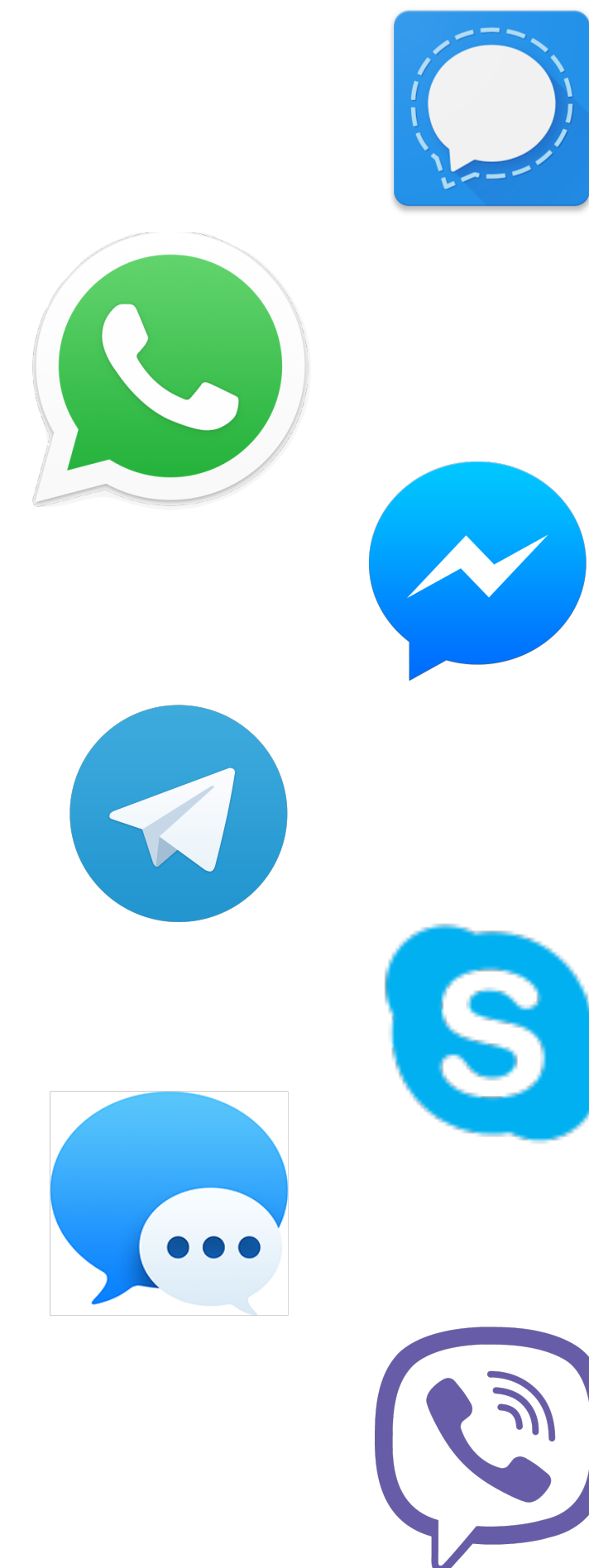


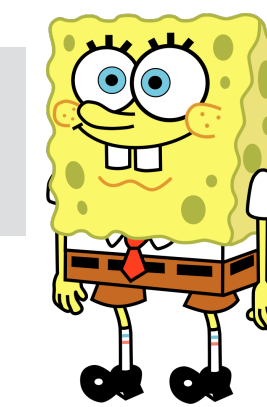
# Optimal Channel Security Against Fine-Grained State Compromise: The Safety of Messaging

Joseph Jaeger  
Igors Stepanovs





Alice and Bob want **E2E** secure communication



## Plenty of Theory ...

Symmetric encryption  
Asymmetric encryption  
Session key exchange  
Signatures

...

## But what about **E2E Tools**?



TLS is for web servers!



≠



PGP is a pain!

### **Why Johnny Can't Encrypt**

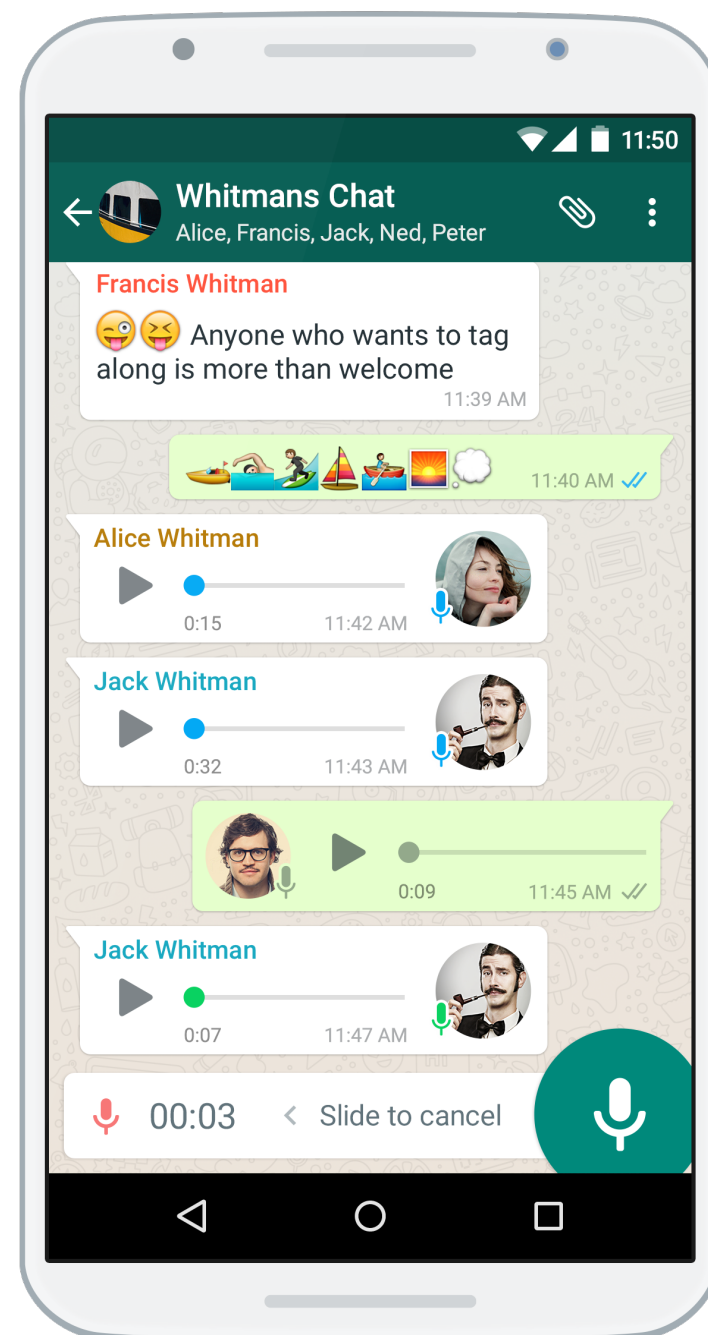
#### ***A Usability Evaluation of PGP 5.0***

ALMA WHITTEN AND J. D. TYGAR



Messaging Apps

Emerging as most  
convenient & usable.



# E2E Messaging Apps

Whatsapp alone encrypts ~55 billion messages/day.

~700 million iPhones in use.

## Apps Targeting E2E Security:



Signal



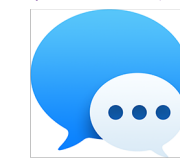
WhatsApp



Skype  
(Private Conversations)



Facebook Messenger  
(Secret Conversations)



iMessage

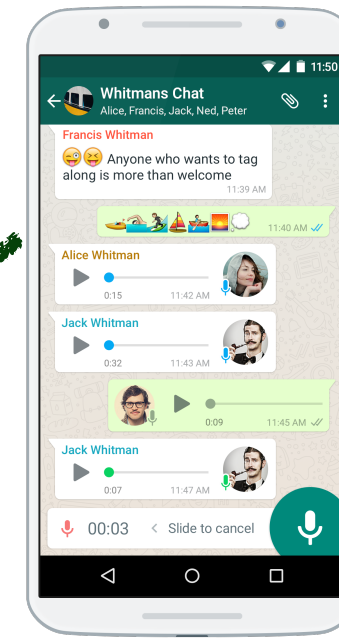


Telegram  
(Secret Chats)



Viber

Many more...



