

Risky Traitor Tracing and New Differential Privacy Negative Results

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Hardness of Non-Interactive Differential Privacy from One-Way Functions

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Risky Traitor Tracing and New
Differential Privacy Negative Results

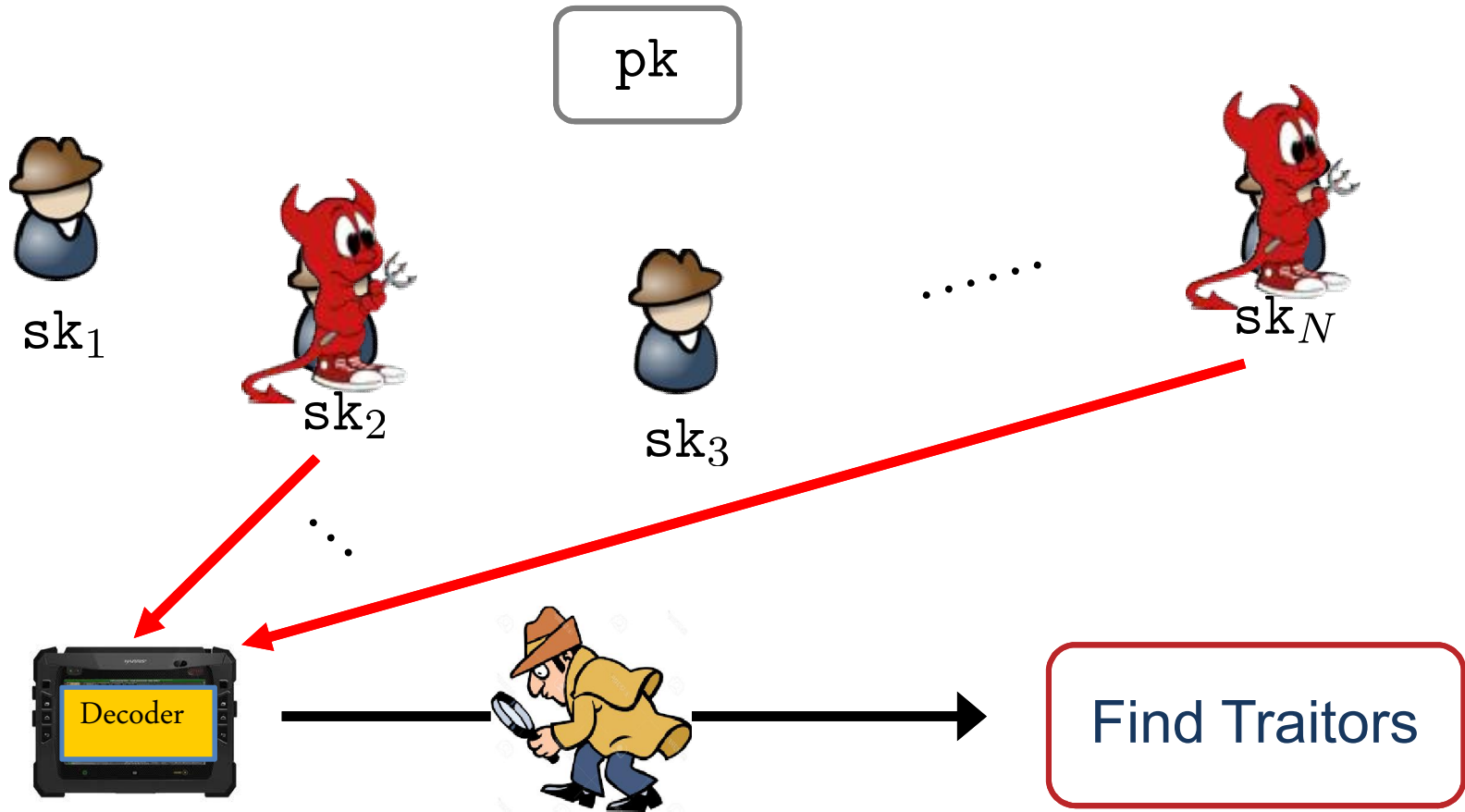
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Traitor Tracing [Chor-Fiat-Naor 94]



Key Challenges:

- (1) Obfuscated Decoder
- (2) Collusions

Tracing Algorithms

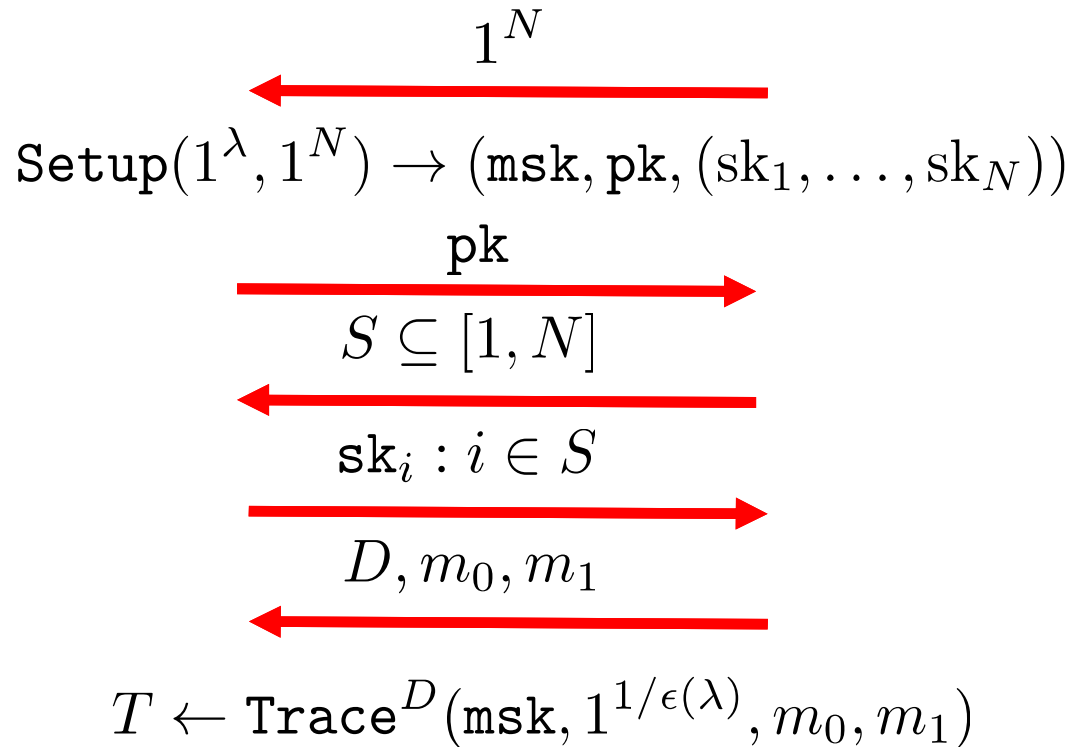
$\text{Setup}(1^\lambda, 1^N) \rightarrow (\text{msk}, \text{pk}, (\text{sk}_1, \dots, \text{sk}_N))$

$\text{Enc}(\text{pk}, m \in \mathcal{M}) \rightarrow \text{ct}$

$\text{Dec}(\text{sk}, \text{ct}) \rightarrow m \in \mathcal{M}$

$\text{Trace}^D(\text{msk}, 1^y, m_0, m_1) \rightarrow T \subseteq [1, N]$

ExptTT_{A,ε}(λ)



(1) No false trace: $\Pr[\exists i : i \in T, i \notin S] = \text{negl}(\lambda)$

(2) Catch: $\Pr[T \neq \emptyset] \geq \Pr[D \text{ } \epsilon\text{-distinguishes } (m_0, m_1)]$

It's About the Ciphertext Size!

PKE: $N \cdot \text{poly}(\lambda)$

Bilinear Maps [Boneh-Sahai-Waters06,Boneh-Waters06...]: $\sqrt{N} \cdot \text{poly}(\lambda)$

Functional Encryption/iO [GGHRSW13,Boneh-Zhandry14]: $\text{poly}(\lambda, \lg N) = \text{poly}(\lambda)$

Can we get better efficiency from standard assumptions if we relax tracing requirement?



(* Subsequent to this work, G-Koppula-Waters gave an LWE-based standard TT scheme matching FE/iO-based efficiency.)

