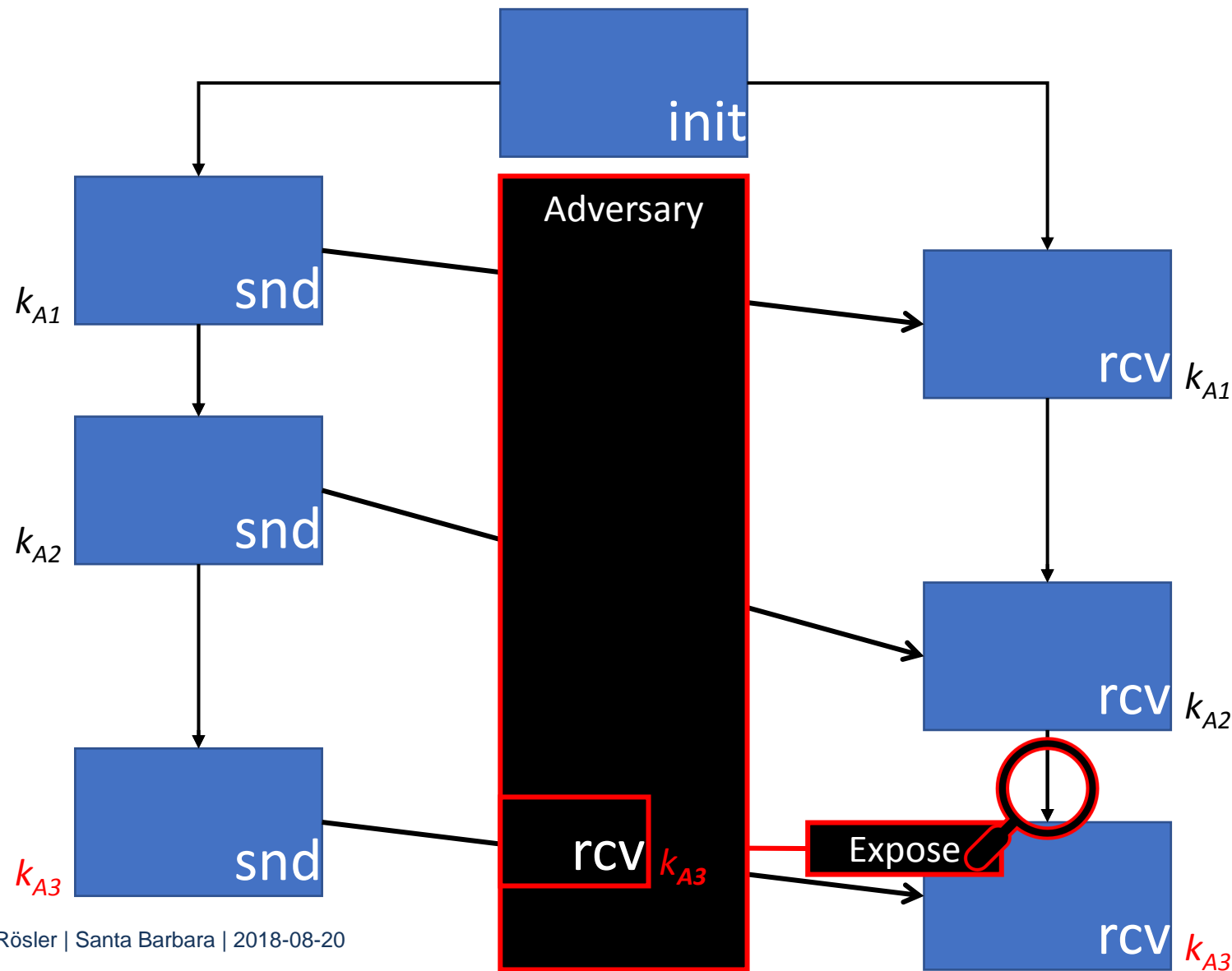
- Impersonation  
⇒ No future Challenge on Bob



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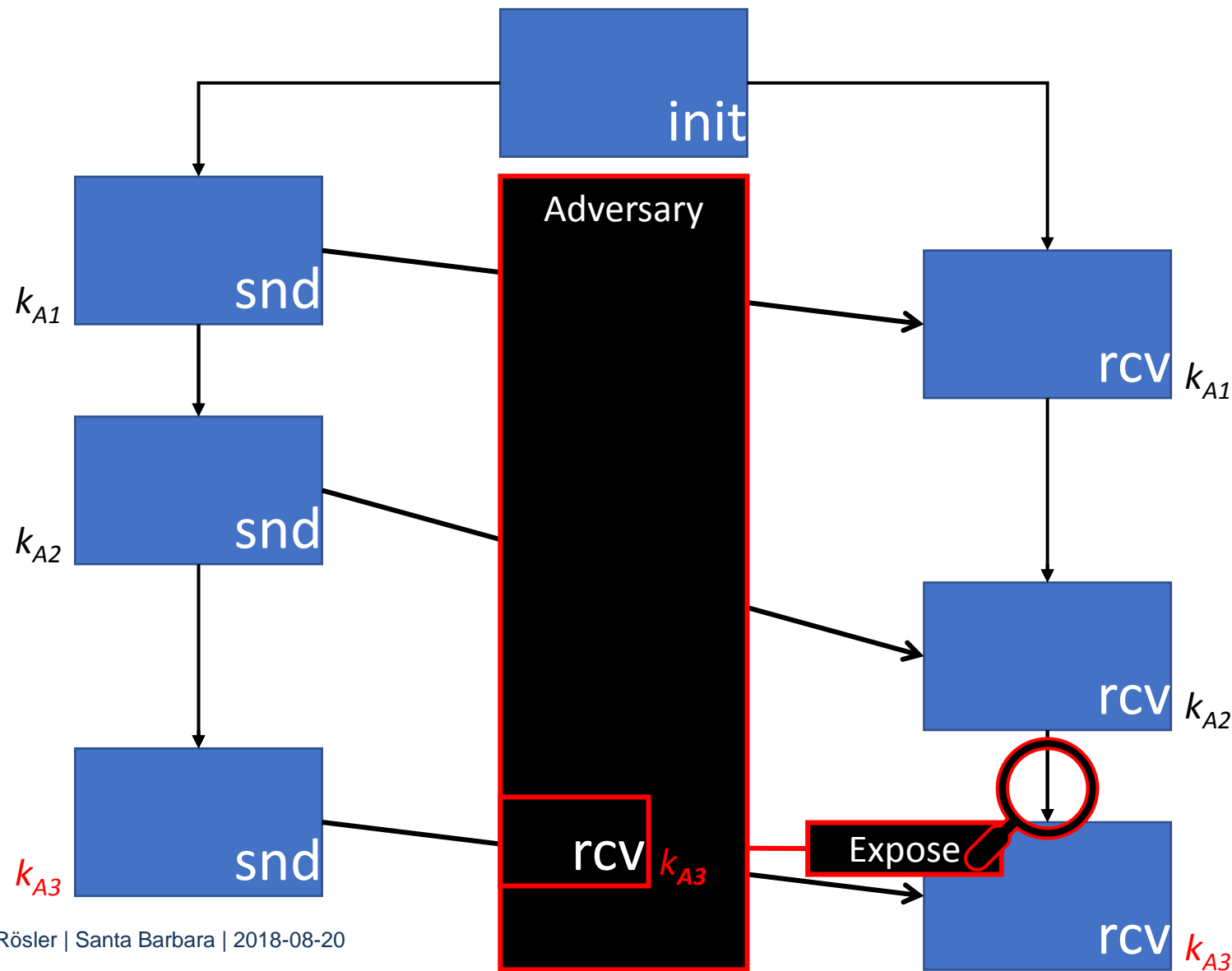
- Impersonation  
⇒ No future Challenge on Bob
- Expose Bob  
→ Allowed in our model



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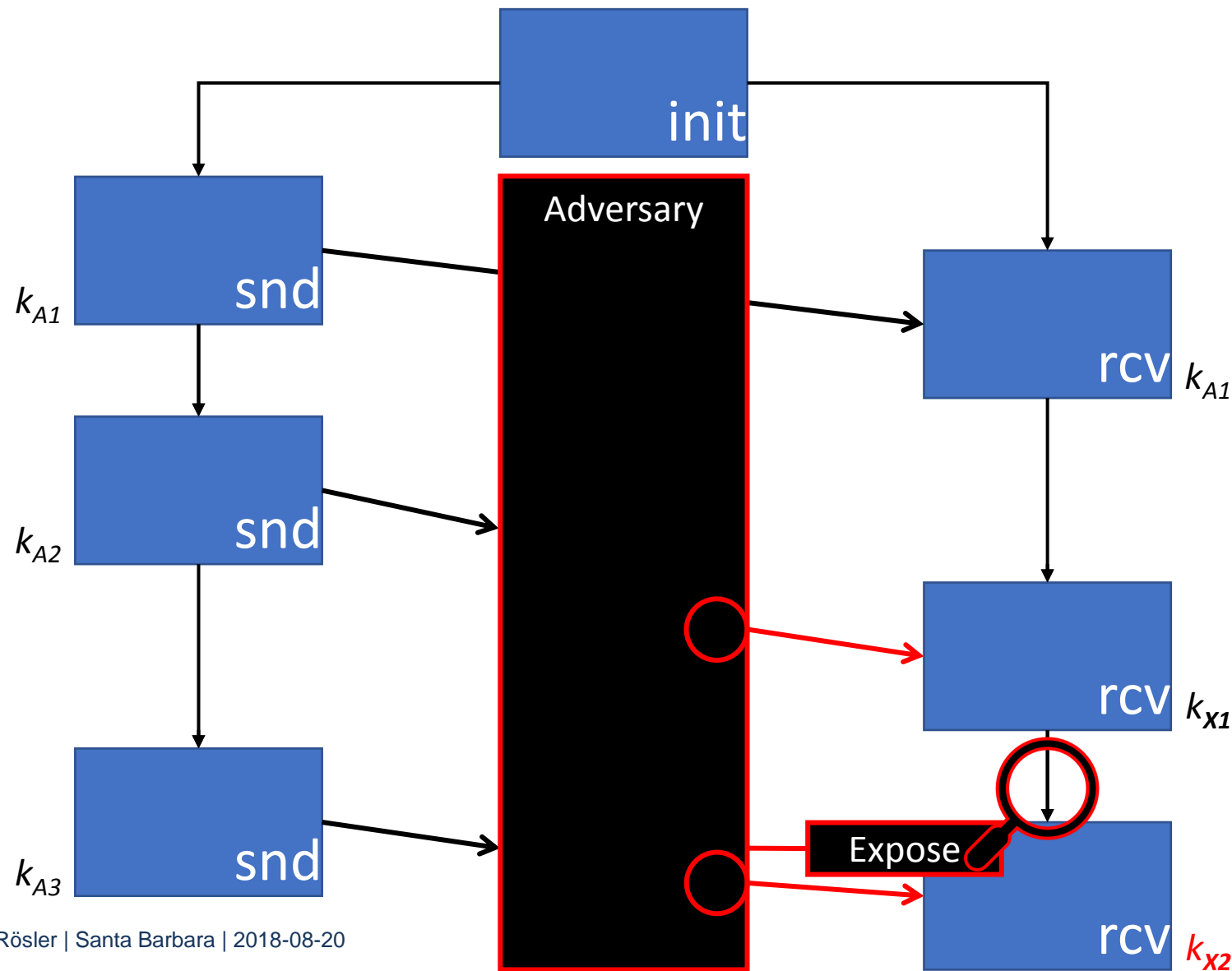
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- Expose Bob  
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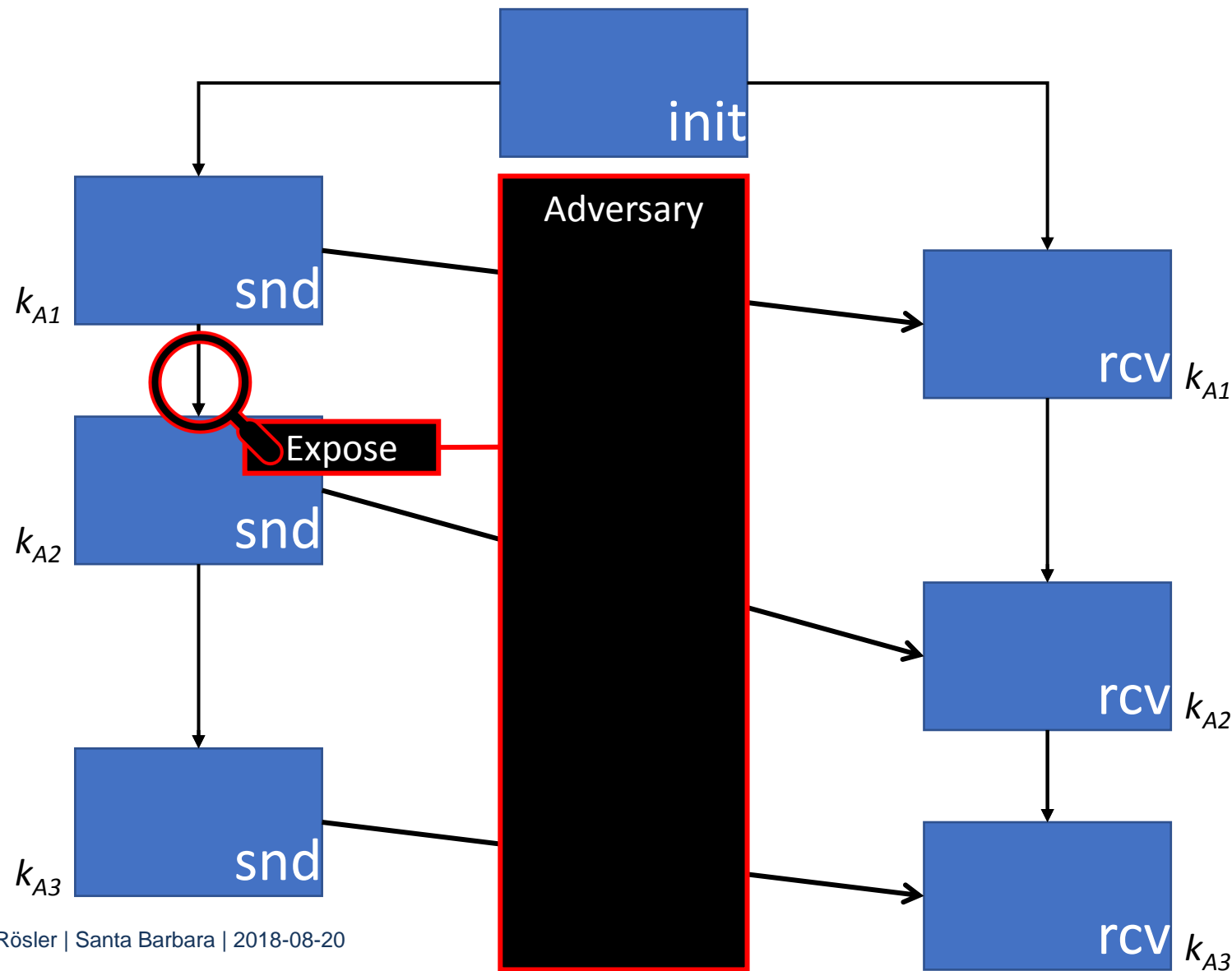
- Impersonation  
⇒ No future Challenge on Bob
- Expose Bob  
⇒ No future Challenge **if synchronous**  
(= if no previous active attack)