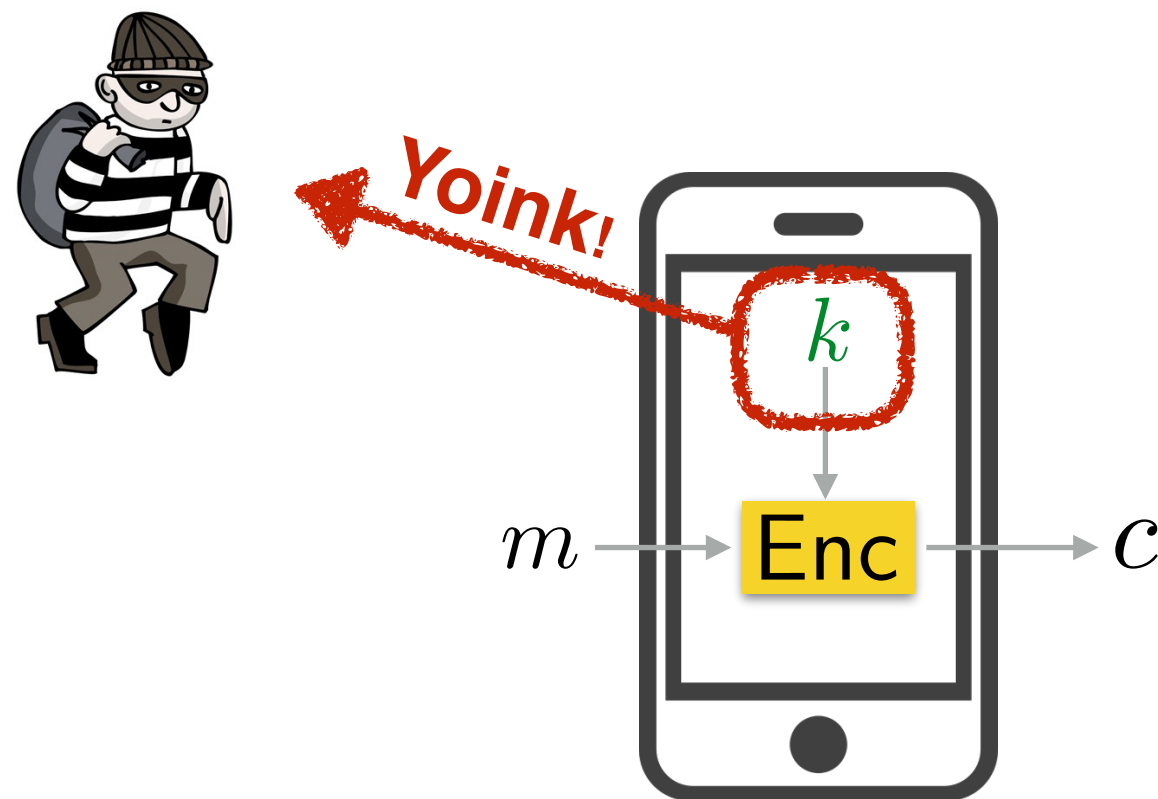
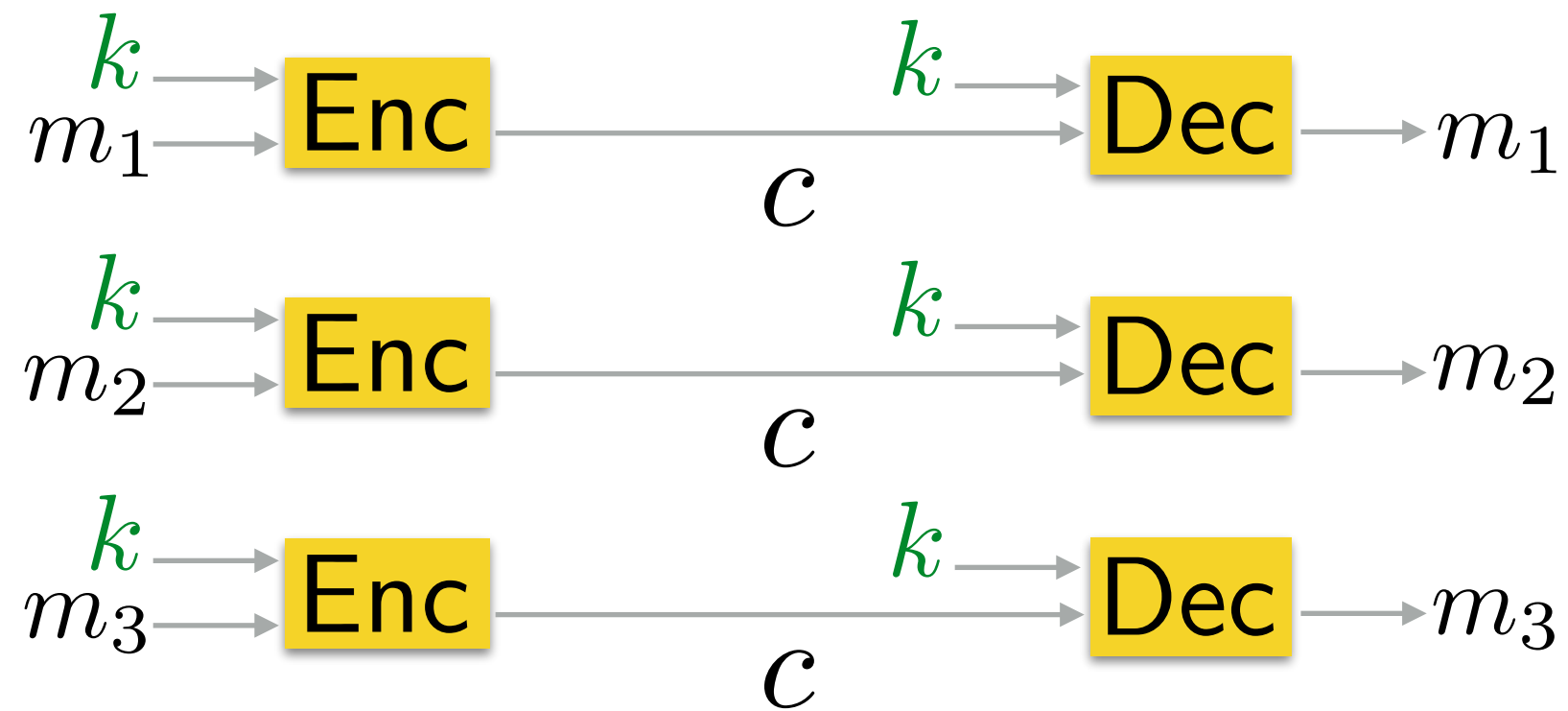
**Understanding their security is important!**

These are all based on Open Whisper System's  
**Double Ratchet Algorithm.** (i.e. the techniques of Signal)

We aim to better understand its **goal**:  
**Security against state compromise**

