

# Breaking the Bluetooth Pairing – The Fixed Coordinate Invalid Curve Attack

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Workshop on Attacks in Cryptography 2

# Overview

- Bluetooth is a widely deployed platform for wireless communication between mobile devices.
- Examples:
  - Mobile computers – mobile-phones and laptops.
  - Computer peripherals – mice and keyboards.
  - Wearable smart devices – fitness tracker and smart watches.
  - Audio equipments – wireless headphones and speakers.
  - IoT – smart door locks and smart lights.



- The Bluetooth standard is comprised of two main protocols
  - Bluetooth BR/EDR, and
  - Bluetooth Low Energy (aka. Bluetooth Smart)
- Both protocols promise to provide confidentiality and MitM protection.
- In this talk we show that none of these protocols provide the promised protections.

# Bluetooth Pairing

- The Bluetooth pairing establishes connection between two devices.
- The latest pairing protocols are
  - Bluetooth BR/EDR – Secure Simple Pairing (SSP)
  - Bluetooth Low Energy – Low Energy Secure Connections (LE SC)
- Both LE SC and SSP are variants of authenticated Elliptic-Curve Diffie-Hellman protocol for key-exchange.

# Legacy Pairing Eavesdropping Attack

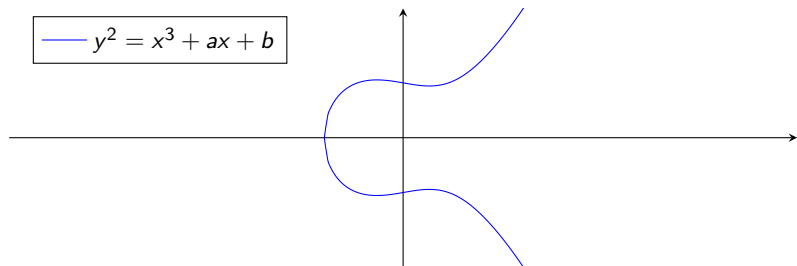
- From [R13] BTLE “Legacy Pairing” is vulnerable to an eavesdropping attack.
  - Legacy Pairing is protected by a 6-digit decimal mutual temporary key.
  - The attack recovers the session key by exhaustively searching through all million possible temporary keys.
  - This vulnerability was mitigated by LE SC using ECDH.
- There is an open-source software that recovers the session key from captured Legacy Pairing traffic.



# Introduction to Elliptic Curves

- Elliptic curves over finite fields are defined by group equation and the underlying field  $\mathbb{F}_q$ .<sup>1</sup>
- Consider curves in Weierstrass form

$$y^2 = x^3 + ax + b.$$



<sup>1</sup>The figures are drawn over  $\mathbb{R}$  for intuition, while the formulae are defined over  $\mathbb{F}_q$  as used in cryptography.

# Introduction to Elliptic Curves

- The elements of the group are:
  - All pairs  $P = (P_x, P_y) \in \mathbb{F}_q^2$  that satisfy the curve equation.
  - An identity element called *point-at-infinity* denoted by  $\infty$ .
- The group operation is point addition denoted by  $+$ .
- Point inverse is denoted by  $[-1]P$ .
- Scalar Multiplication denoted by  $[\alpha]P$  is defined to be the sum

$$\sum_{i=1}^{\alpha} P.$$

# Introduction to Elliptic Curves

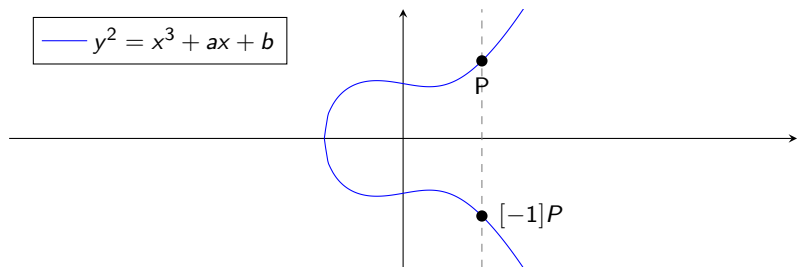
- The group operation is point addition.
- The use the following notations:
  - Point Addition – Adding two group elements  $P, Q \in E$ , st.  $P \neq Q$ .
  - Point Doubling – Adding a group element  $P \in E$  to itself.
  - Repeated Addition – Denote  $[\alpha]P$  to be the sum of  $\alpha$  times repeated additions of  $P$  to itself.