# Modeling Unidirectional RKE

- What is Ratcheting?
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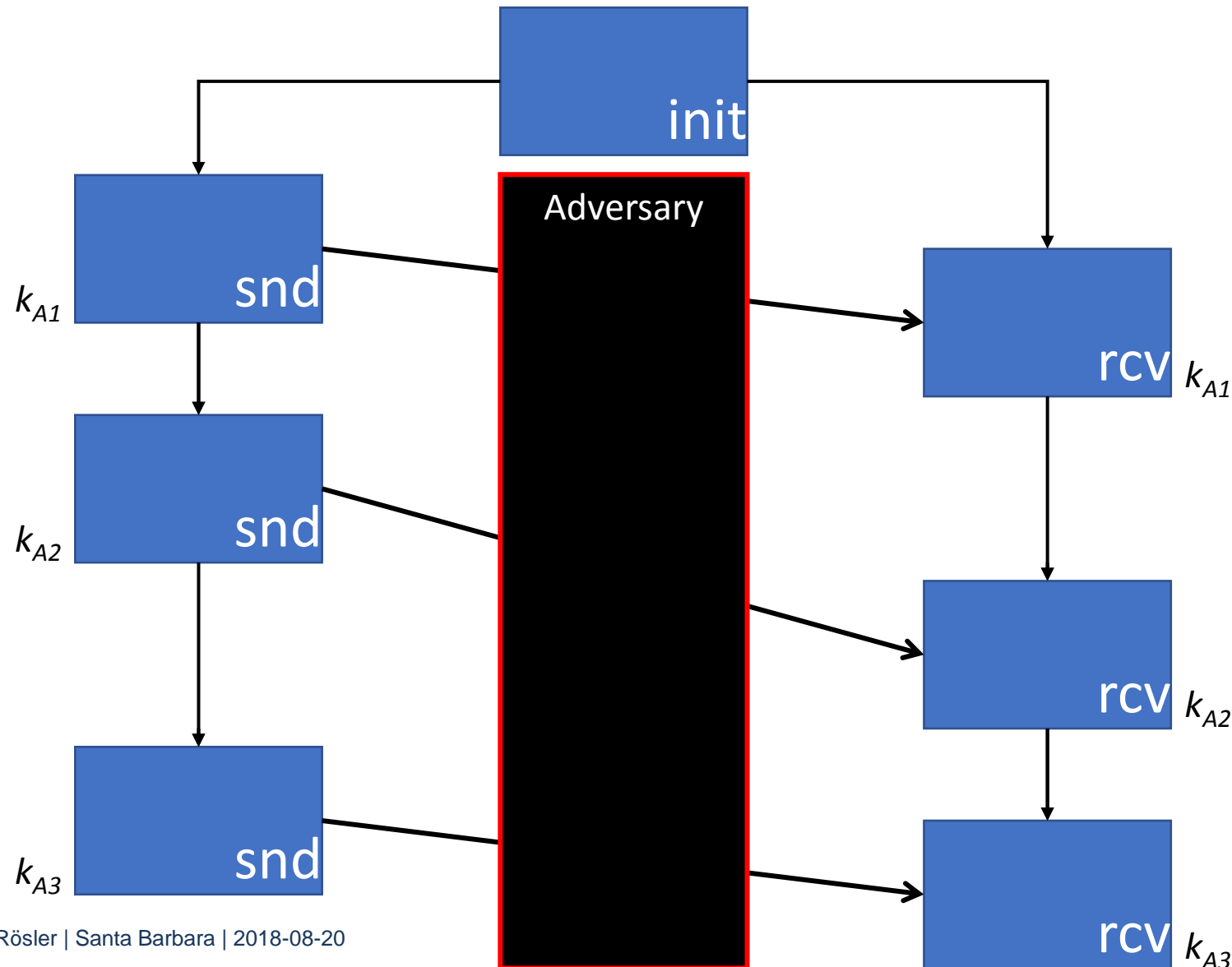
- Impersonation  
⇒ No future Challenge on Bob
  - Expose Bob  
⇒ No future Challenge if synchronous
- ⇒ Exposure of Alice (solely) “okay”



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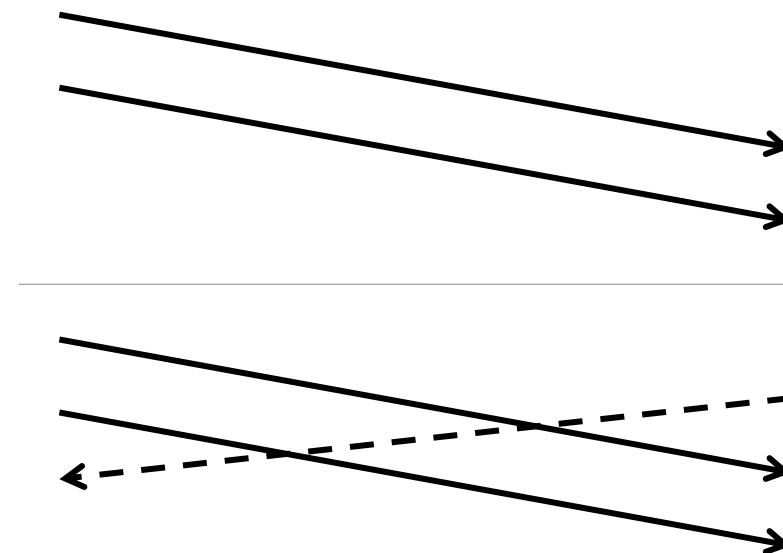
- Impersonation  
⇒ No future Challenge on Bob
- **Expose Bob**  
⇒ **No future Challenge if synchronous**
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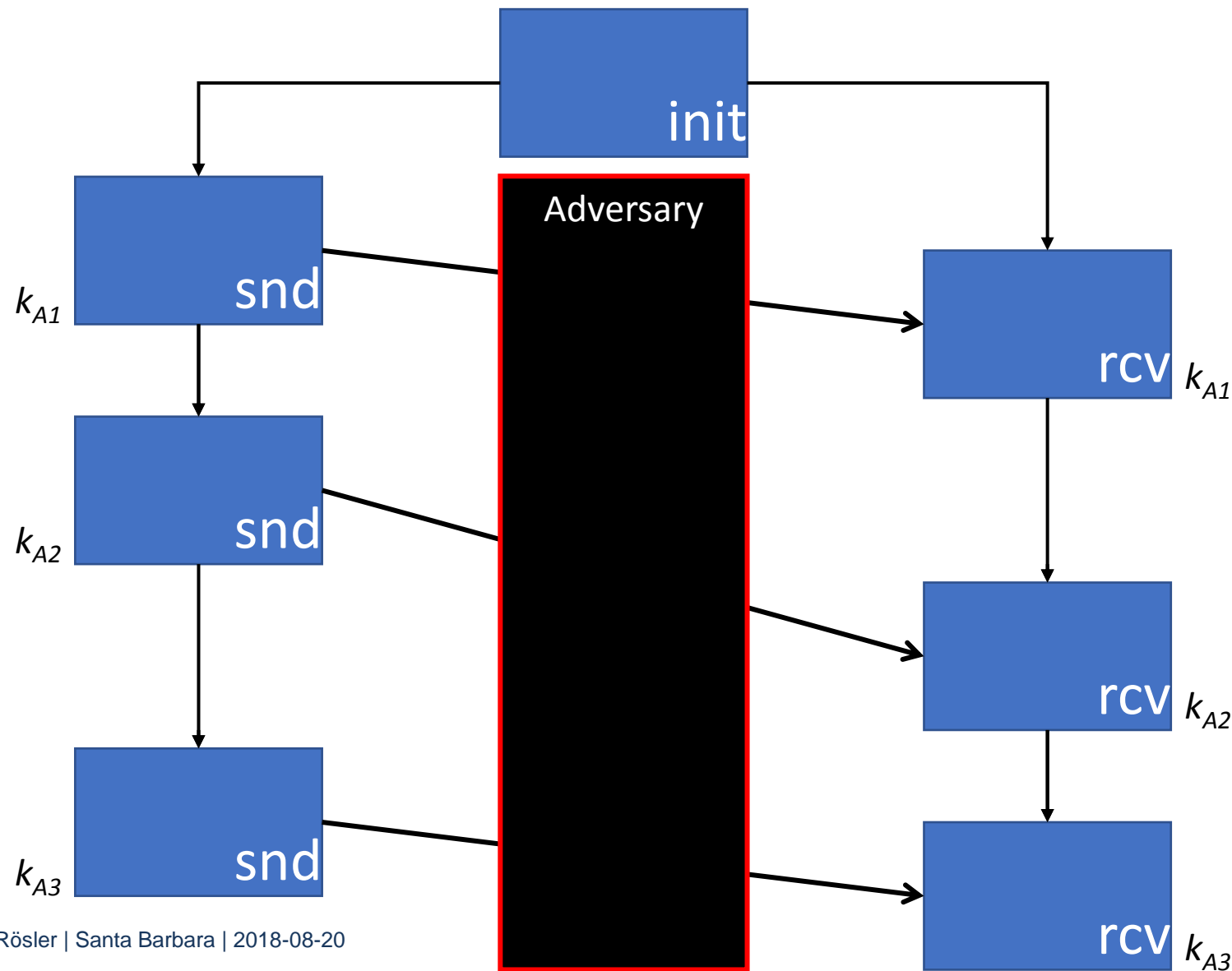
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# Constructing Unidirectional RKE

- What is Ratcheting?
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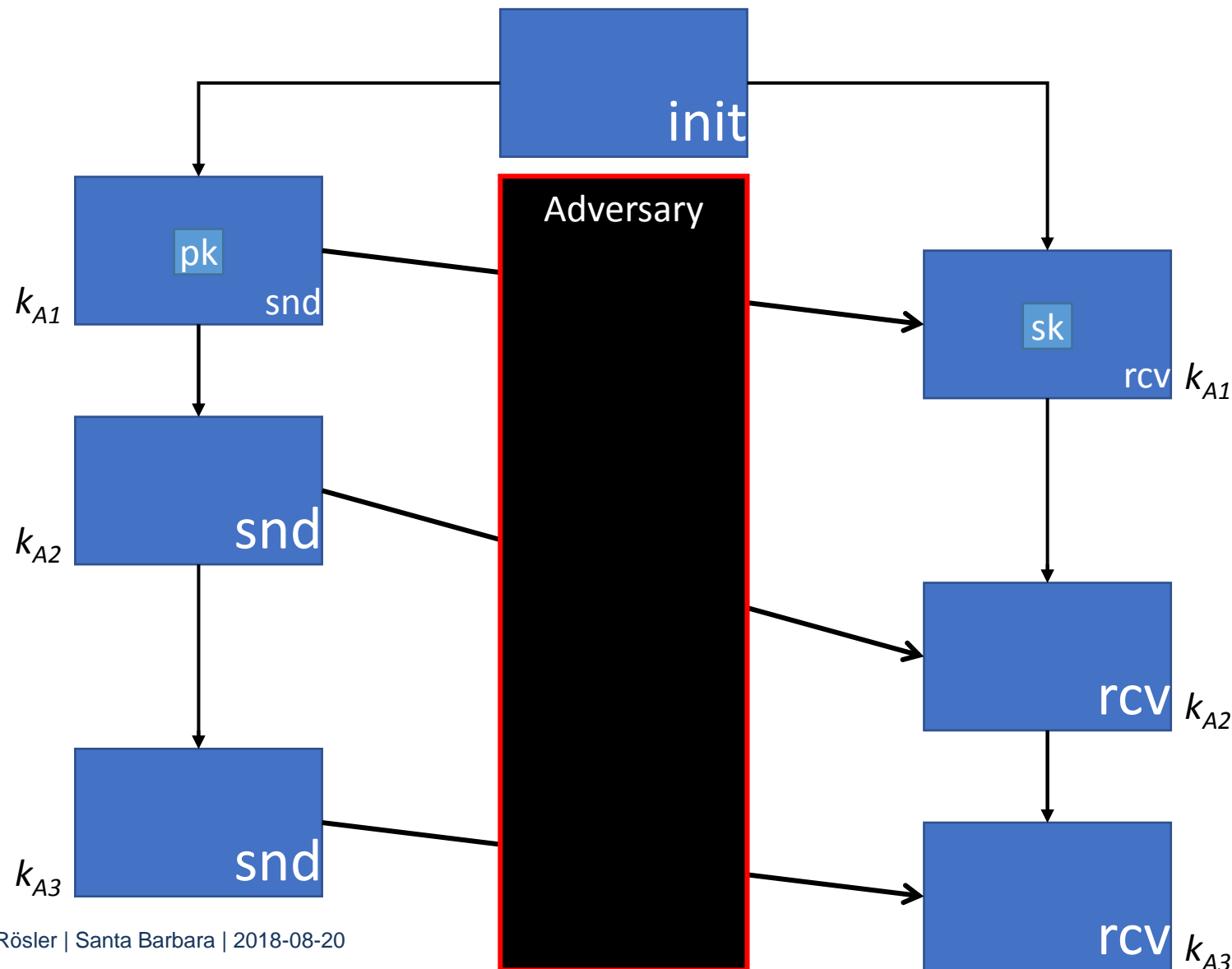
- **Expose Alice okay**
- **Expose Bob**  
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# Constructing Unidirectional RKE

- What is Ratcheting?
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- **Expose Alice okay**  
→ Public key crypto
- **Expose Bob**  
⇒ No future Challenge if synchronous



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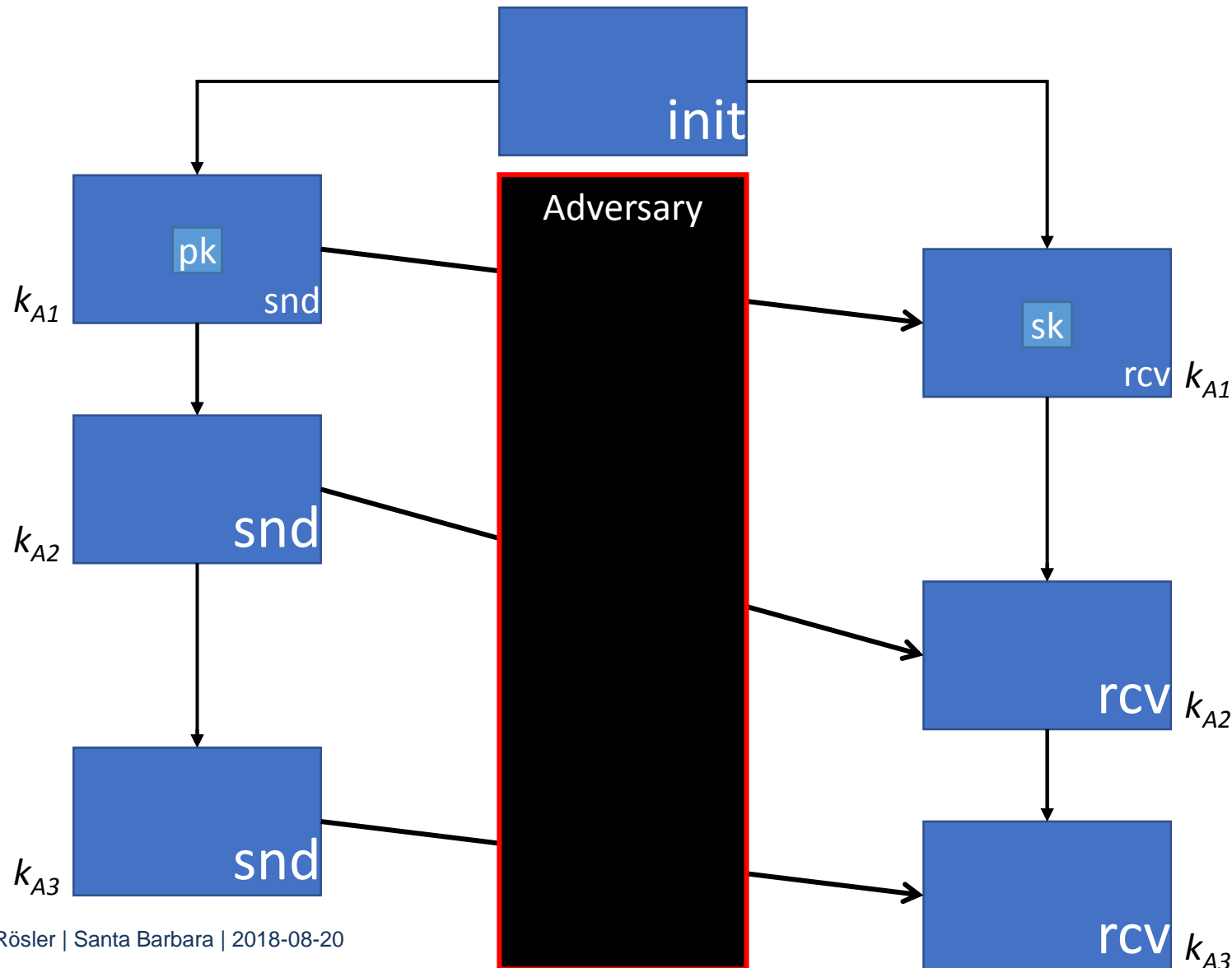
- Expose Alice okay**