## Traditional Encryption

$$k \in \vec{K}_A \cap \vec{K}_B$$

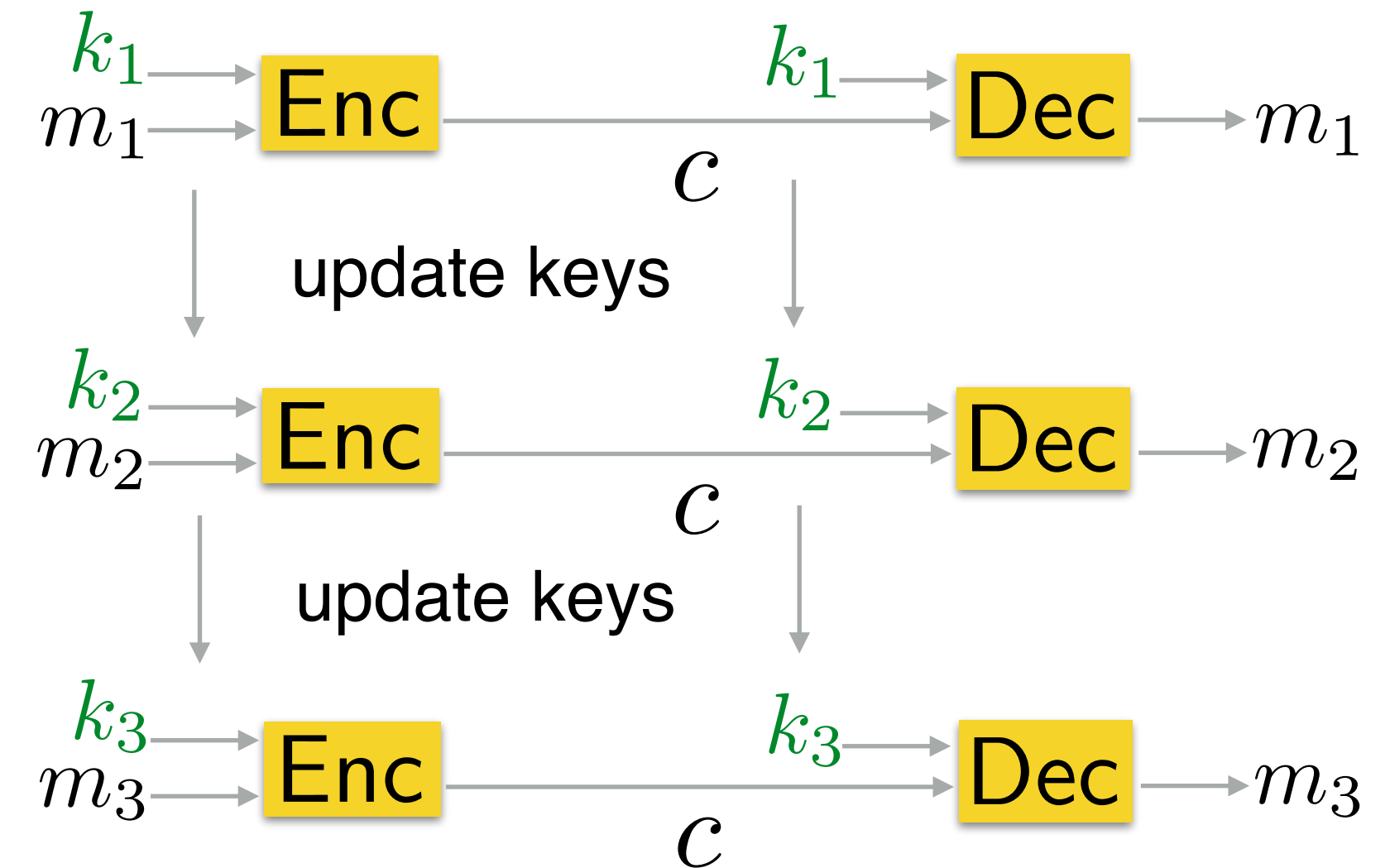


### How does attacker access secrets?

- Steals physical device
- Malware
- Border searches
- Unpatched vulnerabilities
- ...

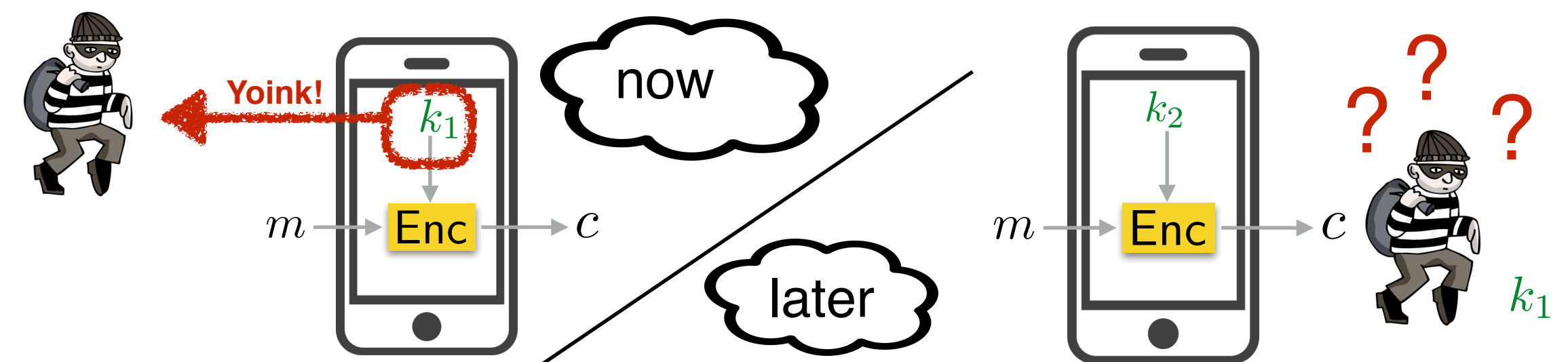
## Key Updating Encryption

$$k \in \vec{K}_A \cap \vec{K}_B$$



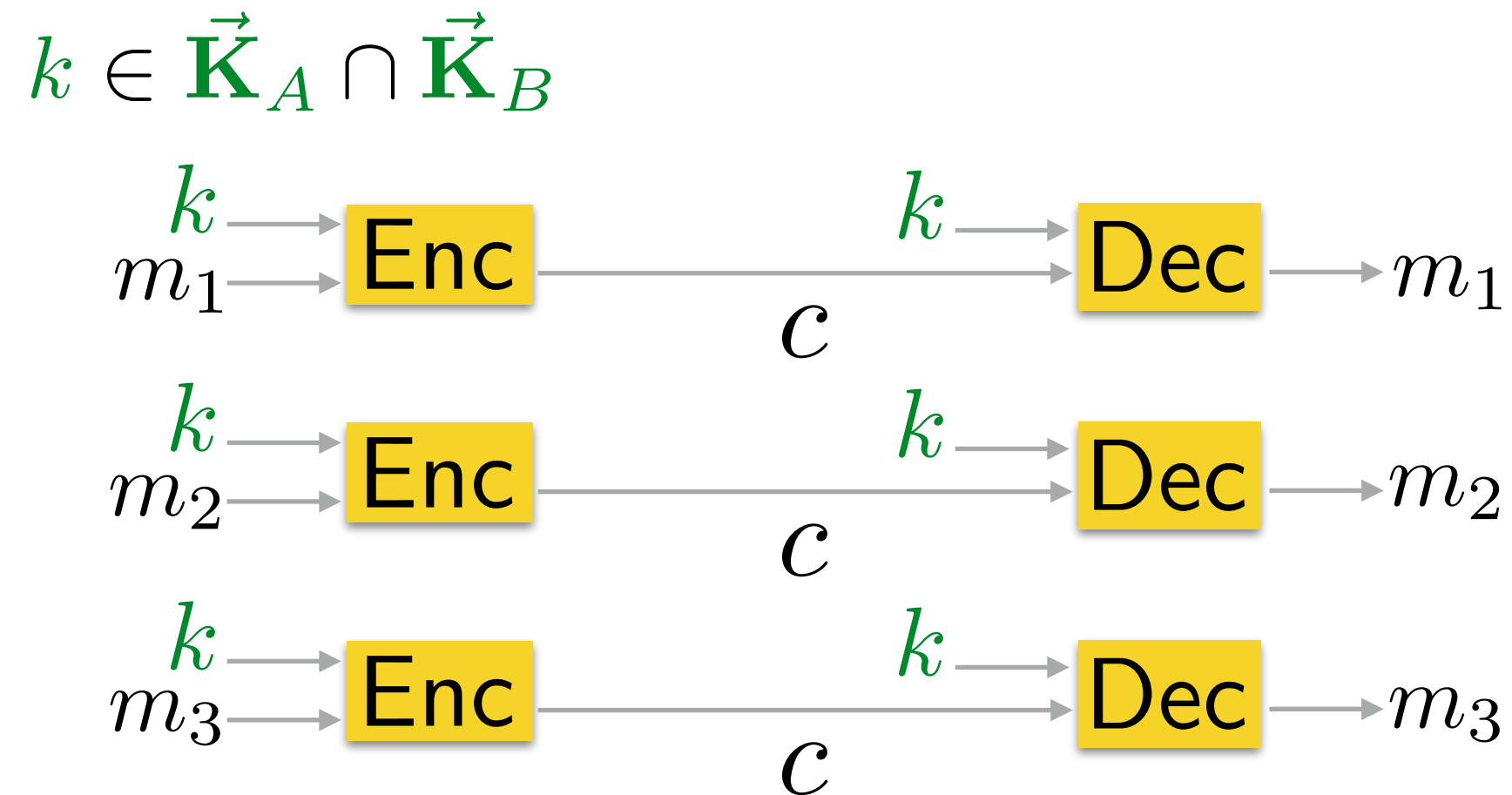
### Addressed in practice:

Messaging app designers in practice are trying to protect against this threat by updating the secret key using ratcheting.