Relaxing Tracing

Standard Traitor Tracing

(1) No false trace: $\Pr[\exists i : i \in T, i \notin S] = \text{negl}(\lambda)$

(2) Catch: $\Pr[T \neq \emptyset] \geq \Pr[D \text{ } \epsilon\text{-distinguishes } (m_0, m_1)]$

f(\cdot, \cdot)-*Risky* Traitor Tracing

(1) No false trace: $\Pr[\exists i : i \in T, i \notin S] = \text{negl}(\lambda)$

(2) Catch: $\Pr[T \neq \emptyset] \geq f(\lambda, n) \cdot \Pr[D \text{ } \epsilon\text{-distinguishes } (m_0, m_1)]$

(Main) Results [G-Koppula-Russell-Waters]

Theorem. Under simple assumptions over bilinear groups, we build a secure *f-risky Traitor Tracing* scheme with $|ct|$ ciphertext size.

$$\forall k > 0, \quad f(\lambda, N) = \frac{k}{N} \implies |ct| = O(k \cdot \lambda)$$

Theorem. Secure $\frac{1}{N}$ -*risky Traitor Tracing* scheme implies differential privacy negative results.

Remaining Talk

Part I: Risky Traitor Tracing

Part II: Differential Privacy Negative
Results (Luke)

Standalone Risky TT Applications

- Persistent decoder setting
 - Periodic key refreshes, decoder must work across cycles
 - Catching probability can be amplified
- Resource constrained settings
 - Get best possible tracing w/ 10 KB ciphertext overhead
- Risk averse attackers
 - Deterrence against attackers if traitors heavily penalized
 - Heavy penalty vs. Low catching probability

Framework for Risky TT – Mixed Bit Matching Encryption

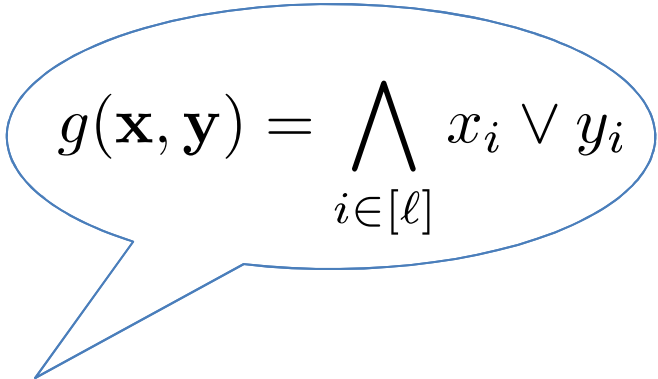
$$\text{Setup}(1^\lambda, 1^\ell) \rightarrow (\text{pk}, \text{msk})$$

$$\text{Enc-PK}(\text{pk}, m) \rightarrow \text{ct}$$

$$\text{Enc-SK}(\text{msk}, m, \mathbf{y} \in \{0, 1\}^\ell) \rightarrow \text{ct}$$

$$\text{KeyGen}(\text{msk}, \mathbf{x} \in \{0, 1\}^\ell) \rightarrow \text{sk}$$

$$\text{Dec}(\text{sk}, \text{ct}) \rightarrow m$$


$$g(\mathbf{x}, \mathbf{y}) = \bigwedge_{i \in [\ell]} x_i \vee y_i$$

Correctness Enc-PK: Dec outputs m

Correctness Enc-SK: Dec outputs m iff $g(\mathbf{x}, \mathbf{y}) = 1$

Mixed Bit Matching Security

Security: 3 properties

PK/SK CT Hiding

→

Distinguish

$\underline{\text{Enc-PK}}(\text{pk}, m)$ vs $\underline{\text{Enc-SK}}(\text{msk}, m, \underline{1^\ell})$

CT Hiding

→

Distinguish

$\text{Enc-SK}(\text{msk}, m_0, \underline{y_0})$ vs $\text{Enc-SK}(\text{msk}, m_1, \underline{y_1})$

Key Hiding

→

Distinguish

$\text{KeyGen}(\text{msk}, \underline{x_0})$ vs $\text{KeyGen}(\text{msk}, \underline{x_1})$