→ KEM:

$$\text{enc}(\text{pk}) \rightarrow_{\xi} \text{c} \text{ k} \quad \text{dec}(\text{sk} \text{ c}) \rightarrow_{\xi} \text{k}$$

- Expose Bob**

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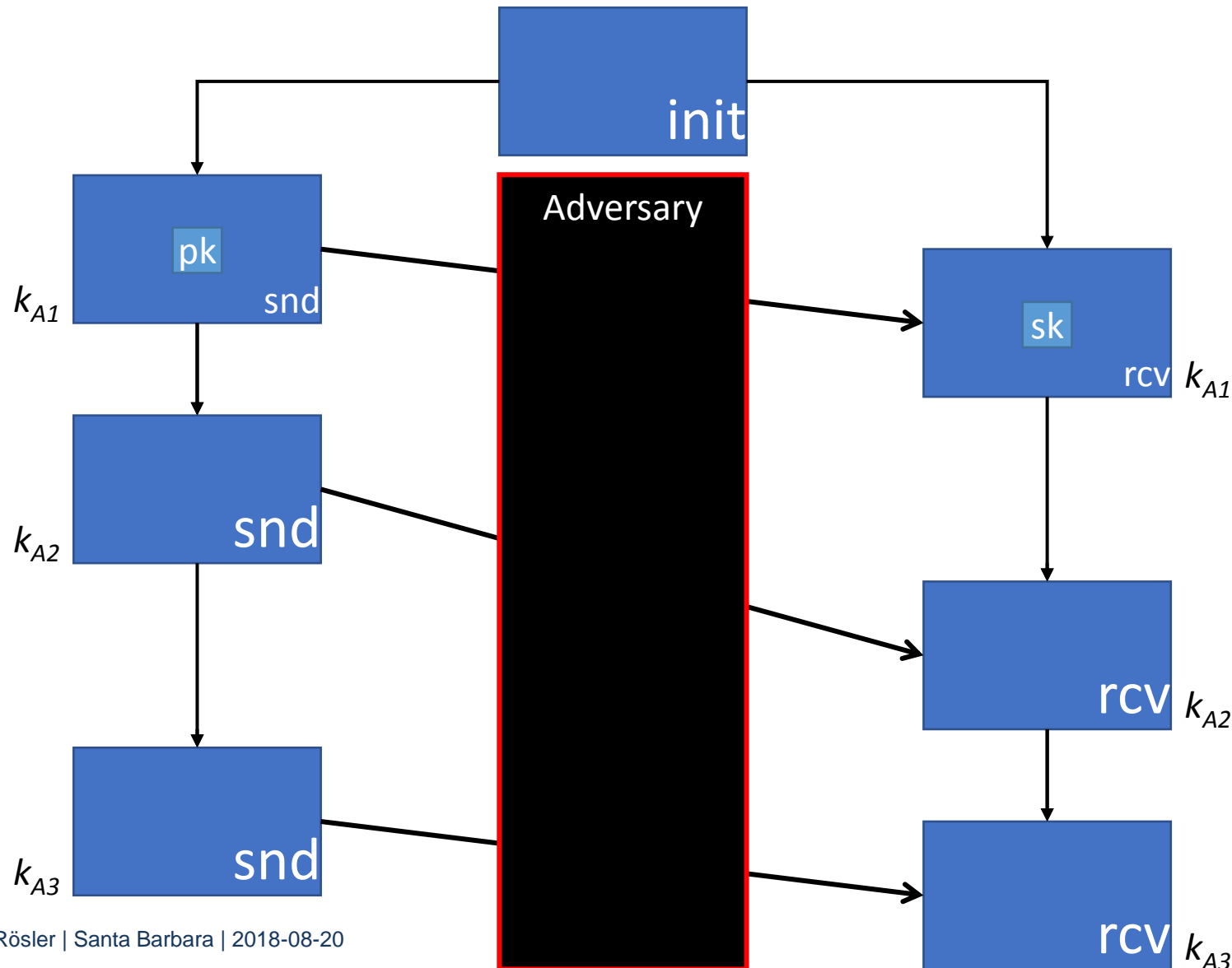
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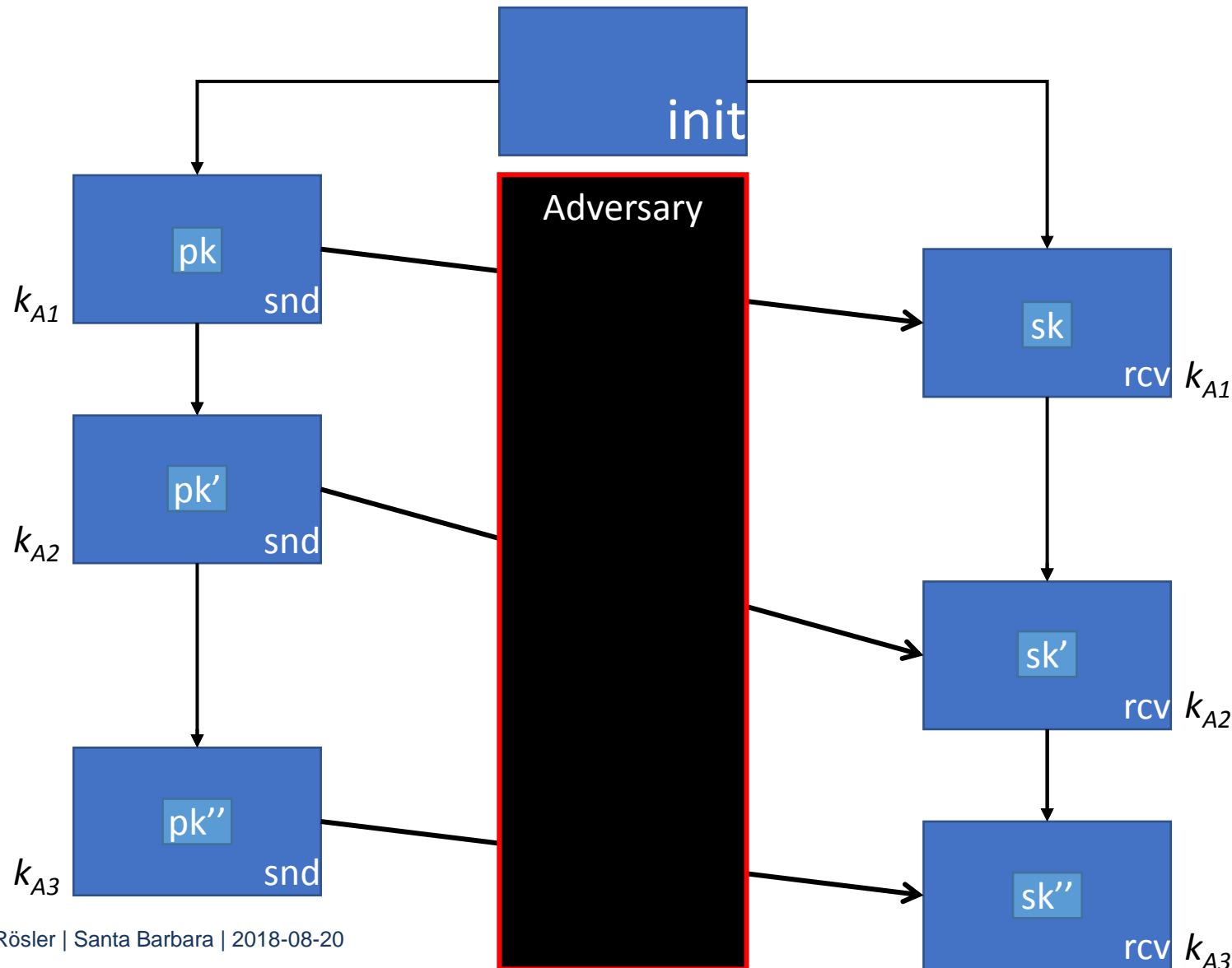
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- Expose Bob**

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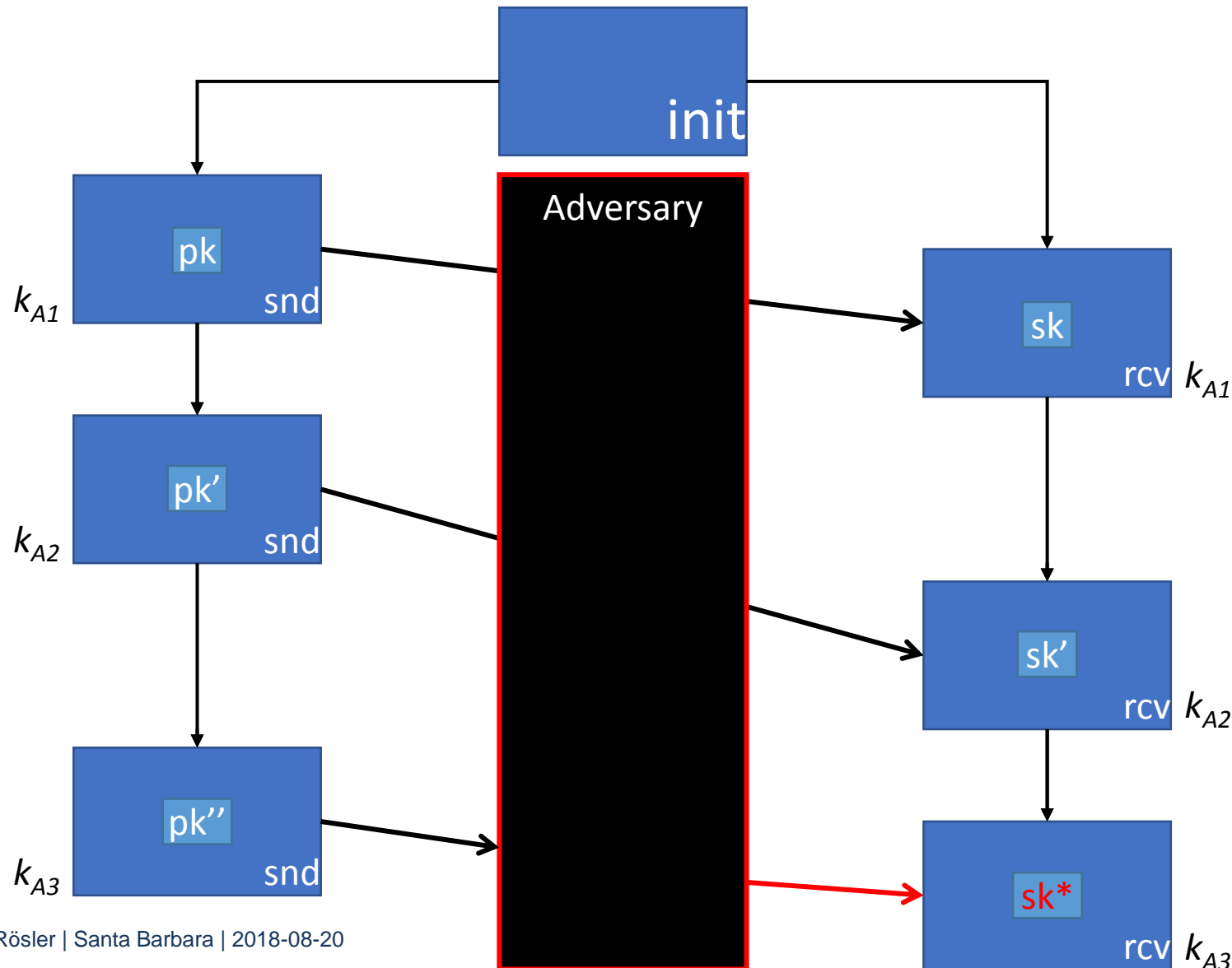
→ Forward secrecy of Bob's state



# Constructing Unidirectional RKE

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 → KEM:  
 $\text{enc}(\text{pk}) \rightarrow_{\xi} \text{c} \text{ k}$      $\text{dec}(\text{sk} \text{ c}) \rightarrow_{\xi} \text{k}$
- **Expose Bob**  
 ⇒ **No future Challenge if synchronous**  
 → Forward secrecy of Bob's state  
 → Divergence of states



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- Expose Bob**

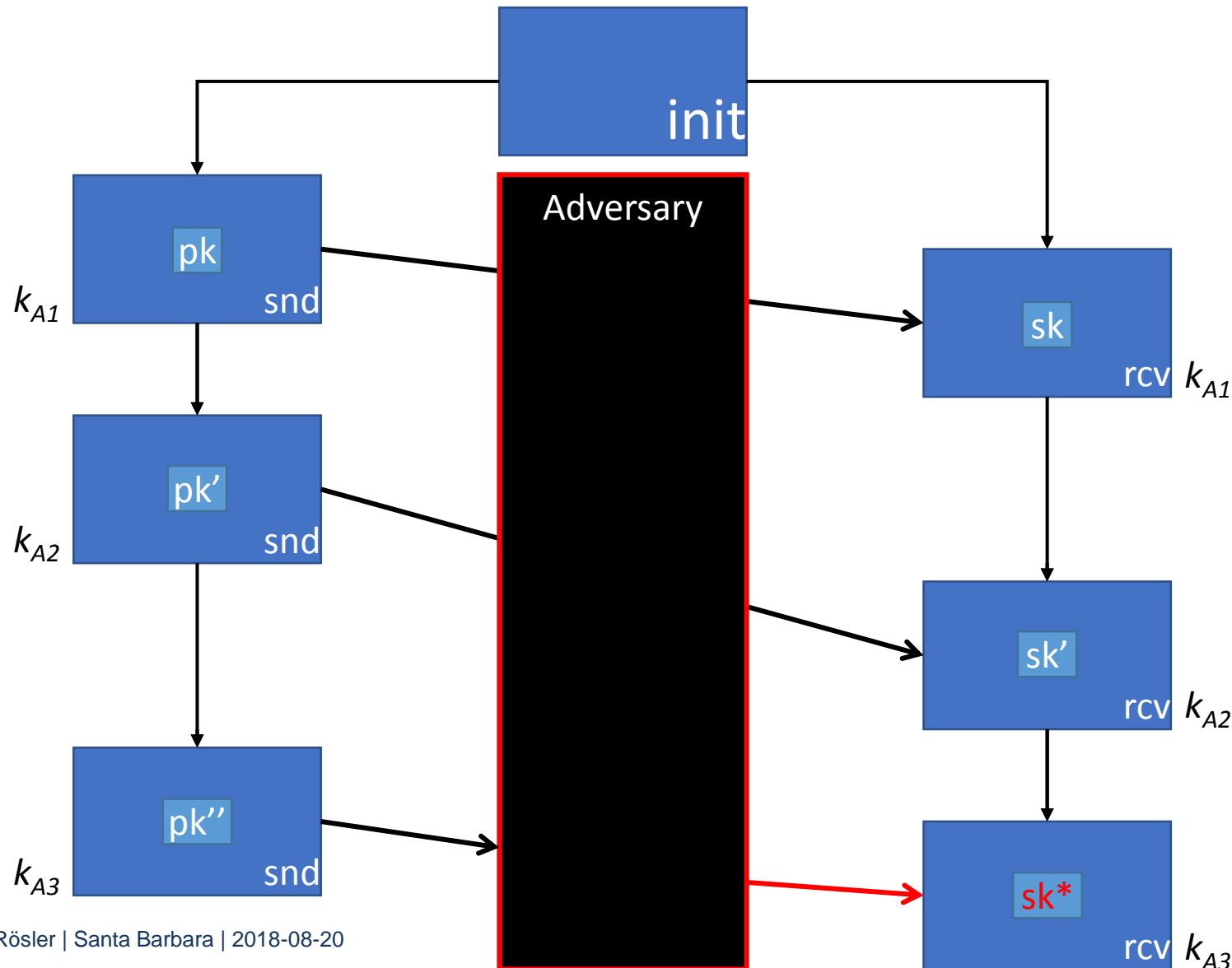
⇒ **No future Challenge if synchronous**