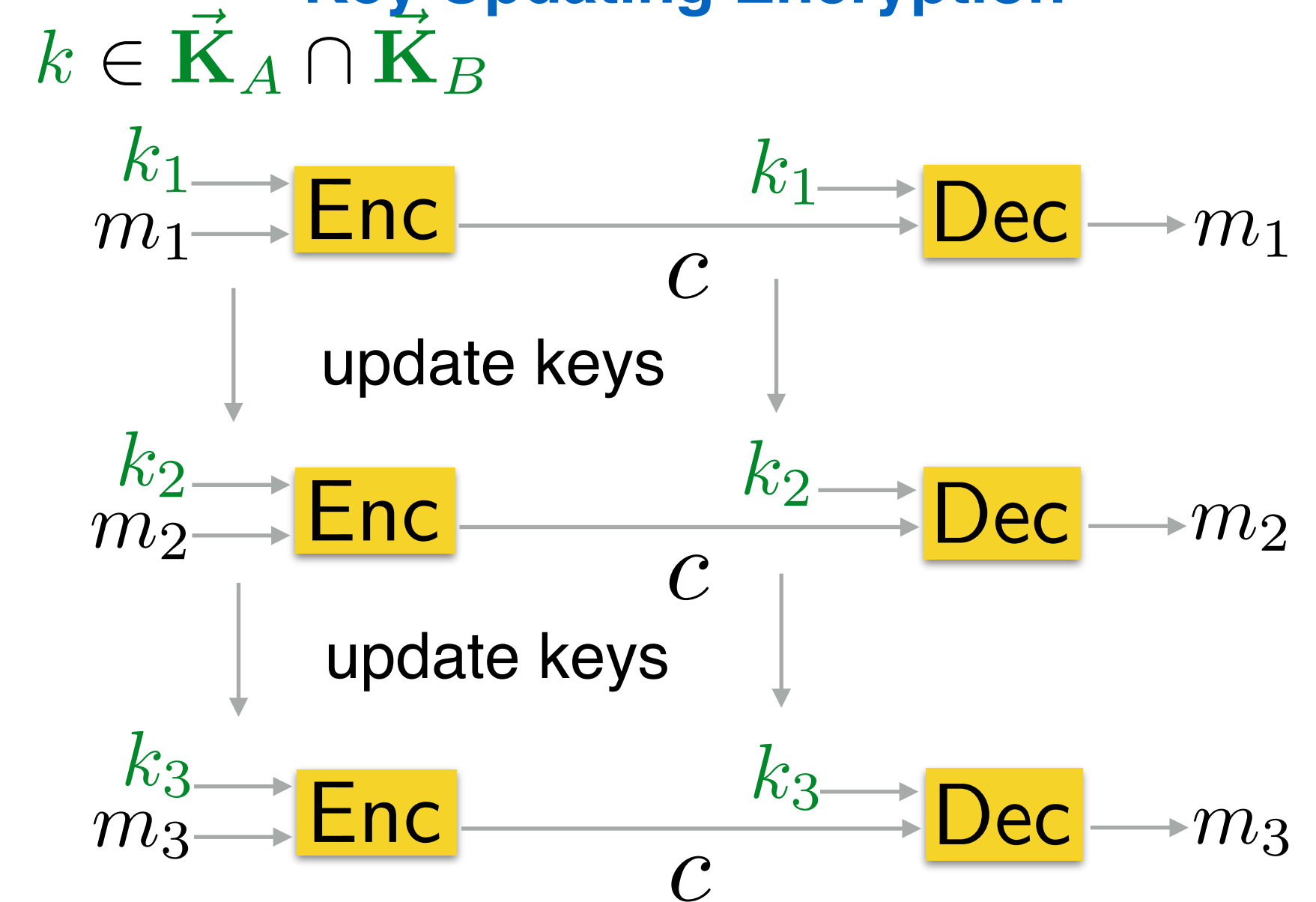




## Traditional Encryption



## Key Updating Encryption



### Informal goals:

- **Forward security:** prior keys or communications remain secure
- **Backward security:** future keys or communications remain secure

### Exactly what threat these goals prevent in practice needs careful consideration ...

- **Less useful when** threat is persistent malware than can directly exfiltrate messages.
- **More useful when** users delete old messages, malware exfiltrates keys instead of messages, malware's presence limited by software security.

Forward and backward security are of particular interest for secure messaging because conversations can be very long lived ... a chat session can stay open for a year ...

## Prior Work

What security goal does ratcheting achieve?

Formalize it

Show that ratcheting achieves it.

### A Formal Security Analysis of the Signal Messaging Protocol

Katriel Cohn-Gordon<sup>1</sup>, Cas Cremers<sup>1</sup>, Benjamin Dowling<sup>2</sup>, Luke Garratt<sup>1</sup>, and Douglas Stebila<sup>3</sup>

Analyzed entirety of Signal key exchange and ratcheting  
Does not model encryption

### Ratcheted Encryption and Key Exchange: The Security of Messaging

Mihir Bellare<sup>1(✉)</sup>, Asha Camper Singh<sup>2</sup>, Joseph Jaeger<sup>1</sup>, Maya Nyayapati<sup>2</sup>,  
and Igors Stepanovs<sup>1</sup>

Introduced ratcheted key exchange and ratcheted encryption.  
One-directional communication  
Only sender's state vulnerable

### Towards Bidirectional Ratcheted Key Exchange

Bertram Poettering<sup>1</sup> and Paul Rösler<sup>2(✉)</sup>

Extended ratcheted key exchange to be bidirectional  
Does not model encryption

## Prior Work

What security goal does ratcheting achieve?

Formalize it

Show that ratcheting achieves it.

## Our Work

What is the BEST POSSIBLE messaging security we can achieve in the face of fine-grained state compromise?

Formalize it

Show how to achieve it.

NOT ratcheting!

# Our Contributions

## Optimal Channel Security Against Fine-Grained State Compromise: The Safety of Messaging

Joseph Jaeger<sup>1</sup> and Igors Stepanovs<sup>1</sup>

1. Define **strongest possible** security of a **channel** against **fine-grained state compromise**.

2. Define **Key-Updatable Digital Signatures (KUDS)**  
**Key-Updatable Public-Key Encryption (KUPKE)**

Changed from proceedings version due to bugs in security proofs.

3. Constructions of **KUDS** and **KUPKE**.



5. **Proofs** that our constructions achieve our **strong** definitions of security.



## Our Threat Model

all preventable attacks should be prevented



We want the best achievable integrity and privacy.

Our **Adversary** has:

Complete control of communication.

Ability to arbitrarily and repeatedly expose secrets.