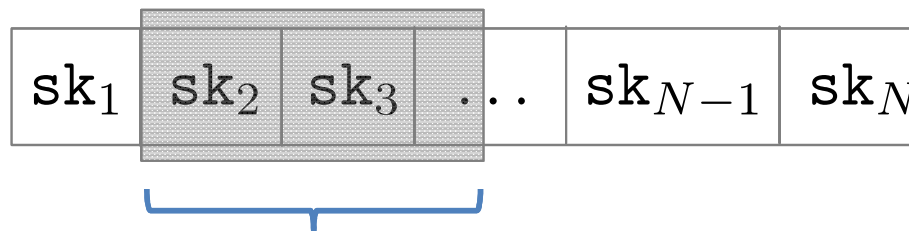
Transformation to Risky TT

$$\underline{\text{Setup}(1^\lambda, 1^N) \rightarrow (\text{pk}, \text{msk}, \{\text{sk}_i\}_{i \leq N})}$$

$$\text{mBME.Setup}(1^\lambda, 1^{k+1}) \rightarrow (\text{mbme.pk}, \text{mbme.msk})$$

$$\text{pk} = \text{mbme.pk}$$

$$\text{msk} = \text{mbme.msk}$$



Choose random window of size k

Transformation to Risky TT

$$\underline{\text{Setup}(1^\lambda, 1^N) \rightarrow (\text{pk}, \text{msk}, \{\text{sk}_i\}_{i \leq N})}$$

$$\text{mBME.Setup}(1^\lambda, 1^{k+1}) \rightarrow (\text{mbme.pk}, \text{mbme.msk})$$

Choose random target window start location $w \in [N - k]$

	mBME.KeyGen	
$\mathbf{x}_1, \dots, \mathbf{x}_{w-1} = 0\ 0 \ \dots \ 0\ 0\ 0$	\longrightarrow	$\text{sk}_1, \dots, \text{sk}_{w-1}$
$\mathbf{x}_w = 0\ 0 \ \dots \ 0\ 0\ 1$	\longrightarrow	sk_w
$\mathbf{x}_{w+1} = 0\ 0 \ \dots \ 0\ 1\ 1$	\longrightarrow	sk_{w+1}
$\vdots \quad \quad \quad \vdots \quad \quad \quad \ddots \quad \quad \quad \vdots$		\vdots
$\mathbf{x}_{w+k-1} = 0\ 1 \ \dots \ 1\ 1\ 1$	\longrightarrow	sk_{w+k-1}
$\mathbf{x}_{w+k}, \dots, \mathbf{x}_N = 1\ 1 \ \dots \ 1\ 1\ 1$	\longrightarrow	$\text{sk}_{w+k}, \dots, \text{sk}_N$