→ Forward secrecy of Bob's state

→ Divergence of states

→ Random oracle:

$$\text{H}(\text{c} \text{ k}) \rightarrow k_{xn} \text{ sk}$$





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- Expose Bob**

⇒ **No future Challenge if synchronous**

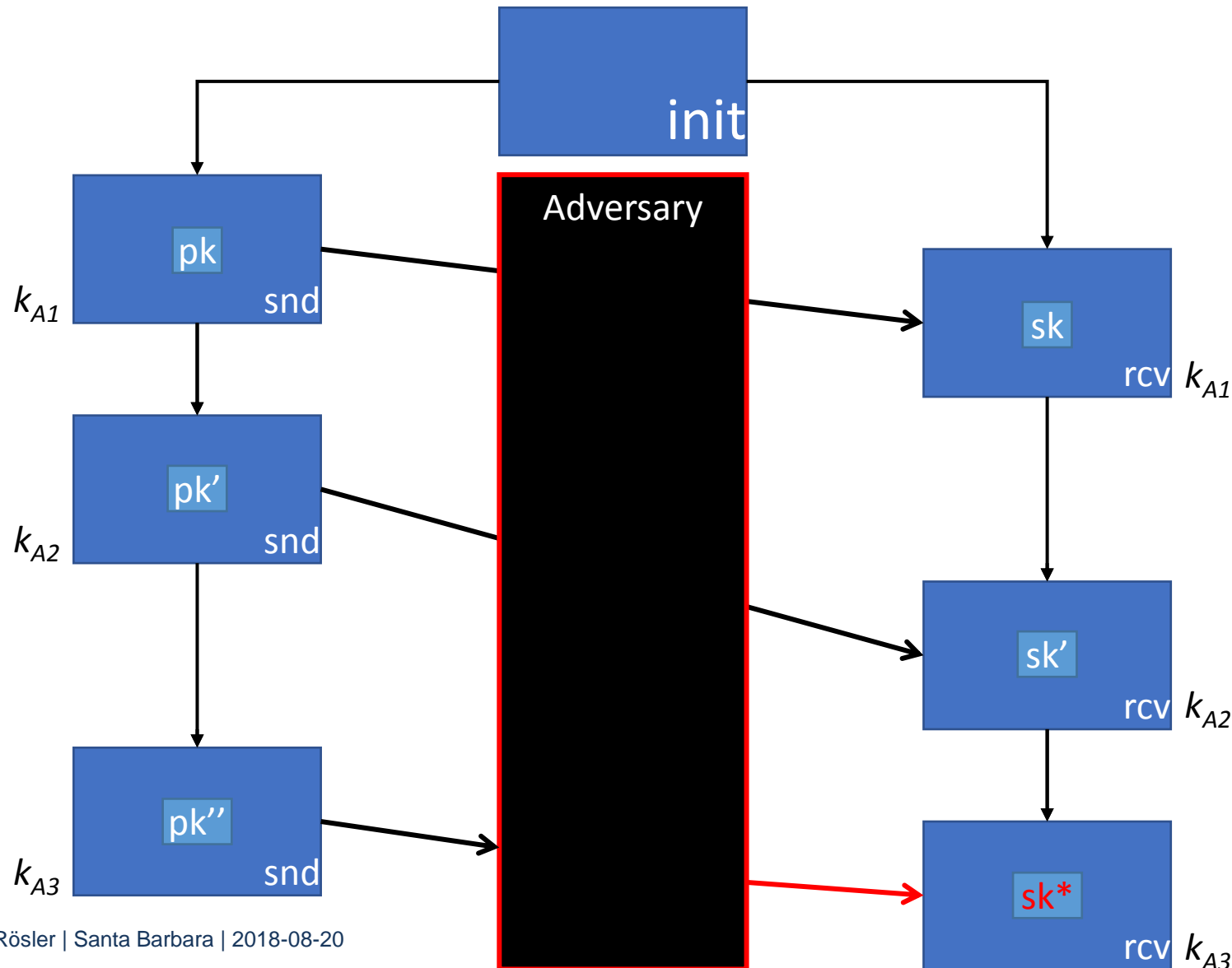
→ Forward secrecy of Bob's state

→ Divergence of states

→ Random oracle:

$$\text{H}(\text{c} \text{ k}) \rightarrow k_{xn} \text{ sk}$$

$$\text{gen}(\text{sk}) \rightarrow \text{pk}$$



# Constructing Unidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Expose Alice okay**

→ KEM:

$$\text{enc}(\text{pk}) \rightarrow_{\xi} \text{c} \text{ k} \quad \text{dec}(\text{sk} \text{ c}) \rightarrow_{\xi} \text{k}$$

- Expose Bob**

⇒ **No future Challenge if synchronous**

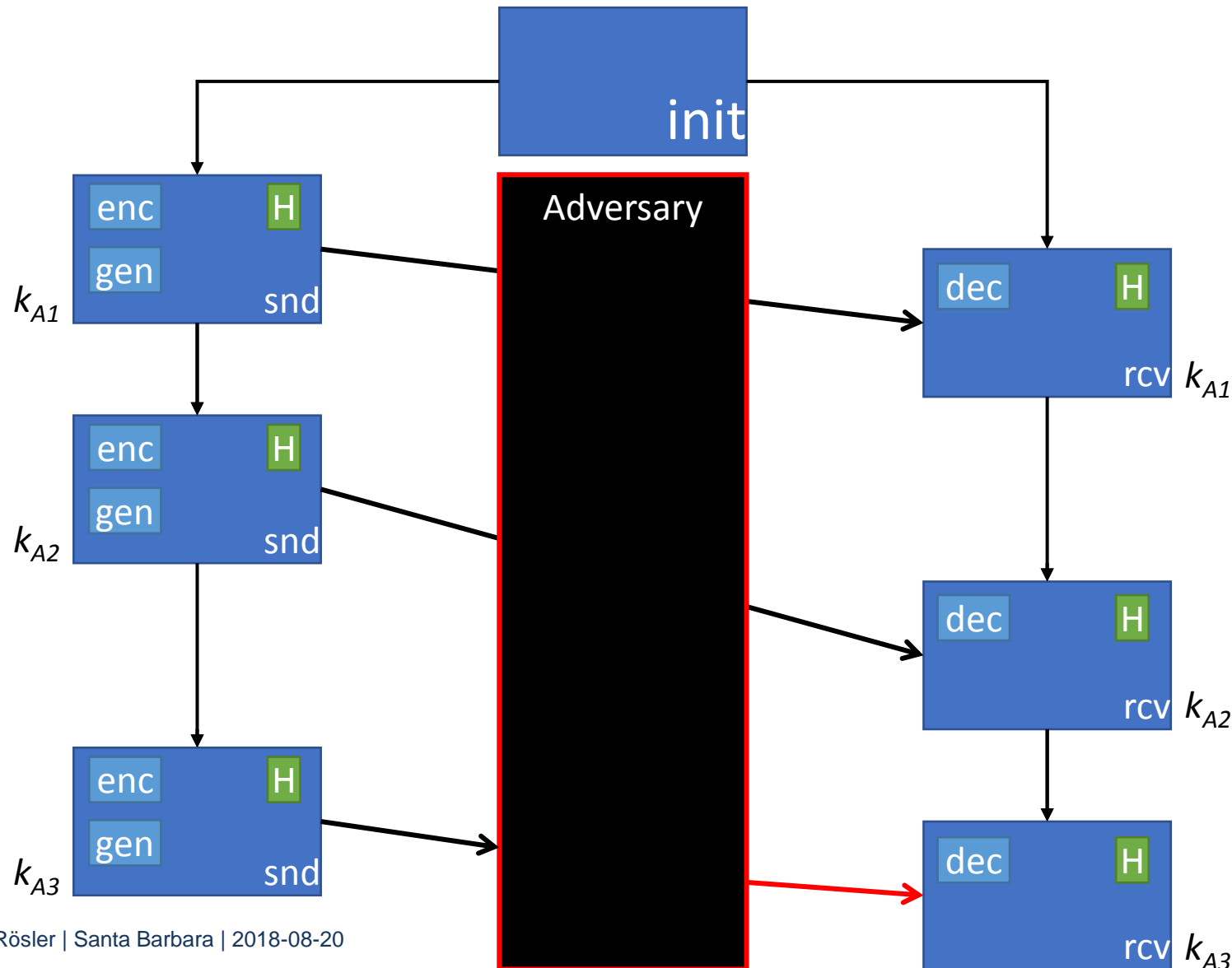
→ Forward secrecy of Bob's state

→ Divergence of states

→ Random oracle:

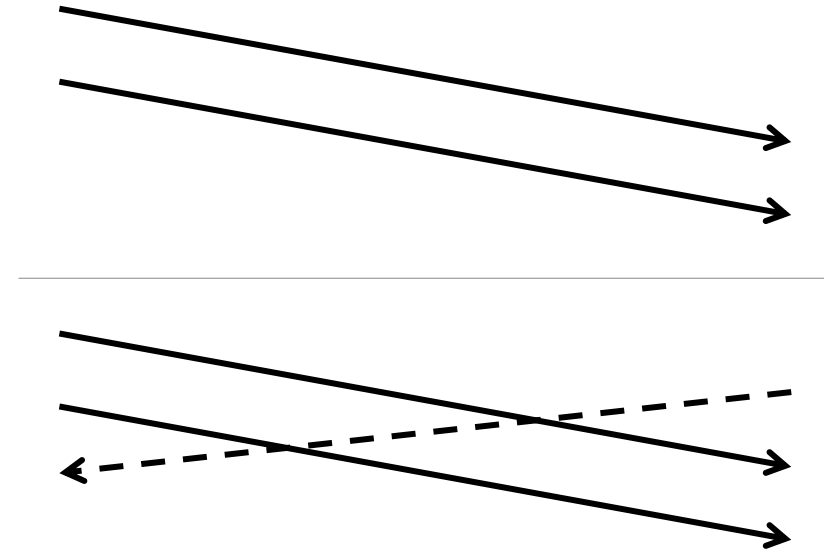
$$\text{H}(\text{c} \text{ k}) \rightarrow k_{xn} \text{ sk}$$

$$\text{gen}(\text{sk}) \rightarrow \text{pk}$$



# Agenda

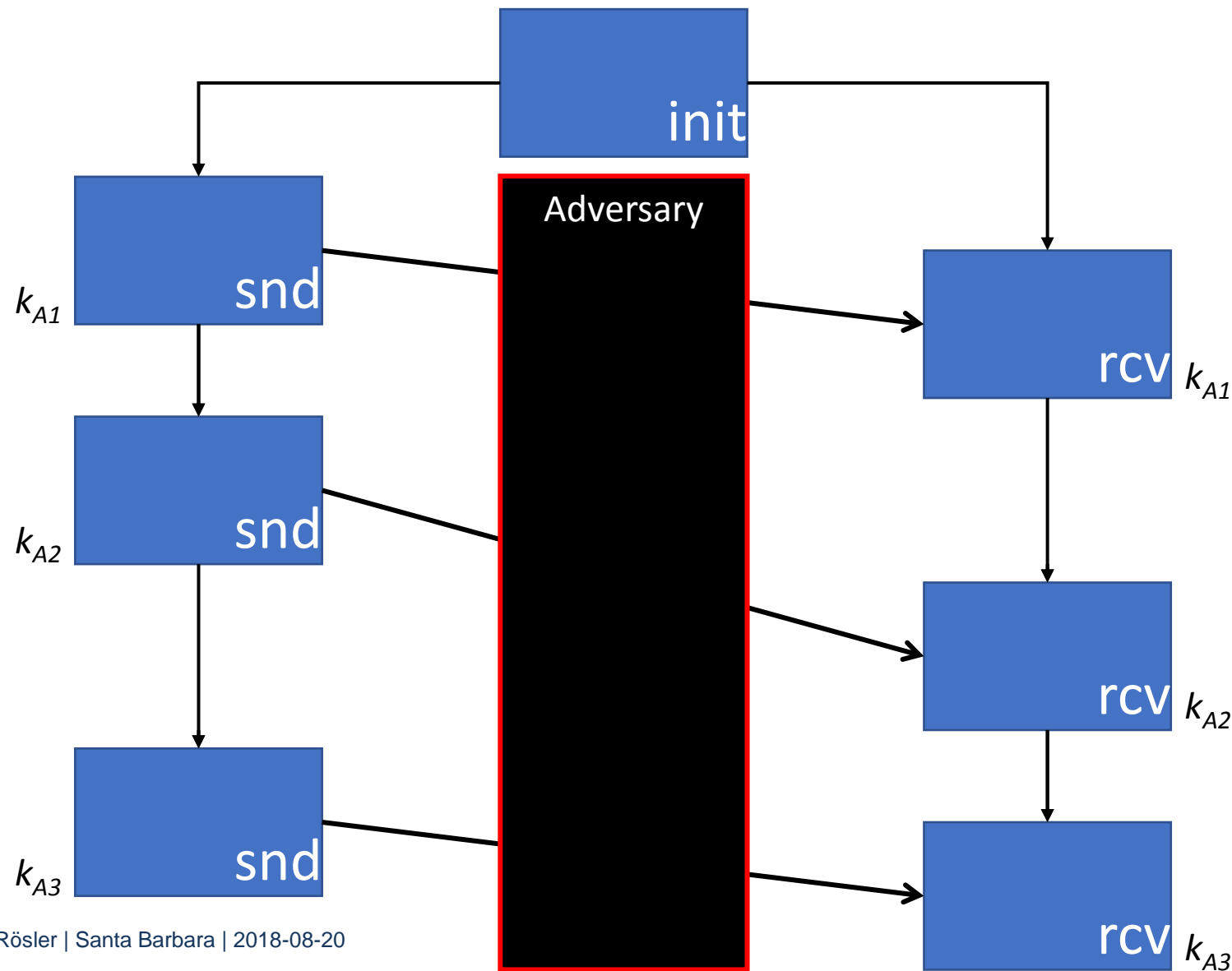
1. The Primitive Ratcheted Key Exchange
2. General Adversary Model
3. Unidirectional Ratcheting  
→ Model and Construction
4. **Sesquidirectional Ratcheting**  
→ **Model** and Construction
5. Results



# Modeling Unidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

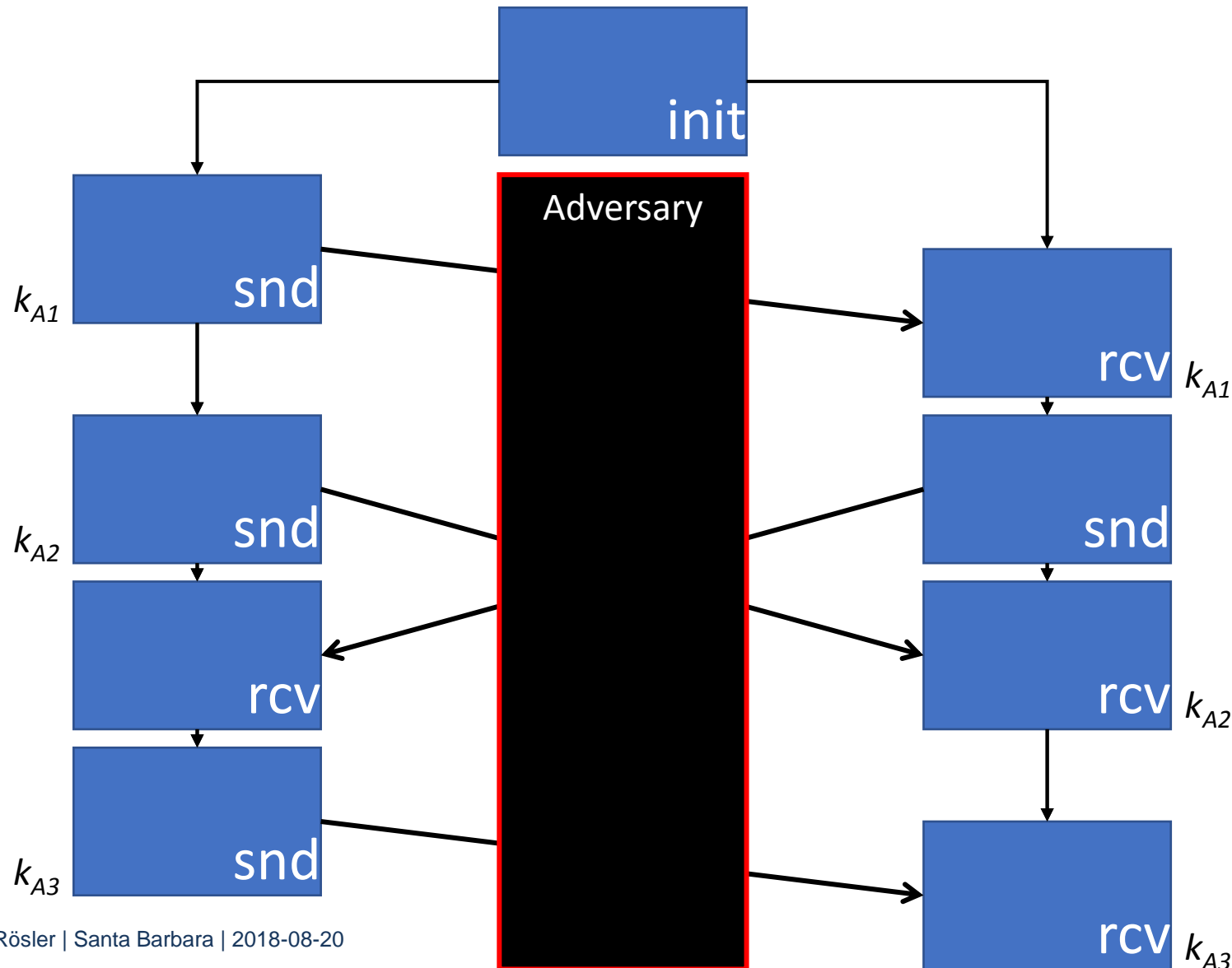
- Impersonation  $A \rightarrow B$   
 $\Rightarrow$  No future Challenge on Bob
- Expose Bob  
 $\Rightarrow$  No future Challenge if synchronous