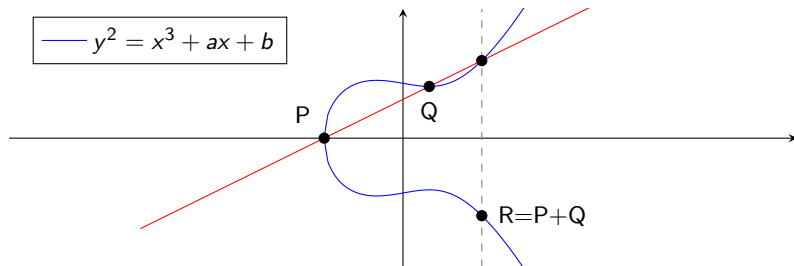
# Point Inversion

- Given a point  $P = (P_x, P_y)$  the inverse of  $P$  is computed by reflecting it across the  $x$ -axis

$$[-1]P = (P_x, -P_y).$$



# Point Addition



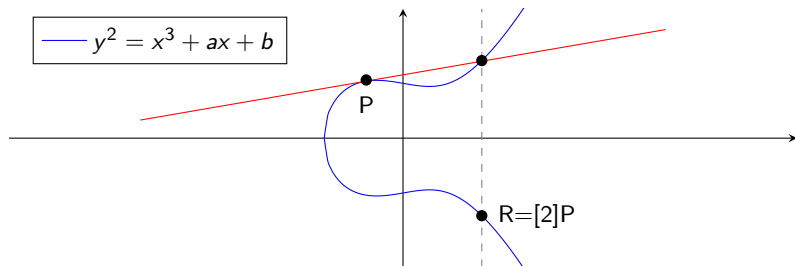
$$s \equiv (Py - Qy)(Px - Qx)^{-1} \pmod{q}$$

$$Rx \equiv s^2 - Px - Qx \pmod{q}$$

$$Ry \equiv Py - s(Rx - Px) \pmod{q}$$

*It can be seen that these formulae do not involve the curve parameter  $b$ .*

# Point Doubling



$$s \equiv (3Px^2 + a)(2Py)^{-1} \pmod{q}$$

$$Rx \equiv s^2 - 2Px \pmod{q}$$

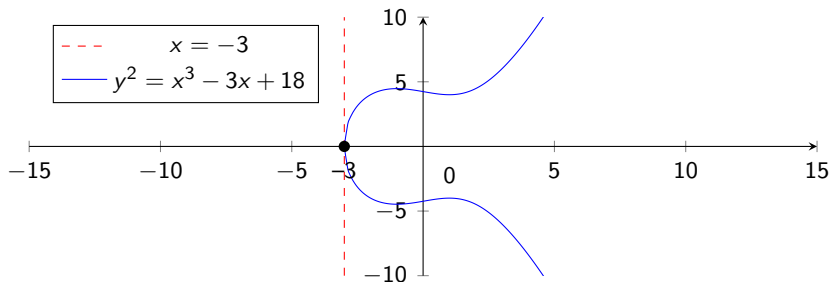
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# Order Two Points