## Does this matter in practice?

Hard to say - requires better knowledge of attacks occurring in practice

## Can we just tweak Signal?

Probably not - seems to require fundamentally different techniques

## Does the Double Ratchet Algorithm (Signal) achieve this?

**Answer: No. For example an attacker can,**

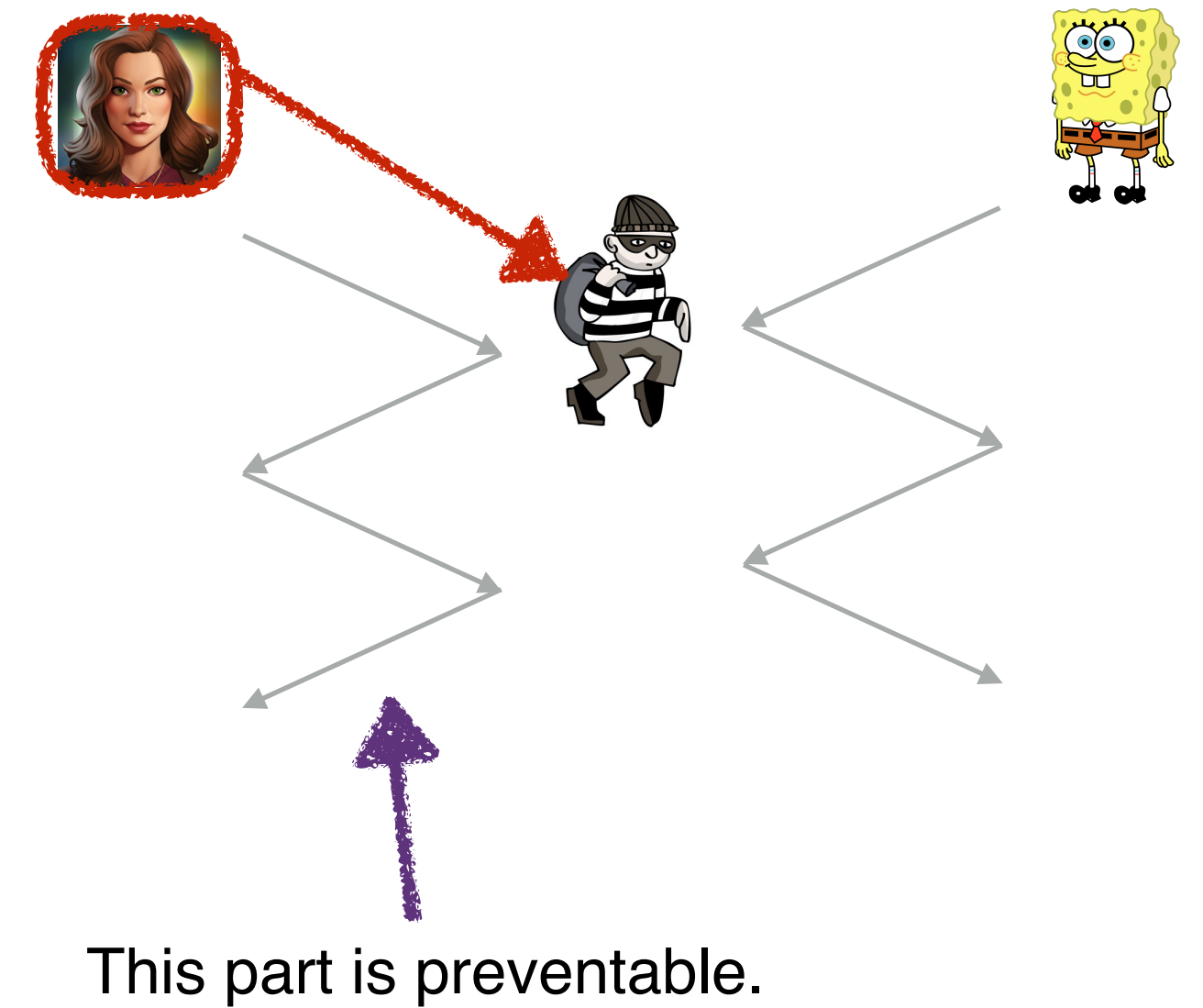
forge messages **to** an exposed user

read ciphertexts **from** an exposed user

and more

## An Implication:

One exposure allows perfect MITM

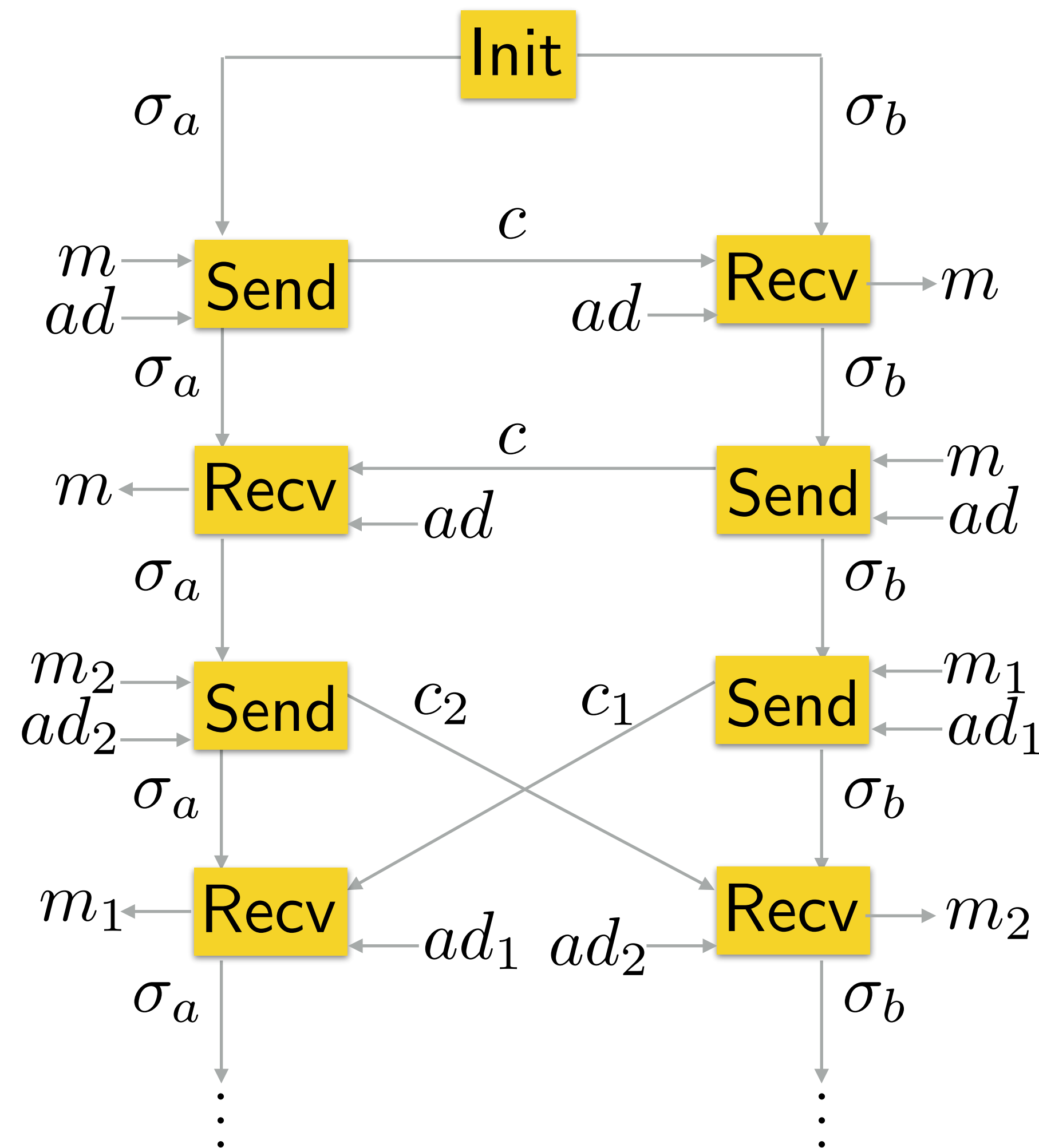


# (Bidirectional) Channel Syntax

From

Security Notions for Bidirectional Channels

Giorgia Azzurra Marson and Bertram Poettering



Stateful encryption...

Allowing bidirectional communication.

Allows messages to cross “on the wire”,  
But preserves message order in either direction.