# Modeling Sesquidirectional RKE

What is Ratcheting?  
 • Modeling RKE  
 Construction Intuition  
 Results

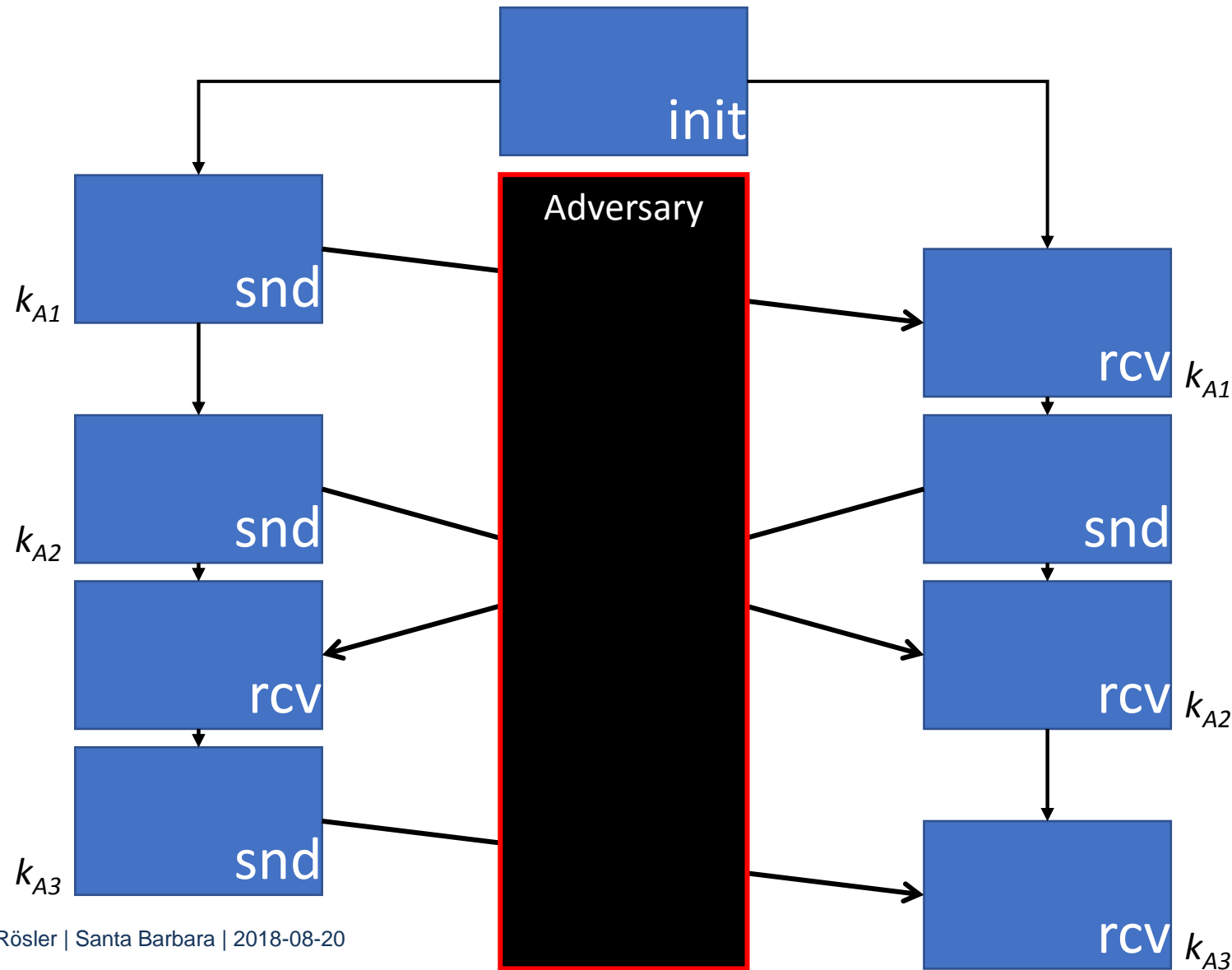
- Impersonation  $A \rightarrow B$   
 $\Rightarrow$  No future Challenge on Bob
- Expose Bob  
 $\Rightarrow$  No future Challenge if synchronous



# Modeling Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

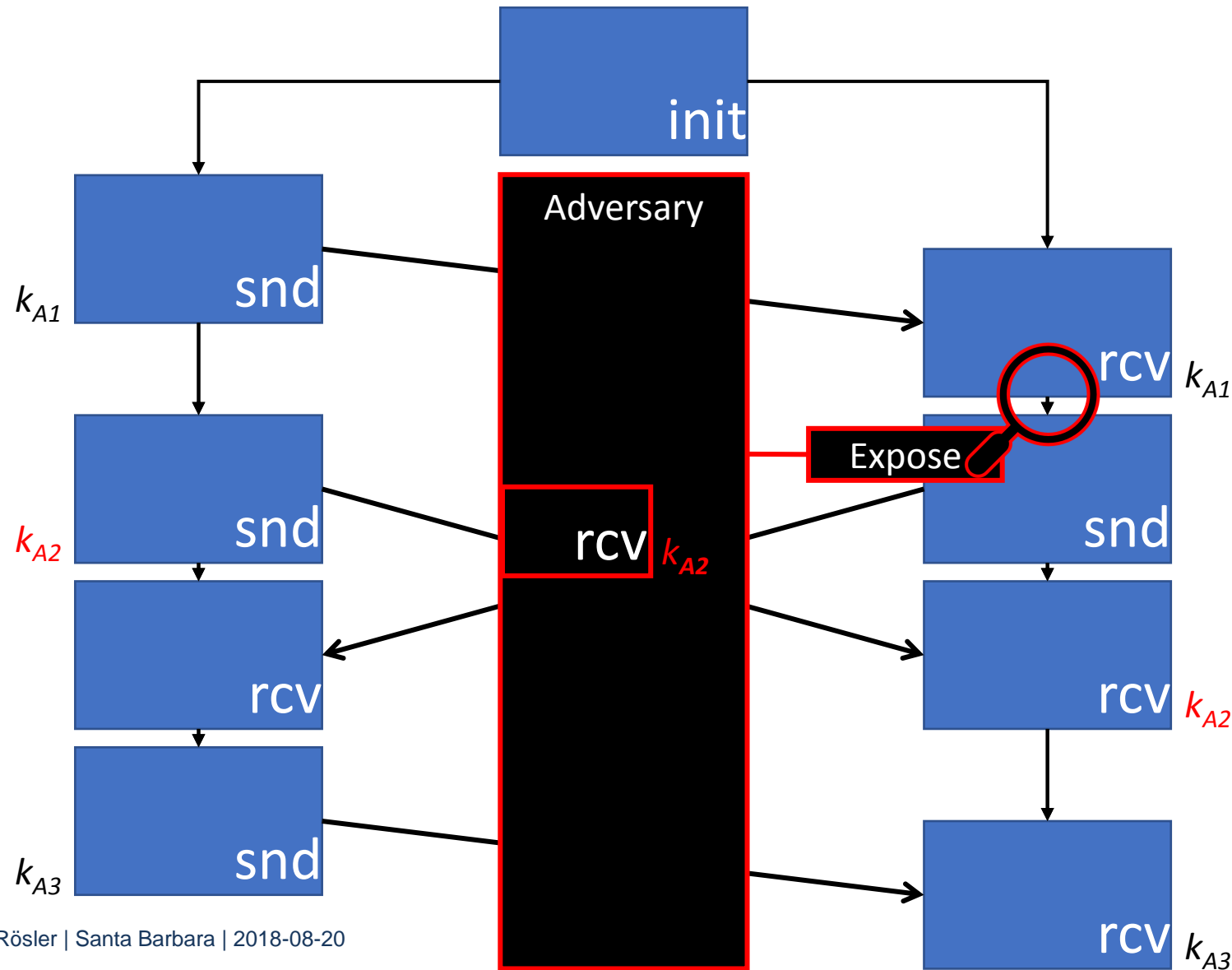
- Impersonation  $A \rightarrow B$   
 $\Rightarrow$  No future Challenge on Bob
- Impersonation  $B \rightarrow A$   
 $\Rightarrow$  No future Challenge on Alice
- Expose Bob  
 $\Rightarrow$  No future Challenge if synchronous



# Modeling Sesquidirectional RKE

What is Ratcheting?  
 • Modeling RKE  
 Construction Intuition  
 Results

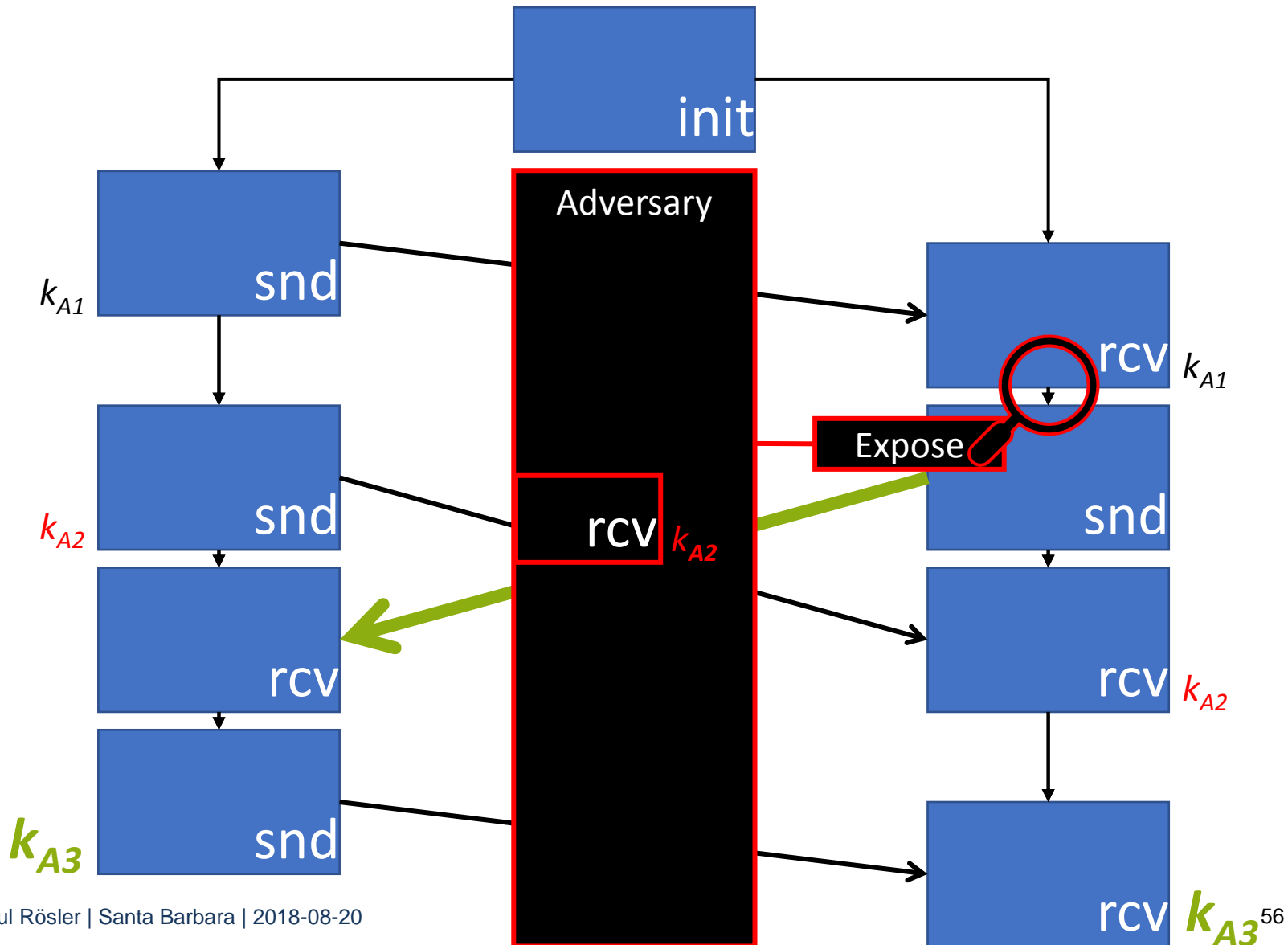
- Impersonation  $A \rightarrow B$   
 $\Rightarrow$  No future Challenge on Bob
- Impersonation  $B \rightarrow A$   
 $\Rightarrow$  No future Challenge on Alice
- Expose Bob  
 $\Rightarrow$  No future Challenge if synchronous  
**until Bob recovered**



# Modeling Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Impersonation  $A \rightarrow B$   
 $\Rightarrow$  No future Challenge on Bob
- Impersonation  $B \rightarrow A$   
 $\Rightarrow$  No future Challenge on Alice
- Expose Bob  
 $\Rightarrow$  No future Challenge if synchronous  
**until Bob recovered**