- An important observation is that every point of the form  $P = (P_x, 0)$  equals its own inverse, thus has order two

$$P + P = P + [-1]P = \infty.$$



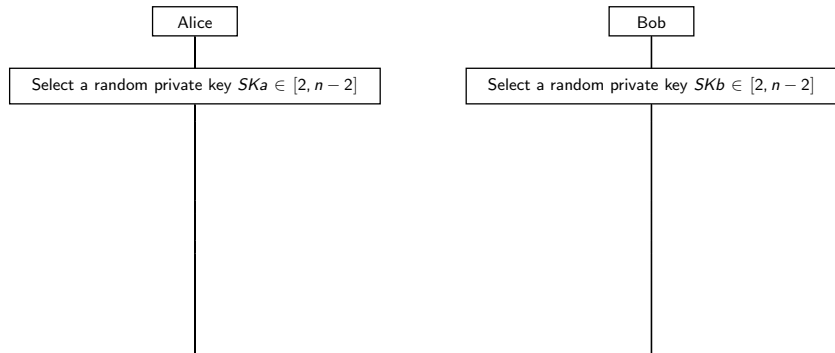
# Elliptic Curve Diffie-Hellman

- The *Elliptic Curve Diffie-Hellman* (ECDH) protocol is a variant of the Diffie-Hellman key exchange protocol.
- Both parties agree on an Elliptic Curve  $E$  and a generator point  $P \in E$ .
- Then they communicate as follows:



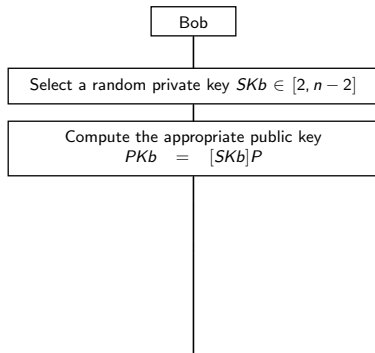
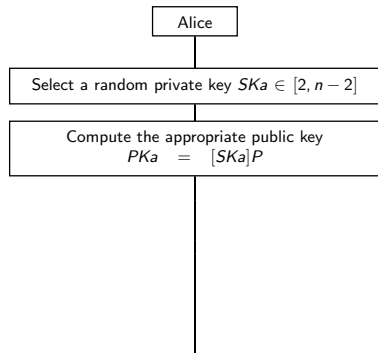
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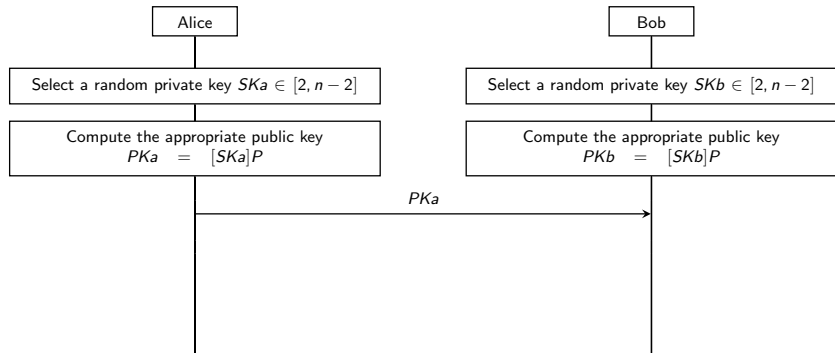
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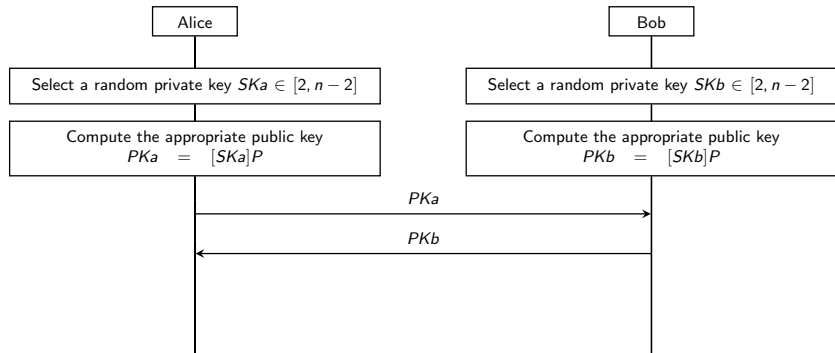
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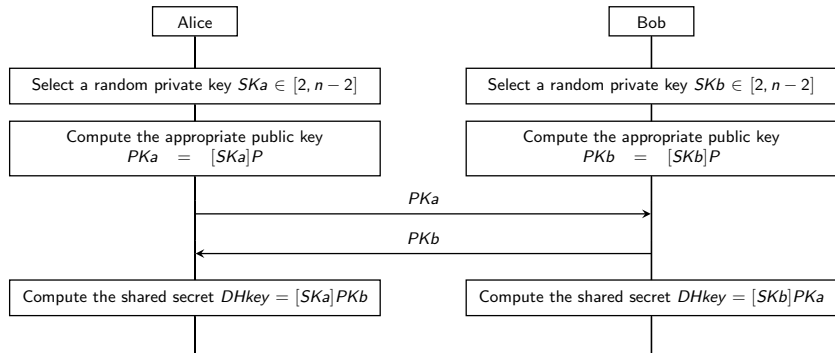
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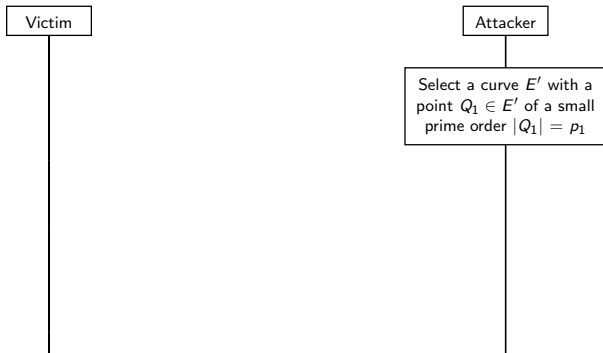