# Defining security

## Step 1: specify interface

**SEND**( $u, m_0, m_1, ad$ )

party u encrypts one of two messages

**RECV**( $u, c, ad$ )

party u receives a ciphertext

**EXP**( $u, rand$ )

party u exposes secret state

### Attacker Goals:

- Tell which message is encrypted or
- Forge a new ciphertext

Game  $\text{INTER}_{\text{Ch}}^{\mathcal{D}}$

$b \leftarrow_{\$} \{0, 1\}$

$s_{\mathcal{I}} \leftarrow r_{\mathcal{I}} \leftarrow s_{\mathcal{R}} \leftarrow r_{\mathcal{R}} \leftarrow 0$

$(\sigma_{\mathcal{I}}, \sigma_{\mathcal{R}}) \leftarrow_{\$} \text{Ch.Init}$

$(z_{\mathcal{I}}, z_{\mathcal{R}}) \leftarrow_{\$} (\text{Ch.SendRS})^2$

$(\eta_{\mathcal{I}}, \eta_{\mathcal{R}}) \leftarrow_{\$} (\text{Ch.RecvRS})^2$

$b' \leftarrow_{\$} \mathcal{D}^{\text{SEND}, \text{RECV}, \text{EXP}}$

Return ( $b' = b$ )

SEND( $u, m_0, m_1, ad$ )

If nextop  $\neq (u, \text{"send"})$

and nextop  $\neq \perp$  then return  $\perp$

If  $|m_0| \neq |m_1|$  then return  $\perp$

$(\sigma_u, c) \leftarrow \text{Ch.Send}(\sigma_u, ad, m_b; z_u)$

nextop  $\leftarrow \perp$

$s_u \leftarrow s_u + 1; z_u \leftarrow_{\$} \text{Ch.SendRS}$

$\text{ctable}_{\bar{u}}[s_u] \leftarrow (c, ad)$

Return  $c$

RECV( $u, c, ad$ )

If nextop  $\neq (u, \text{"recv"})$

and nextop  $\neq \perp$  then return  $\perp$

$(\sigma_u, m) \leftarrow \text{Ch.Recv}(\sigma_u, ad, c; \eta_u)$

nextop  $\leftarrow \perp; \eta_u \leftarrow_{\$} \text{Ch.RecvRS}$

If  $m \neq \perp$  then  $r_u \leftarrow r_u + 1$

If  $b = 0$  and  $(c, ad) \neq \text{ctable}_u[r_u]$  then

Return  $m$

Return  $\perp$

EXP( $u, rand$ )

If nextop  $\neq \perp$  then return  $\perp$

$(z, \eta) \leftarrow (\varepsilon, \varepsilon)$

If rand = "send" then

nextop  $\leftarrow (u, \text{"send"}); z \leftarrow z_u$

Else if rand = "recv" then

nextop  $\leftarrow (u, \text{"recv"}); \eta \leftarrow \eta_u$

Return  $(\sigma_u, z, \eta)$

**Adversary has:**

Complete control of communication.

Ability to expose secrets.

# Defining security

## Step 2: generic attacks

We specified eight attacks that would break security of *any* channel.

### For Example

Expose state of one user  
and create forgery to other

Expose state of one user  
and decrypt ciphertext from other

Expose sending randomness of user  
to know which message is encrypted

### NOT generic attacks

(i.e. attacks we require security against)

Expose state of user  
and create forgery to same

Expose state of user  
and decrypt ciphertext from same

Adversary  $\mathcal{D}_1^{\text{SEND,RECV,EXP}}$   
 $(\sigma, z, \eta) \leftarrow \text{EXP}(\mathcal{I}, \varepsilon)$   
 $n \leftarrow \max_{c \in [\text{Ch.Send}(\sigma, \varepsilon, 1)]} |c|$   
 $m \leftarrow_{\$} \{0, 1\}^{n+2}$   
 $c \leftarrow \text{SEND}(\mathcal{I}, m, 1, \varepsilon)$   
 If  $|c| \leq n$  then return 1  
 Return 0

Adversary  $\mathcal{D}_2^{\text{SEND,RECV,EXP}}$   
 $c \leftarrow \text{SEND}(\mathcal{I}, 1, 1, \varepsilon)$   
 $m \leftarrow \text{RECV}(\mathcal{R}, c, \varepsilon)$   
 If  $m = \perp$  then return 1  
 Return 0

Adversary  $\mathcal{D}_3^{\text{SEND,RECV,EXP}}$   
 $(\sigma, z, \eta) \leftarrow \text{EXP}(\mathcal{I}, \varepsilon)$   
 $(\sigma, c) \leftarrow_{\$} \text{Ch.Send}(\sigma, \varepsilon, 1)$   
 $m \leftarrow \text{RECV}(\mathcal{R}, c, \varepsilon)$   
 If  $m = \perp$  then return 1  
 Return 0

Adversary  $\mathcal{D}_{3.1}^{\text{SEND,RECV,EXP}}$   
 $(\sigma, z, \eta) \leftarrow \text{EXP}(\mathcal{I}, \varepsilon)$   
 $(\sigma, c) \leftarrow_{\$} \text{Ch.Send}(\sigma, \varepsilon, 1)$   
 $m \leftarrow \text{RECV}(\mathcal{R}, c, \varepsilon)$   
 $(\sigma, c) \leftarrow_{\$} \text{Ch.Send}(\sigma, \varepsilon, 1)$   
 $m \leftarrow \text{RECV}(\mathcal{R}, c, \varepsilon)$   
 If  $m = \perp$  then return 1  
 Return 0

Adversary  $\mathcal{D}_{3.2}^{\text{SEND,RECV,EXP}}$   
 $(\sigma, z, \eta) \leftarrow \text{EXP}(\mathcal{I}, \varepsilon)$   
 $(\sigma, c) \leftarrow_{\$} \text{Ch.Send}(\sigma, \varepsilon, 1)$   
 $m \leftarrow \text{RECV}(\mathcal{R}, c, \varepsilon)$   
 $c \leftarrow \text{SEND}(\mathcal{R}, 0, 1, \varepsilon)$   
 $(\sigma, m) \leftarrow_{\$} \text{Ch.Recv}(\sigma, \varepsilon, c)$   
 If  $m = 1$  then return 1  
 Return 0

Adversary  $\mathcal{D}_4^{\text{SEND,RECV,EXP}}$   
 $c \leftarrow \text{SEND}(\mathcal{I}, 0, 1, \varepsilon)$   
 $(\sigma, z, \eta) \leftarrow \text{EXP}(\mathcal{R}, \varepsilon)$   
 $(\sigma, m) \leftarrow_{\$} \text{Ch.Recv}(\sigma, \varepsilon, c)$   
 If  $m = 1$  then return 1  
 Return 0

Adversary  $\mathcal{D}_5^{\text{SEND,RECV,EXP}}$   
 $(\sigma, z, \eta) \leftarrow \text{EXP}(\mathcal{R}, \varepsilon)$   
 $c \leftarrow \text{SEND}(\mathcal{I}, 0, 1, \varepsilon)$   
 $(\sigma, m) \leftarrow_{\$} \text{Ch.Recv}(\sigma, \varepsilon, c)$   
 If  $m = 1$  then return 1  
 Return 0

Adversary  $\mathcal{D}_6^{\text{SEND,RECV,EXP}}$   
 $(\sigma, z, \eta) \leftarrow \text{EXP}(\mathcal{I}, \text{"send"})$   
 $(\sigma, c) \leftarrow \text{Ch.Send}(\sigma, \varepsilon, 1; z)$   
 $c' \leftarrow \text{SEND}(\mathcal{I}, 0, 1, \varepsilon)$   
 If  $c' = c$  then return 1  
 Return 0



# Defining security

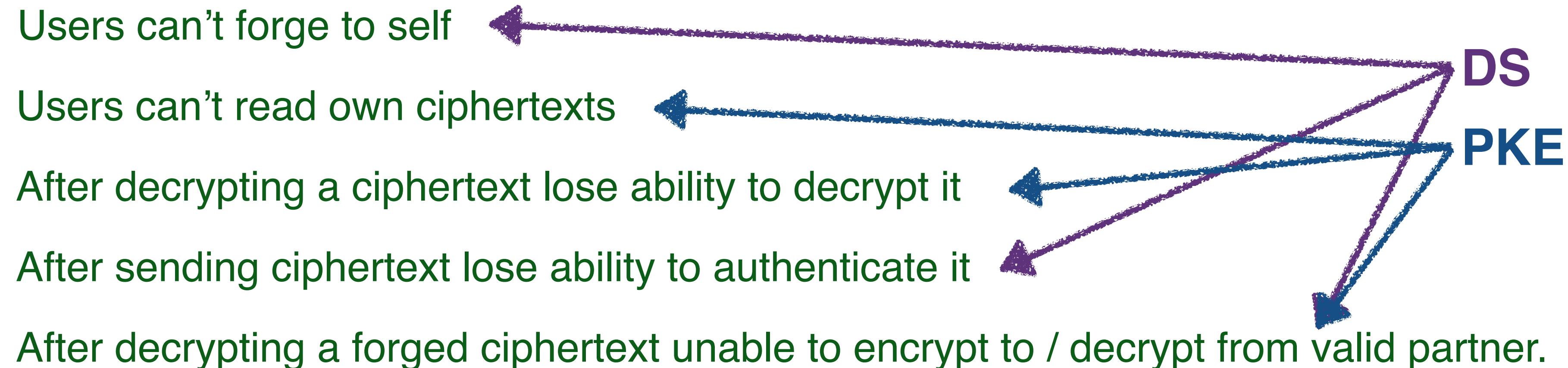
## Step 3: augment interface

Our security definition **AEAC**:  
(Authenticated encryption against compromise)