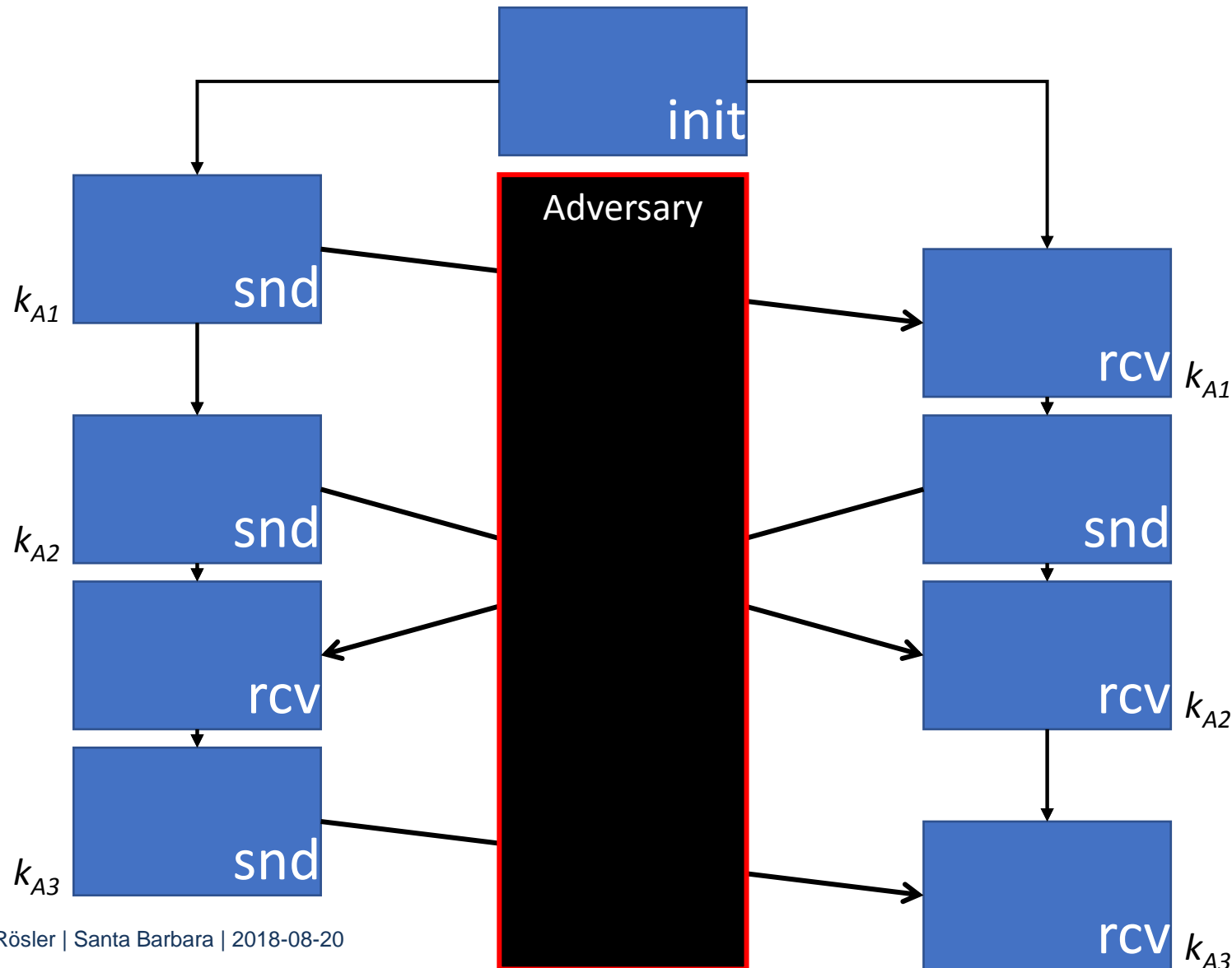




# Modeling Sesquidirectional RKE

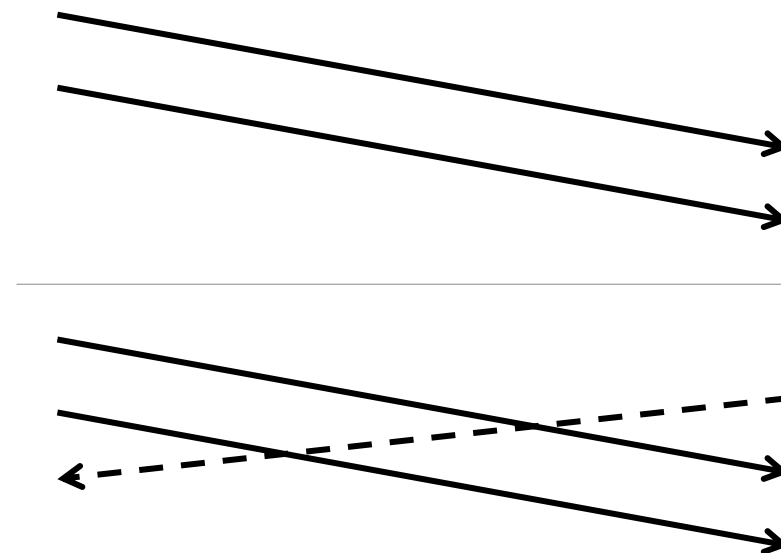
What is Ratcheting?  
Modeling RKE  
Construction Intuition  
Results

- Impersonation  $A \rightarrow B$   
 $\Rightarrow$  No future Challenge on Bob
- Impersonation  $B \rightarrow A$   
 $\Rightarrow$  No future Challenge on Alice
- **Expose Bob**  
 $\Rightarrow$  **No future Challenge if synchronous until Bob recovered**



# Agenda

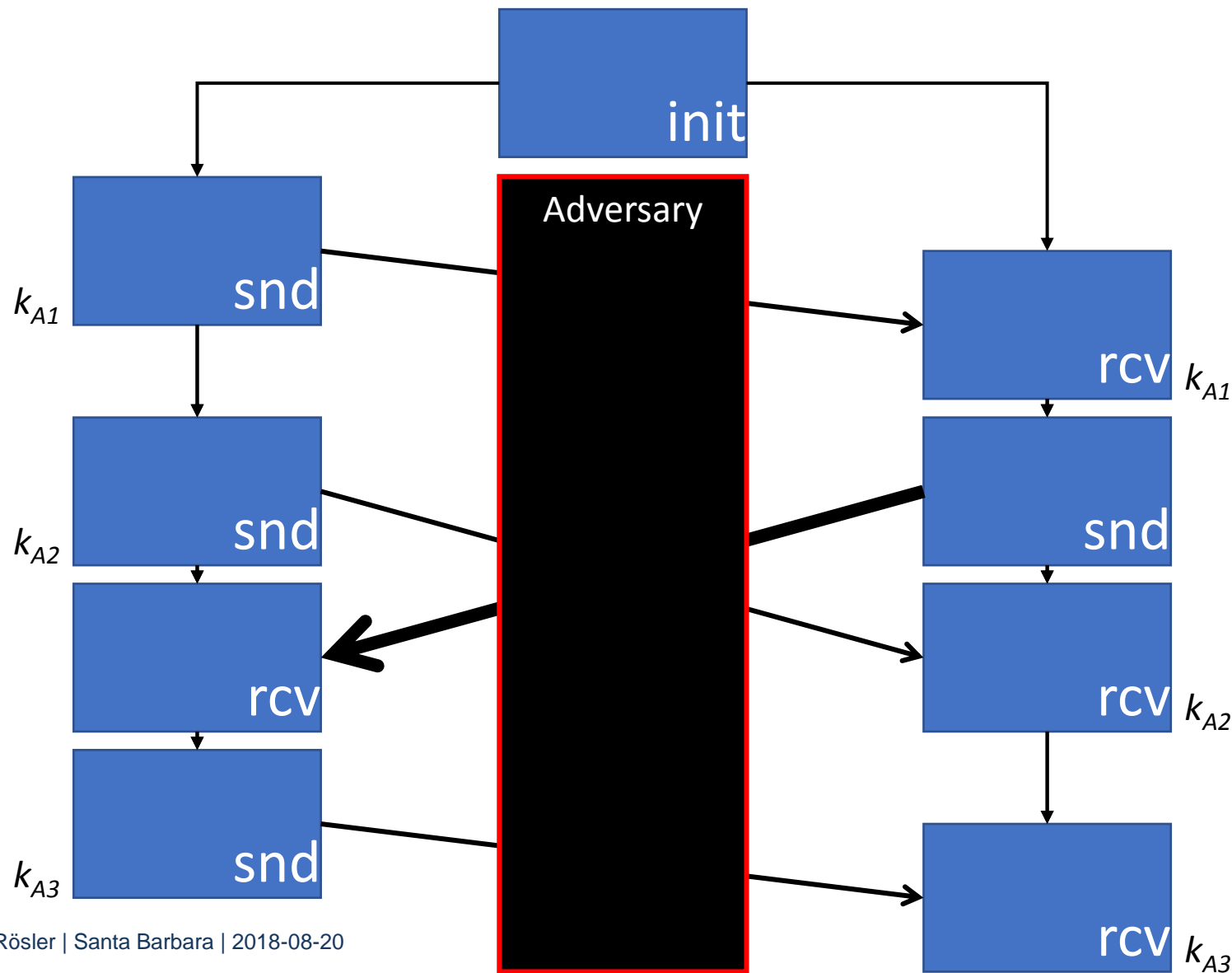
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3. Unidirectional Ratcheting  
→ Model and Construction
4. **Sesquidirectional Ratcheting**  
→ Model and **Construction**
5. Results



# Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

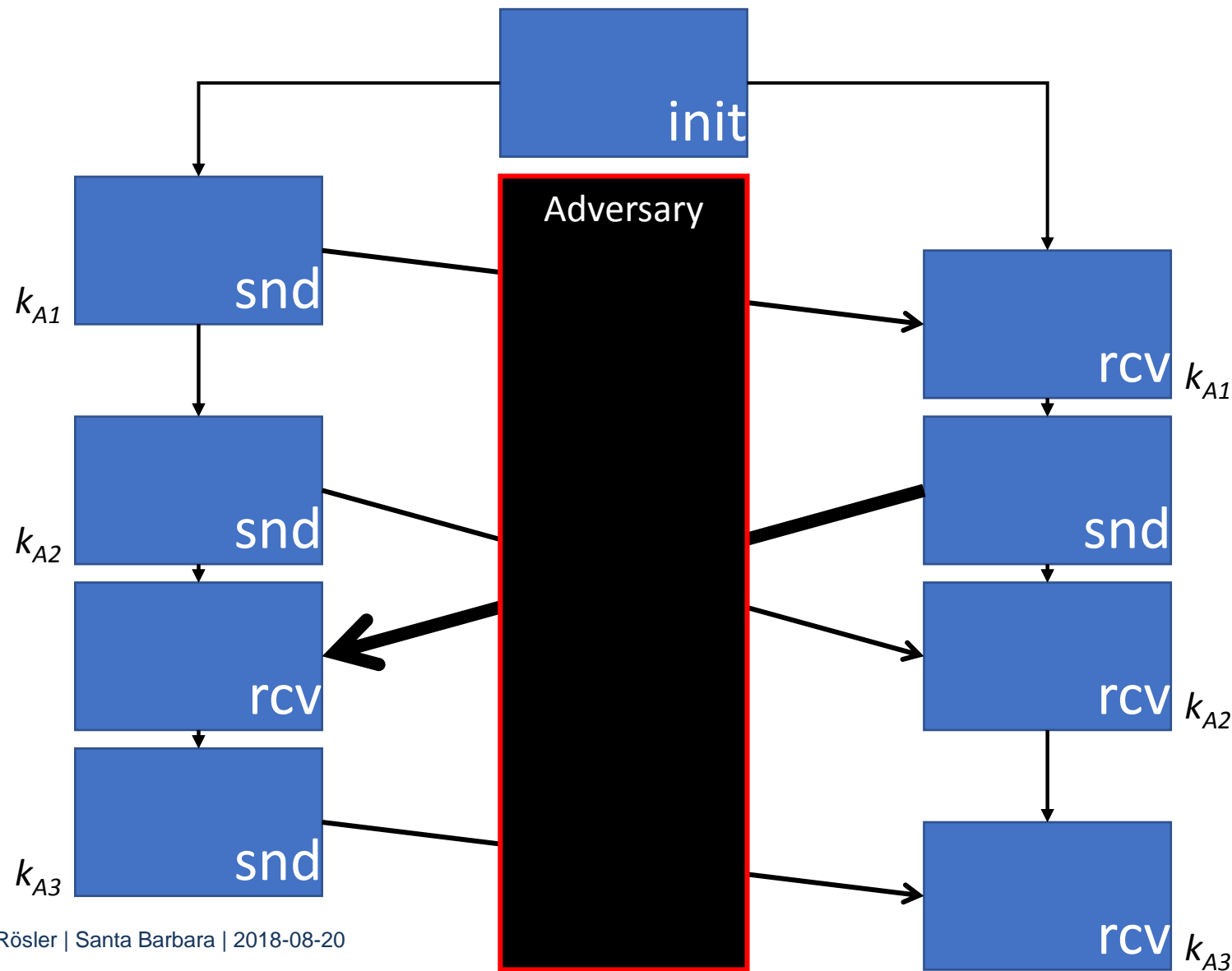
- **Expose Bob**  
 ⇒ **No future Challenge**  
**if synchronous**  
**until Bob recovered**



# Constructing Sesquidirectional RKE

- What is Ratcheting?  
Modeling RKE
- Construction Intuition  
Results

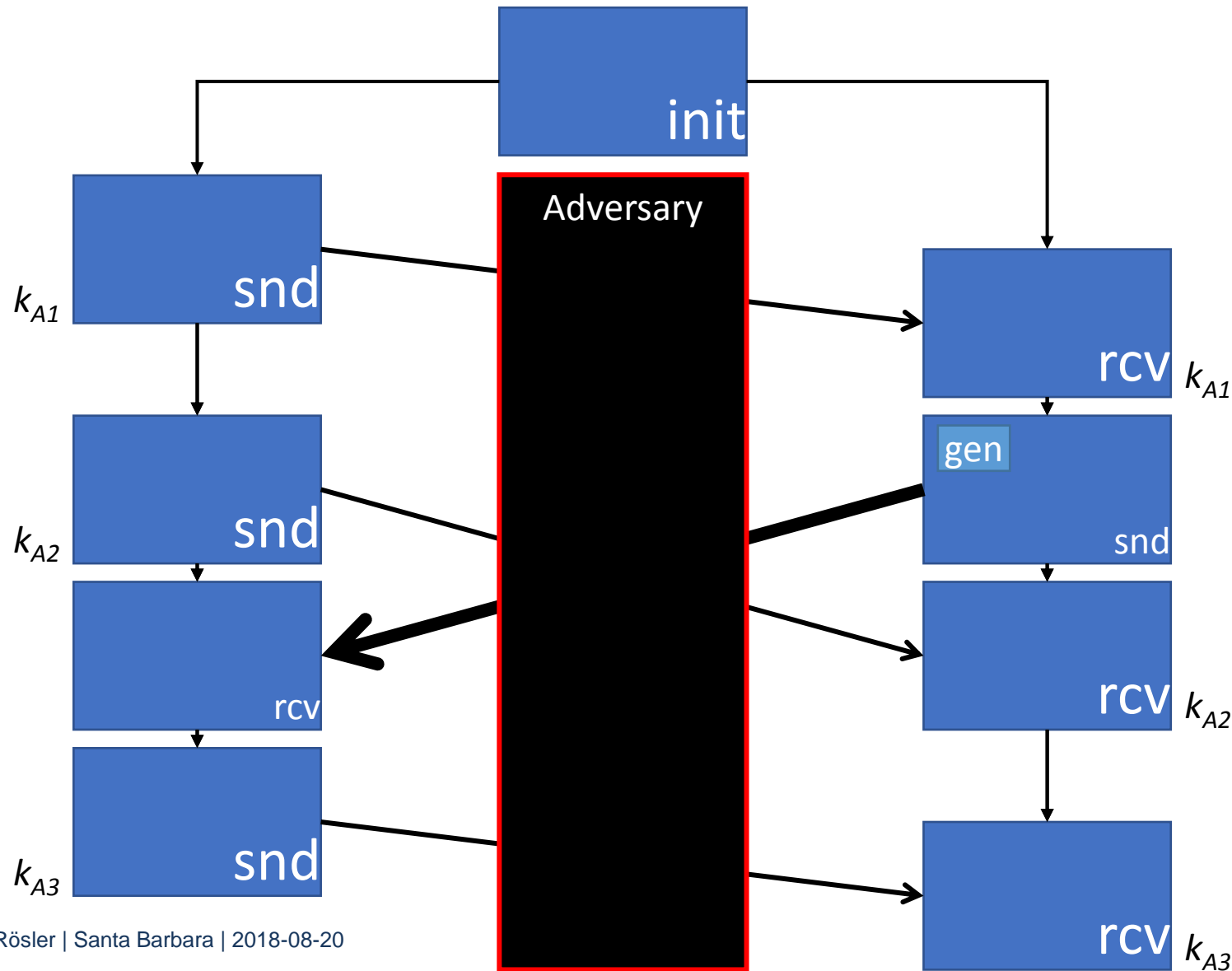
- **Expose Bob**  
 ⇒ **No future Challenge**  
**if synchronous**  
**until Bob recovered**  
 → Forward secrecy  
 and recovery  
 of Bob's state



# Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

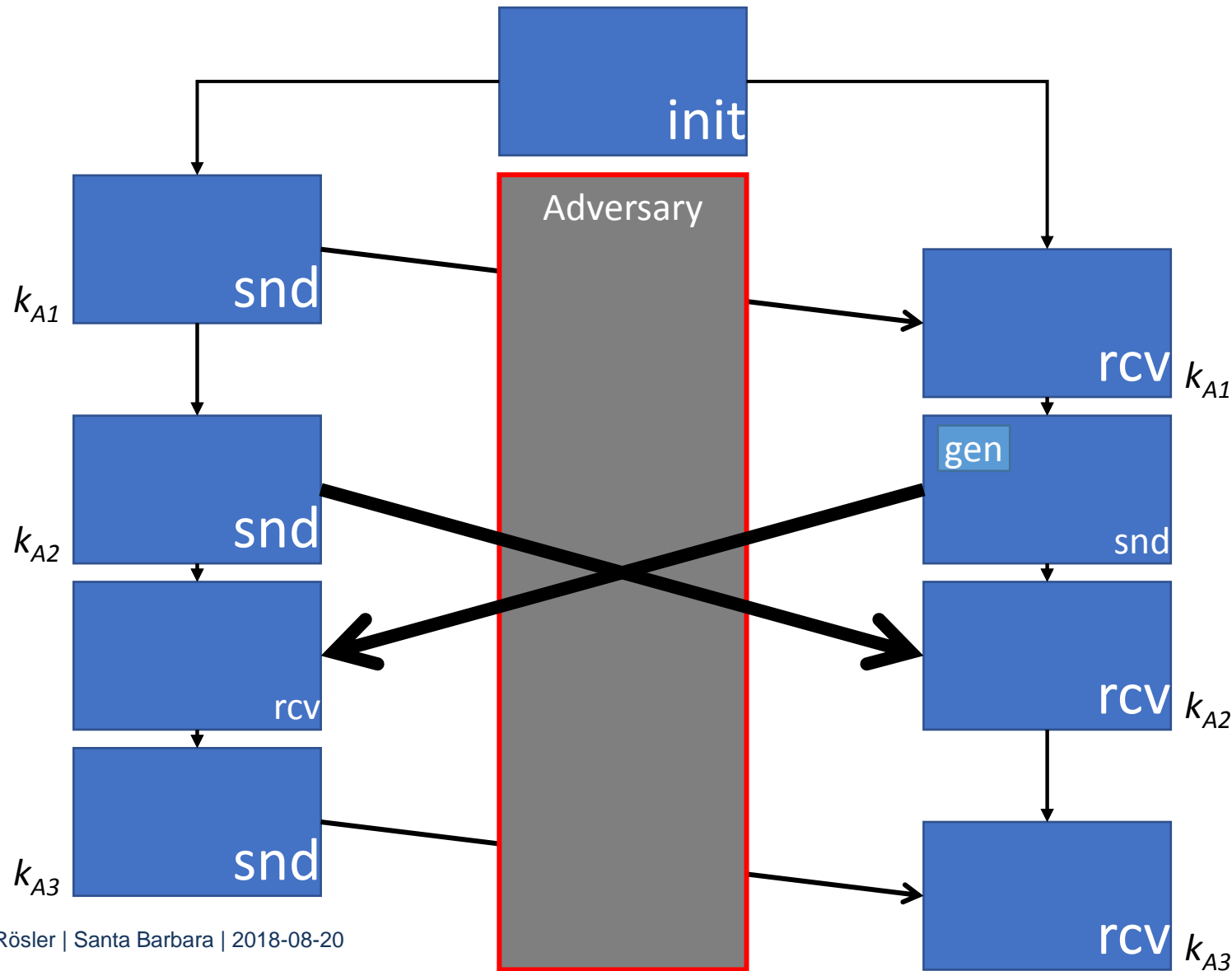
- Expose Bob
  - ⇒ No future Challenge if synchronous until Bob recovered
  - Forward secrecy and recovery of Bob's state
  - Send new **pk**



# Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

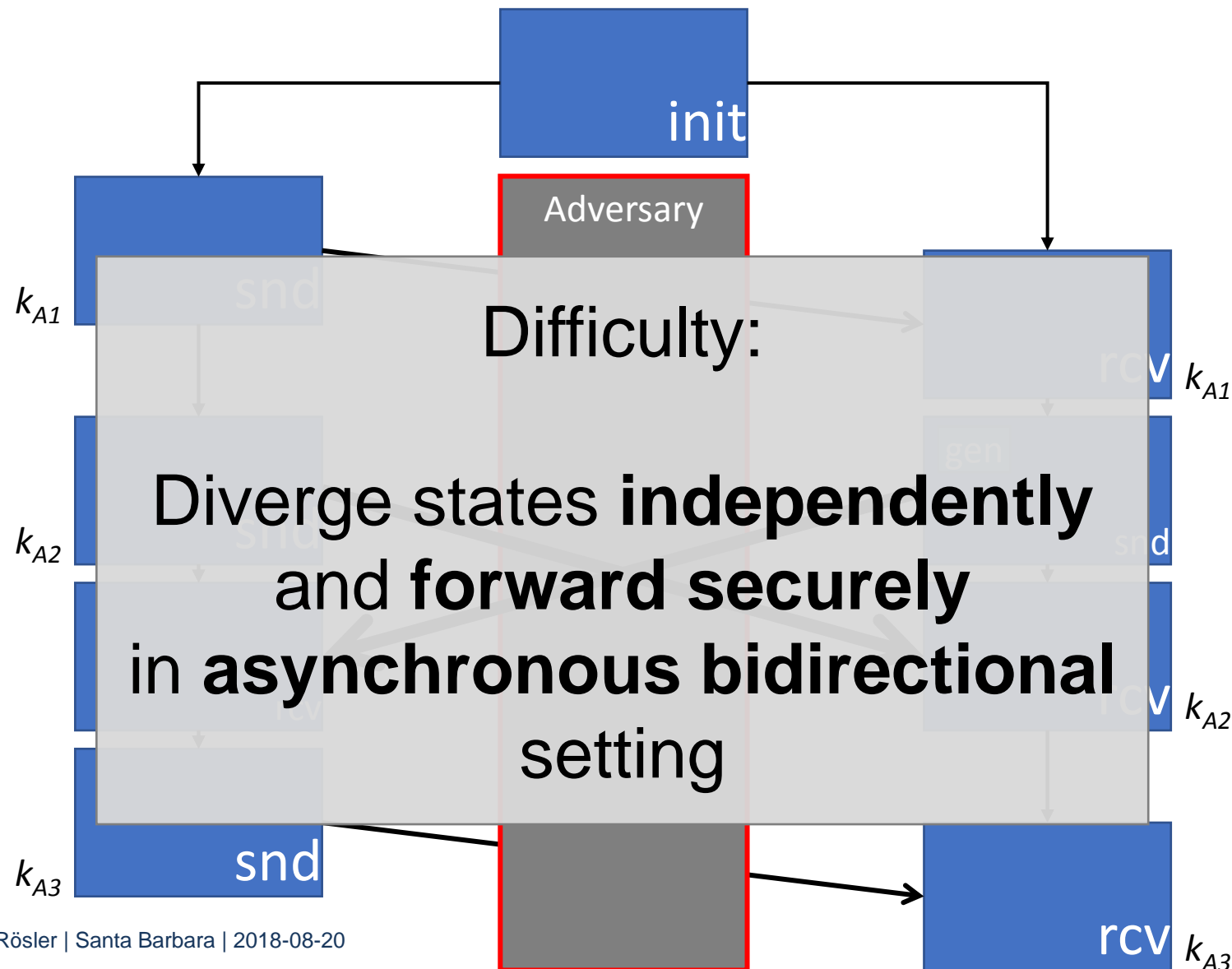
- Expose Bob
  - ⇒ No future Challenge if synchronous until Bob recovered
  - Forward secrecy and recovery of Bob's state
  - Send new **pk**
  - Divergence of states



# Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

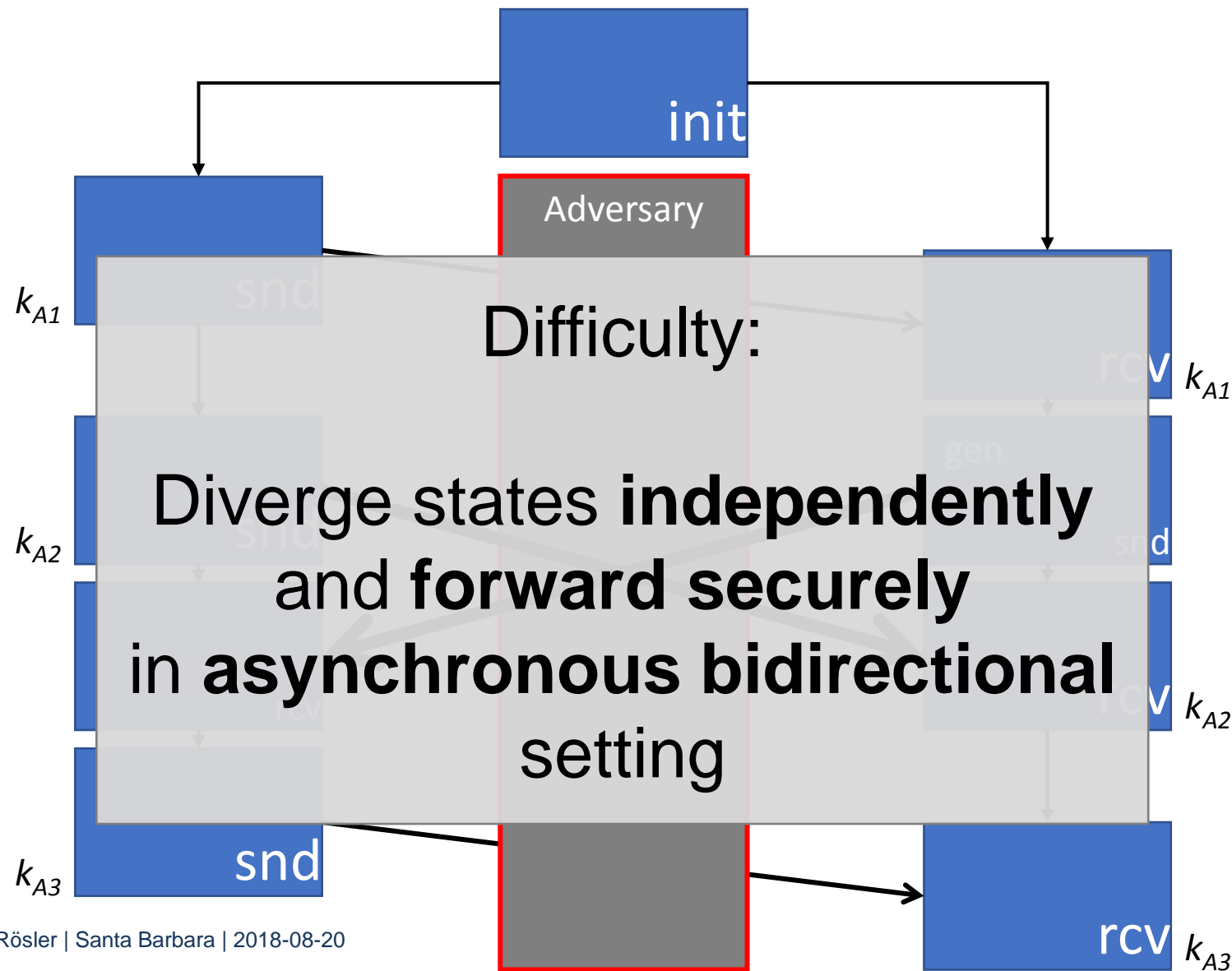
- Expose Bob
  - ⇒ No future Challenge if synchronous until Bob recovered
  - Forward secrecy and recovery of Bob's state
  - Send new **pk**
  - Divergence of states



# Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Expose Bob
  - ⇒ No future Challenge if synchronous until Bob recovered
  - Forward secrecy and recovery of Bob's state
  - Send new **pk**
  - Divergence of states
  - Update key pair





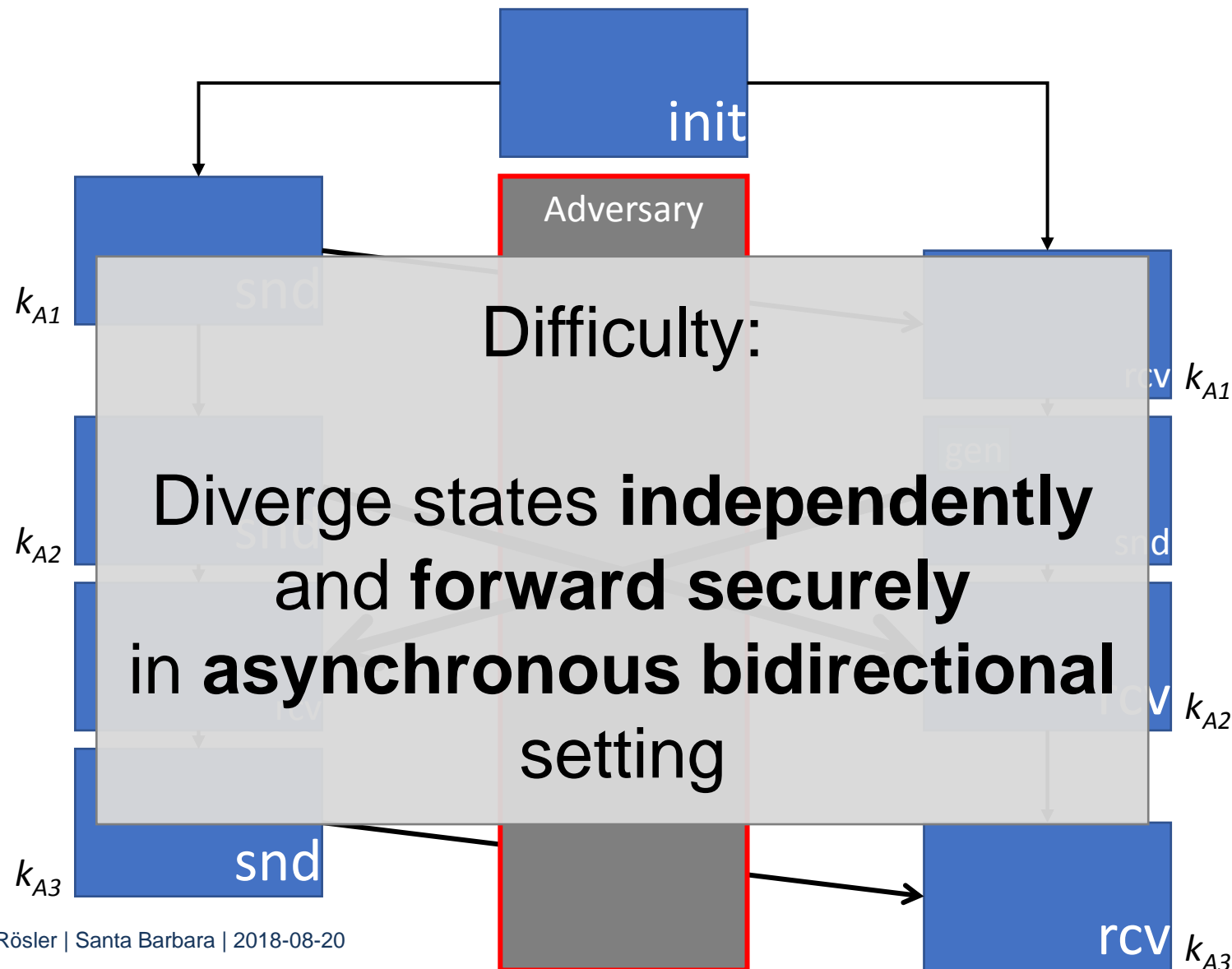
# Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Expose Bob
  - ⇒ No future Challenge if synchronous until Bob recovered
  - Forward secrecy and recovery of Bob's state
  - Send new **pk**
  - Divergence of states
  - Update key pair