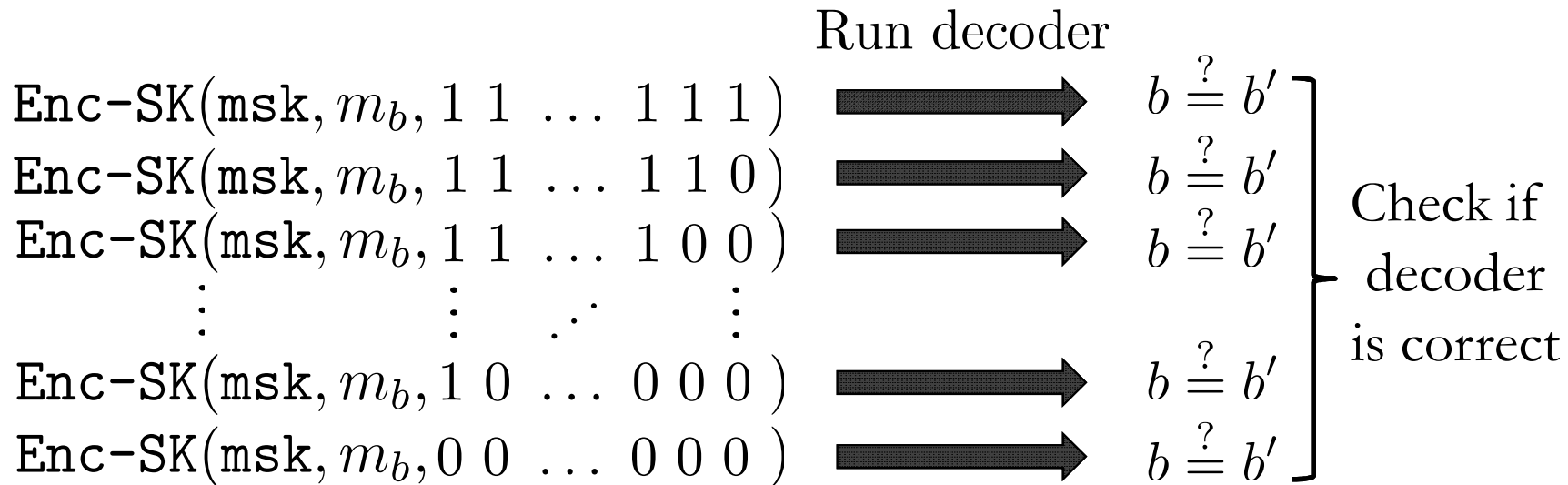
Transformation to Risky TT

$$\underline{\text{Enc}(\text{pk}, m) = \text{mBME}.\text{Enc-PK}(\text{pk}, m)}$$

$$\underline{\text{Dec}(\text{sk}, \text{ct}) = \text{mBME}.\text{Dec}(\text{sk}, \text{ct})}$$

Transformation to Risky TT

$$\underline{\text{Trace}^D(\text{msk}, 1^y, m_0, m_1) \rightarrow T}$$

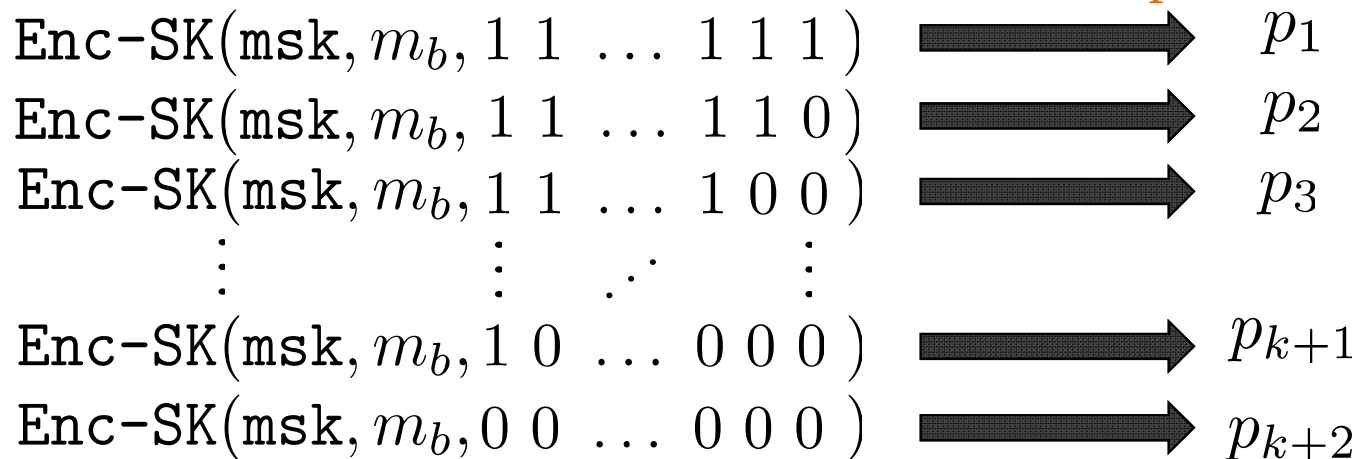


Do this poly times

Transformation to Risky TT

$$\underline{\text{Trace}^D(\text{msk}, 1^y, m_0, m_1) \rightarrow T}$$

Successful decryption
probability



If p_i and p_{i+1} are noticeably far, then
add index $(i + w - 1)$ to the set T

Missing Pieces and Other Results

- Security proof of the transformation
 - Significantly departs from existing proof techniques for TT
- Building Mixed Bit Matching Encryption from Bilinear Maps
- Generic risky amplification
 - Improving success probability of tracing

Remaining Talk

Part I: Building Risky Traitor Tracing

Part II: Differential Privacy Negative Results (Luke)