Added minimal restrictions to disallow generic attacks

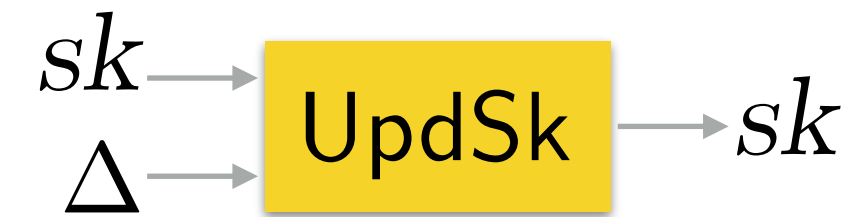
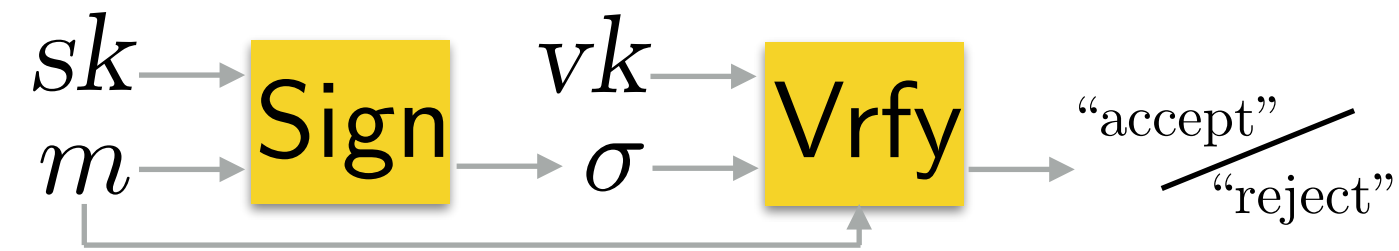
<p><u>Game AEAC<sub>Ch</sub><sup>D</sup></u> <math>b \leftarrow \{0, 1\}</math>; <math>s_I \leftarrow r_I \leftarrow s_R \leftarrow r_R \leftarrow 0</math> <math>\text{restricted}_I \leftarrow \text{false}</math>; <math>\text{restricted}_R \leftarrow \text{false}</math> <math>\text{forg}_I[\cdot] \leftarrow \text{"nontriv"}</math>; <math>\text{forg}_R[\cdot] \leftarrow \text{"nontriv"}</math> <math>\mathcal{X}_I \leftarrow \mathcal{X}_R \leftarrow 0</math>; <math>(st_I, st_R) \leftarrow \text{Ch.Init}</math> <math>(z_I, z_R) \leftarrow (\text{Ch.SendRS})^2</math> <math>(\eta_I, \eta_R) \leftarrow (\text{Ch.RecvRS})^2</math> <math>b' \leftarrow \mathcal{D}^{\text{SEND, RECV, EXP}}</math> Return <math>(b' = b)</math></p> <p><u>SEND(<math>u, m_0, m_1, ad</math>)</u> Require <math>\text{nextop} \in \{(u, \text{"send"}), \perp\}</math> Require <math> m_0  =  m_1 </math> If <math>r_u &lt; \mathcal{X}_u</math> or <math>\text{restricted}_u</math> or <math>\text{ch}_u[s_u + 1] = \text{"forb"}</math>:   Require <math>m_0 = m_1</math> <math>(st_u, c) \leftarrow \text{Ch.Send}(st_u, ad, m_b; z)</math> <math>\text{nextop} \leftarrow \perp</math>; <math>s_u \leftarrow s_u + 1</math>; <math>z_u \leftarrow \text{Ch.SendRS}</math> If <math>\neg \text{restricted}_u</math>: <math>\text{cad}_u[s_u] \leftarrow (c, ad)</math> If <math>m_0 \neq m_1</math>: <math>\text{ch}_u[s_u] \leftarrow \text{"done"}</math> Return <math>c</math></p>	<p><u>RECV(<math>u, c, ad</math>)</u> Require <math>\text{nextop} \in \{(u, \text{"recv"}), \perp\}</math> <math>(st_u, m) \leftarrow \text{Ch.Recv}(st_u, ad, c; \eta_u)</math> <math>\text{nextop} \leftarrow \perp</math>; <math>\eta_u \leftarrow \text{Ch.RecvRS}</math> If <math>m = \perp</math>: return <math>\perp</math> <math>r_u \leftarrow r_u + 1</math> If <math>\text{forg}_u[r_u] = \text{"triv"}</math> and <math>(c, ad) \neq \text{cad}_u[r_u]</math>:   <math>\text{restricted}_u \leftarrow \text{true}</math> If <math>\text{restricted}_u</math> or <math>(b = 0 \text{ and } (c, ad) \neq \text{cad}_u[r_u])</math>:   Return <math>m</math> Return <math>\perp</math></p> <p><u>EXP(<math>u, \text{rand}</math>)</u> // <math>\text{rand} \in \{\varepsilon, \text{"send"}, \text{"recv"}\}</math> Require <math>\text{nextop} = \perp</math> If <math>\text{restricted}_u</math>: Return <math>(st_u, z_u, \eta_u)</math> If <math>\exists i \in (r_u, s_u]</math> s.t. <math>\text{ch}_u[i] = \text{"done"}</math>:   Return <math>\perp</math> <math>\text{forg}_u[s_u + 1] \leftarrow \text{"triv"}</math>; <math>(z, \eta) \leftarrow (\varepsilon, \varepsilon)</math>; <math>\mathcal{X}_u \leftarrow s_u + 1</math> If <math>\text{rand} = \text{"send"}</math> then   <math>\text{nextop} \leftarrow (u, \text{"send"})</math>; <math>z \leftarrow z_u</math>; <math>\mathcal{X}_u \leftarrow s_u + 2</math>   <math>\text{forg}_u[s_u + 2] \leftarrow \text{"triv"}</math>; <math>\text{ch}_u[s_u + 1] \leftarrow \text{"forb"}</math> Else if <math>\text{rand} = \text{"recv"}</math> then   <math>\text{nextop} \leftarrow (u, \text{"recv"})</math>; <math>\eta \leftarrow \eta_u</math> Return <math>(st_u, z, \eta)</math></p>
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### Some implications



# Key-Updatable Digital Signature Schemes

## New Public Key Primitives



**Syntax** Augment DS scheme with algorithms to update keys with respect to arbitrary strings.

**Security** Variant of (one-time) strong unforgeability.

**SIGN**( $m$ )

**UPD**( $\Delta$ )

**EXP**( )

Forgery to a sequence of updates  $\vec{\Delta}_1$  disallowed if exposed key for  $\vec{\Delta}_2 \subseteq \vec{\Delta}_1$

**Construction** From a forward-secure DS scheme.

To update key, sign update string then evolve to future key.