**up** (**sk**,  $\mathcal{T}$ ) → **sk**

**up** (**pk**,  $\mathcal{T}$ ) → **pk**



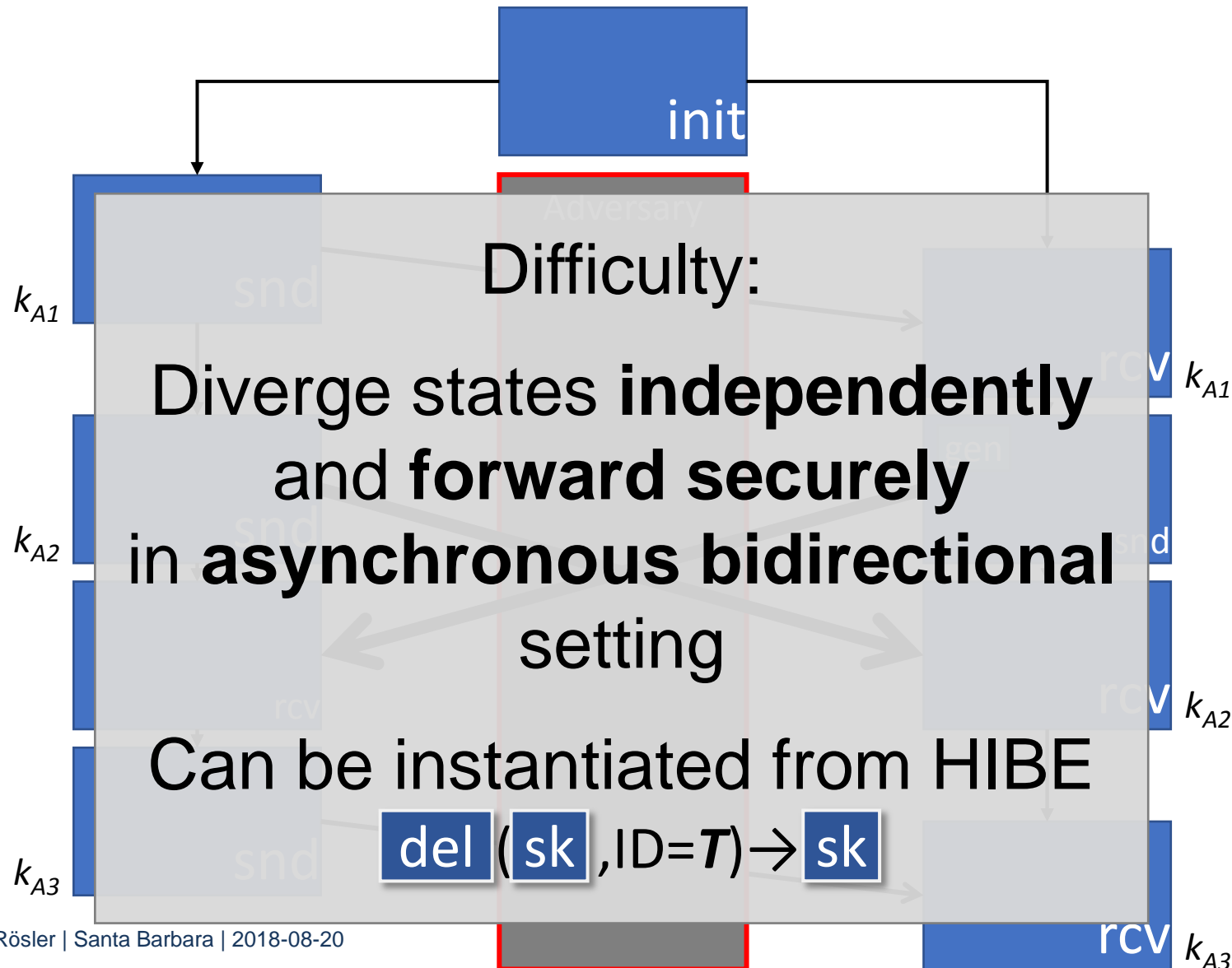
# Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Expose Bob
  - ⇒ No future Challenge if synchronous until Bob recovered
  - Forward secrecy and recovery of Bob's state
  - Send new **pk**
  - Divergence of states
  - Update key pair

**up** (**sk**,  $T$ ) → **sk**

**up** (**pk**,  $T$ ) → **pk**



# Constructing Sesquidirectional RKE

- What is Ratcheting?
- Modeling RKE
- Construction Intuition
- Results

- Expose Bob
- ⇒ No future Challenge if synchronous until Bob recovered

→ Forward secrecy and recovery of Bob's state

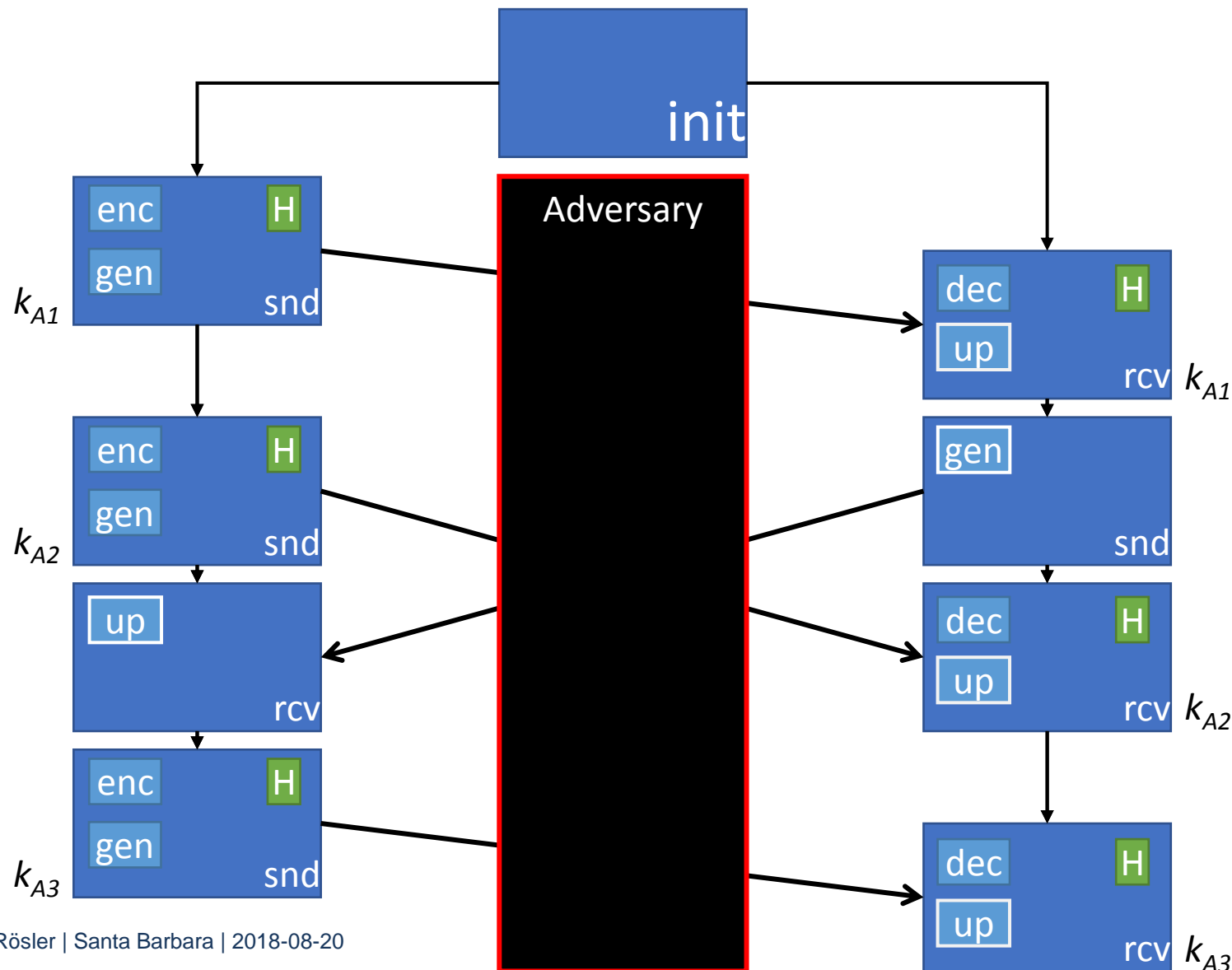
→ Send new **pk**

→ Divergence of states

→ Update key pair

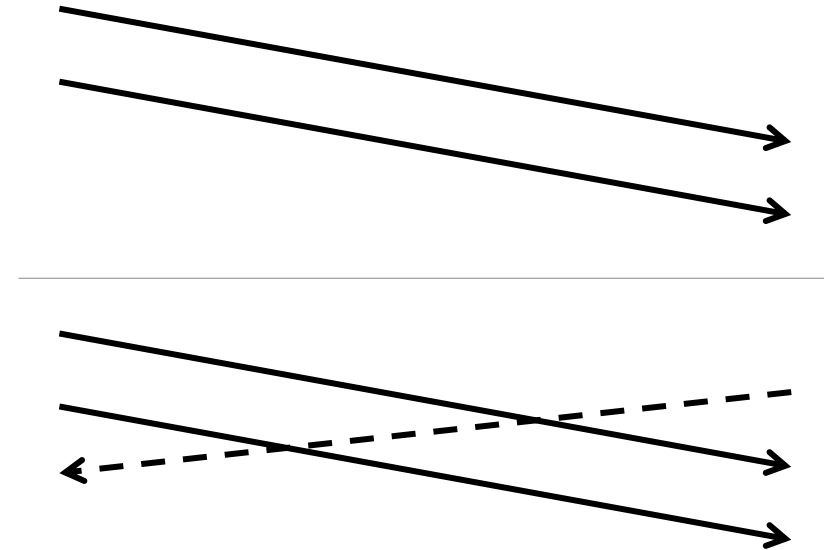
**up** (sk, T) → sk

**up** (pk, T) → pk



# Agenda

1. The Primitive Ratcheted Key Exchange
2. General Adversary Model
3. Unidirectional Ratcheting  
→ Model and Construction
4. Sesquidirectional Ratcheting  
→ Model and Construction
- 5. Results**



# Results

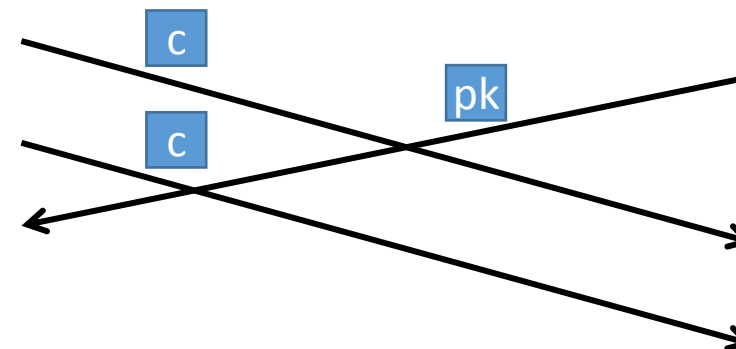
- Unidirectional RKE
  - KEM + ROM (+ MAC)

[ia.cr/2018/296](https://ia.cr/2018/296) (ext. version)

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# Results

- Unidirectional RKE
  - KEM + ROM (+ MAC)
- Sesquidirectional RKE
  - Key updatable KEM (+ signatures)
  - # `up` (`sk`  $\mathcal{T}$ ) = # *crossing* ciphertexts  
→ Depth of HIBE practically bounded

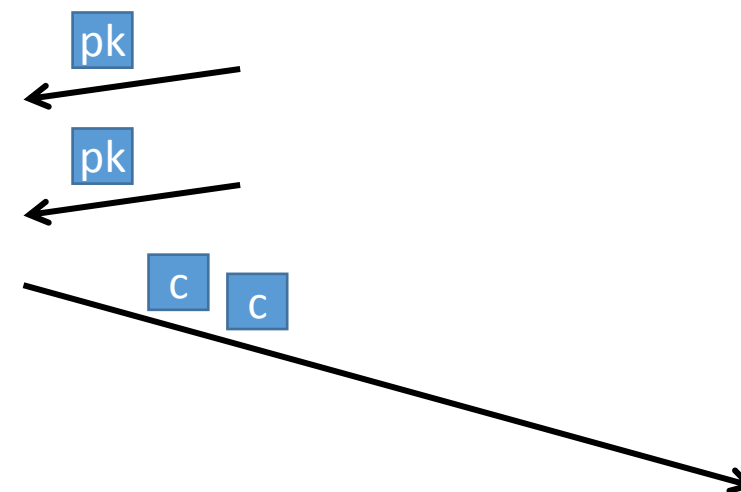


[ia.cr/2018/296](https://ia.cr/2018/296) (ext. version)

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# Results

- Unidirectional RKE
  - KEM + ROM (+ MAC)
- Sesquidirectional RKE
  - Key updatable KEM (+ signatures)
  - # `up` (`sk`  $\mathcal{T}$ ) = # *crossing* ciphertexts
    - Depth of HIBE practically bounded
  - Multi encapsulation
    - Bounded in ping-pong pattern
    - Alternative: key updatable signatures

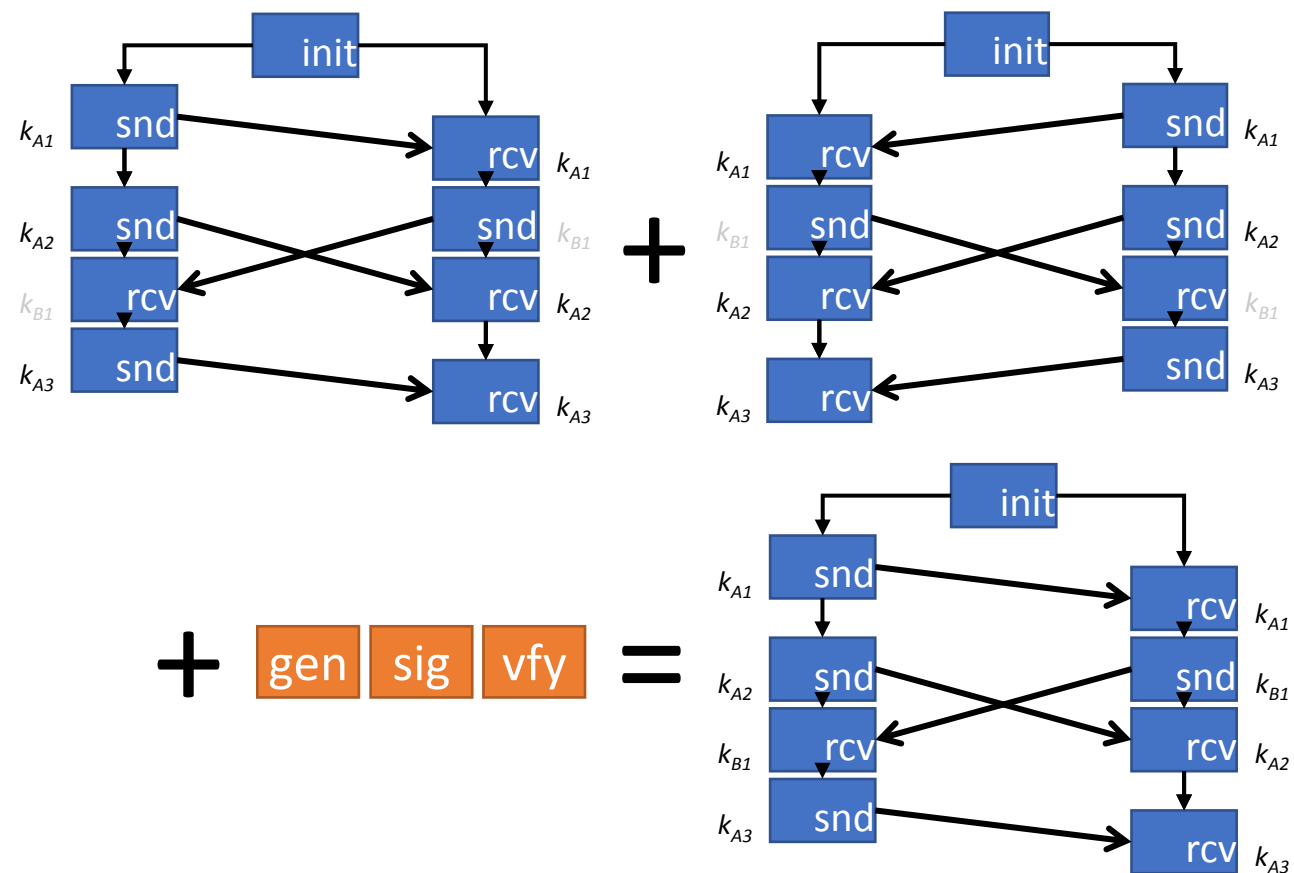


[ia.cr/2018/296](https://ia.cr/2018/296) (ext. version)

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# Results

- Unidirectional RKE
  - KEM + ROM (+ MAC)
- Sesquidirectional RKE
  - Key updatable KEM (+ signatures)
  - # `up` (`sk`  $T$ ) = #crossing ciphertexts
    - Depth of HIBE practically bounded
  - Multi encapsulation
    - Bounded in ping-pong pattern
    - Alternative: key updatable signatures
- BRKE = 2x SRKE + OT signatures
  - Build SRKE, BRKE too complex!



[ia.cr/2018/296](https://ia.cr/2018/296) (ext. version)

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