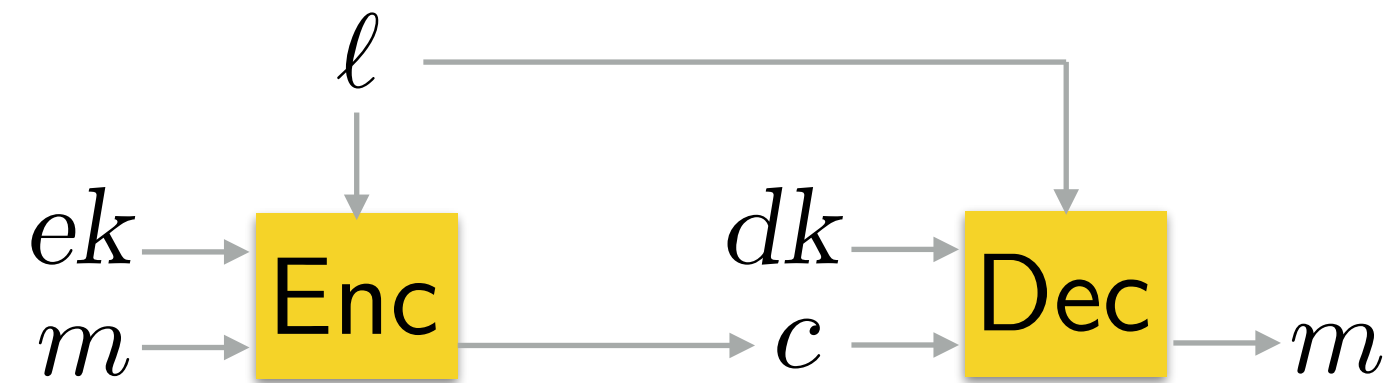
Algorithm  $\text{DS}_{\text{KU}}.\text{UpdSk}(sk, \Delta)$

---

$(sk_{\text{KE}}, i, \Sigma) \leftarrow sk$   
 $\Sigma[i] \leftarrow \$ \text{DS}_{\text{KE}}.\text{Sign}(sk_{\text{KE}}, 0 \parallel \Delta)$   
 $sk_{\text{KE}} \leftarrow \$ \text{DS}_{\text{KE}}.\text{Up}(sk_{\text{KE}})$   
 $sk \leftarrow (sk_{\text{KE}}, i + 1, \Sigma)$   
 Return  $sk$

## Key-Updatable Public Key Encryption

## New Public Key Primitives



**Syntax** Augment PKE scheme with algorithms to update keys with respect to arbitrary strings.

**Security** Variant of CCA-security with labels

$\text{ENC}(m_0, m_1, \ell)$

$\text{DEC}(c, \ell)$

$\text{UPDDK}()$

$\text{UPDEK}()$

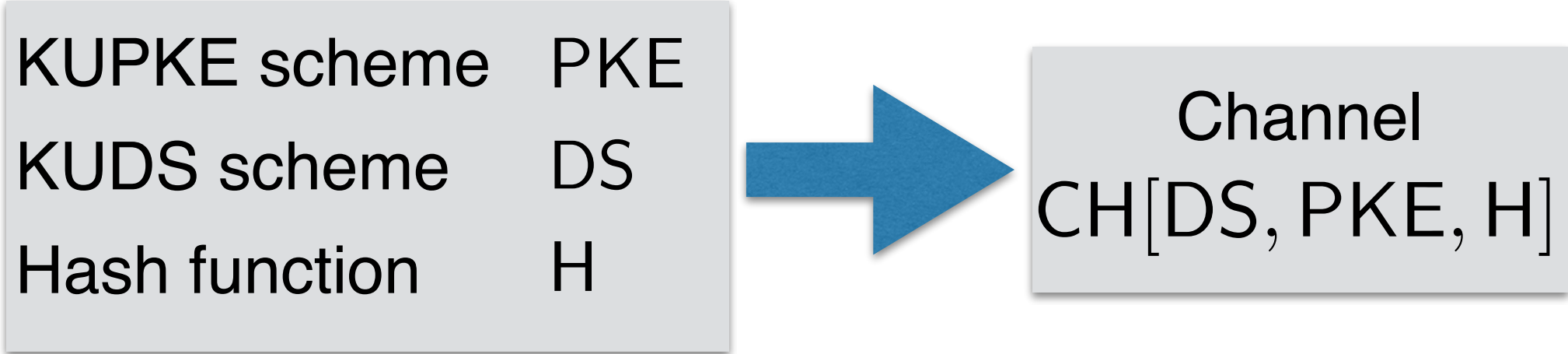
$\text{EXP}()$

Challenge query to sequence of updates  $\vec{\Delta}_1$  disallowed if exposed key for  $\vec{\Delta}_2 \subseteq \vec{\Delta}_1$

**Construction** Immediate from a hierarchical identity-based encryption scheme.  
(Update strings correspond to HIBE identities.)



# Our Construction



## State stored by each party

$s/r$	Sent/Received Counters
$sk/ek$	Signing/Encryption Keys
$vk/\vec{dk}$	Verification/Decryption Keys
$\tau_r/\vec{\tau}_s$	Sent/Received "Transcripts"
$hk$	Hash Function Key

### Algorithm SCh.Send( $\sigma, ad, m$ )

$(s, r, r^{ack}, sk, vk, ek, dk, hk, \tau_r, \vec{\tau}_s) \leftarrow \sigma ; s \leftarrow s + 1$   
 $(sk', vk') \leftarrow \$ DS.Kg ; (ek', dk[s]) \leftarrow \$ PKE.Kg$   
 $\ell \leftarrow (s, r, ad, vk', ek', \tau_r, \vec{\tau}_s[s - 1])$   
 $(ek', c') \leftarrow \$ PKE.Enc(ek, \ell, m, \vec{\tau}_s[r^{ack} + 1, \dots, s - 1])$   
 $v \leftarrow (c', \ell) ; \sigma \leftarrow \$ DS.Sign(sk, v)$   
 $c \leftarrow (\sigma, v) ; \vec{\tau}_s[s] \leftarrow H.Ev(hk, c)$   
 $\sigma \leftarrow (s, r, r^{ack}, sk', vk, ek, dk, hk, \tau_r, \vec{\tau}_s)$   
Return  $(\sigma, c)$

**Privacy** from PKE.

**Integrity** from DS

New keys with every message  
(**Forward/Backward security**)

Key-updates (**Forward security**)  
•  $ek/vk$  updated with sent transcripts  
•  $dk/sk$  update with received transcripts

Counter prevents **reordering**

Paper has 9 attacks against variants



# Security of our Bidirectional Channel

**Theorem:** Suppose

- $H$  is collision-resistant.
- $DS$  is a UFEXP-secure and UNIQ-secure KUDS scheme.
- $PKE$  is an INDEXP-secure KUPKE scheme.

Then our channel,  $SCh = SCH[DS, PKE, H]$  is AEAC-secure.

Tight reduction to multi-user security of underlying primitives.

**Concretely:** Given adversary  $\mathcal{D}$  (making  $q$  queries) we build adversaries  $\mathcal{A}_H, \mathcal{A}_{DS}, \mathcal{B}_{DS}, \mathcal{A}_{PKE}$  such that

$$\text{Adv}_{SCh, \mathcal{D}}^{\text{aeac}} \leq 2(q2^{-\mu} + \text{Adv}_{H, \mathcal{A}_H}^{\text{cr}} + \text{Adv}_{DS, \mathcal{A}_{DS}}^{\text{ufexp}} + \text{Adv}_{DS, \mathcal{B}_{DS}}^{\text{uniq}}) + \text{Adv}_{PKE, \mathcal{A}_{PKE}}^{\text{indexp}}$$

Where  $\mu = H_{\infty}(DS.Kg) + H_{\infty}(PKE.Kg) + H_{\infty}(PKE.Enc)$

## Proof

**Step 1:** Integrity.

**Substep 1.1:** Cannot predict future ciphertext. (Min-entropy)

**Substep 1.2:** Cannot cause transcript collision. (HF security)

**Substep 1.3:** Cannot forge signatures. (DS security)

**Step 2:** Privacy.

**Substep 2.1:** Cannot send ciphertext with new signature. (DS uniqueness)


**Substep 2.2:** Encryption is secure. (PKE security)

Subtle proof step missed by some related papers

## Our Contributions

### Optimal Channel Security Against Fine-Grained State Compromise: The Safety of Messaging

Joseph Jaeger<sup>1</sup> and Igors Stepanovs<sup>1</sup>

1. Define **strongest possible** security of a **channel** against **fine-grained state compromise**.
2. Define **Key-Updatable Digital Signatures (KUDS)**  
**Key-Updatable Public-Key Encryption (KUPKE)**
3. Constructions of **KUDS** and **KUPKE**.
4. 

```
graph LR; A[KUDS scheme] --> C[Construction]; B[KUPKE scheme] --> C; D[Hash function] --> C; C --> E[Secure Channel]
```
5. **Proofs** that our constructions achieve our **strong** definitions of security.

**Thanks! Any questions?**