# Invalid Curve Attack

- The Invalid Curve Attack, introduced by Biehl et al., is a cryptographic attack where invalid group elements (points) are used in order to manipulate the group operations to reveal secret information.

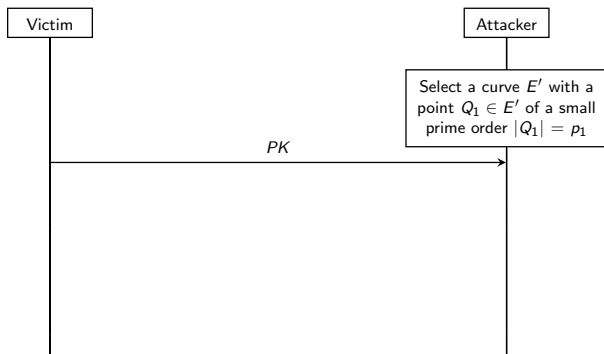
# Invalid Curve Attack

- Let  $SK$  be the secret key of the victim device and let  $PK = [SK]P$  its public key.
- Let  $E'$  be a different group defined by the curve equation  $y^2 = x^3 + ax + b'$  with the same  $a$  and a different  $b'$  parameter.



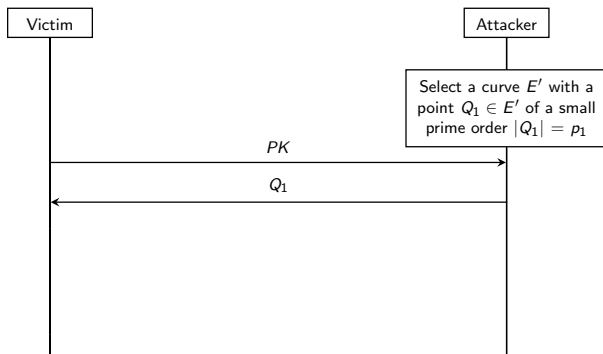
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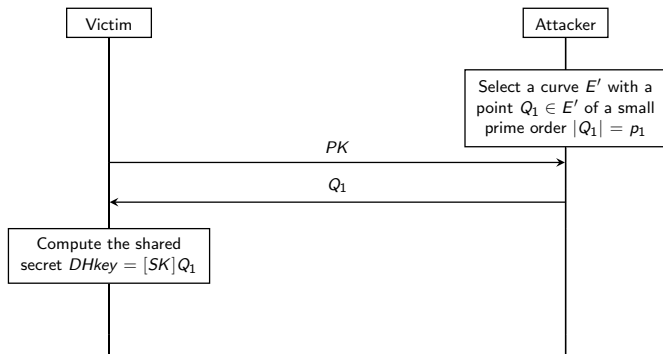
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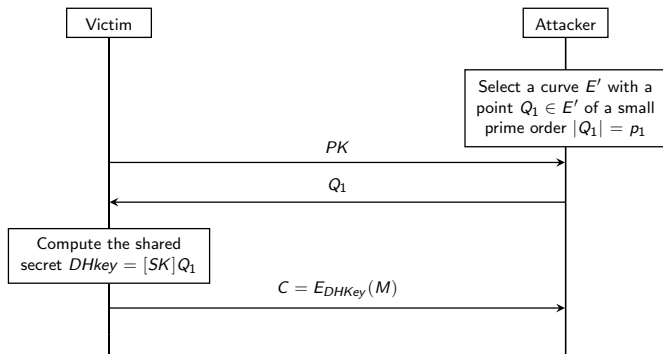
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# Invalid Curve Attack

- For simplicity let's assume that  $M$  is a message known to the attacker.
- The attacker wishes to find the discrete log of  $DHKey$  in the small subgroup generated by  $Q_1$ .
- Let  $a_1$  be the discrete log of  $DHkey$ :

$$a_1 \equiv SK \pmod{p_1}.$$

- The attacker finds  $a_1$  by iterating over all  $a_1 \in [0, p_1 - 1]$  and checking whether  $E_{[a_1]Q_1}(M) = C$ .
- This exchange repeats with a different subgroup orders  $p_i$  until the product of the primes satisfies

$$\prod_{i=1}^k p_i > n.$$

- Finally, the attacker recovers the victim's private key using the Chinese-Remainder-Theorem.

# The Invalid Curve Attack

- The original Invalid Curve Attack relies on the following assumptions
  - The key-exchange could be initiated multiple times with the **same** private key.
  - The attacker can select any pair  $(x, y) \in \mathbb{F}_q^2$  as a point.
- As a mitigation the BT specification suggests refreshing the ECDH key-pair on every pairing attempt.
- Most implementors follow this suggestion.

# Bluetooth Pairing

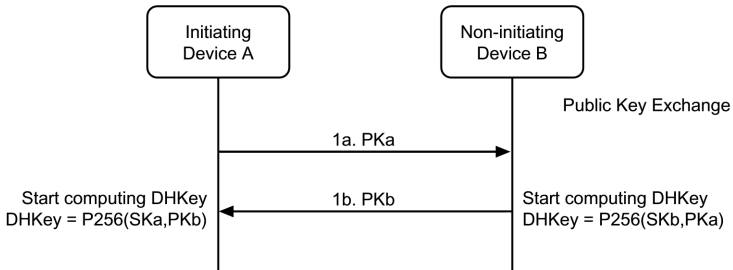
- The pairing protocol is part of the Bluetooth link layer protocol.
  - It generates the encryption keys for the rest of the protocol.
- Due to the similarity of SSP and LE SC, our attack applies to both protocols.
  - For this presentation we arbitrarily chose to concentrate on LE SC.

# Bluetooth LE Secure Connections

The protocol comprises of four phases:

- Phase 1 – Feature exchange (irrelevant for this talk).
- Phase 2 – Key exchange.
- Phase 3 – Authentication.
- Phase 4 – Key derivation.

# Bluetooth LE SC Phase 2 – Key Exchange



## Function f4 – Commitment Value Generation Function

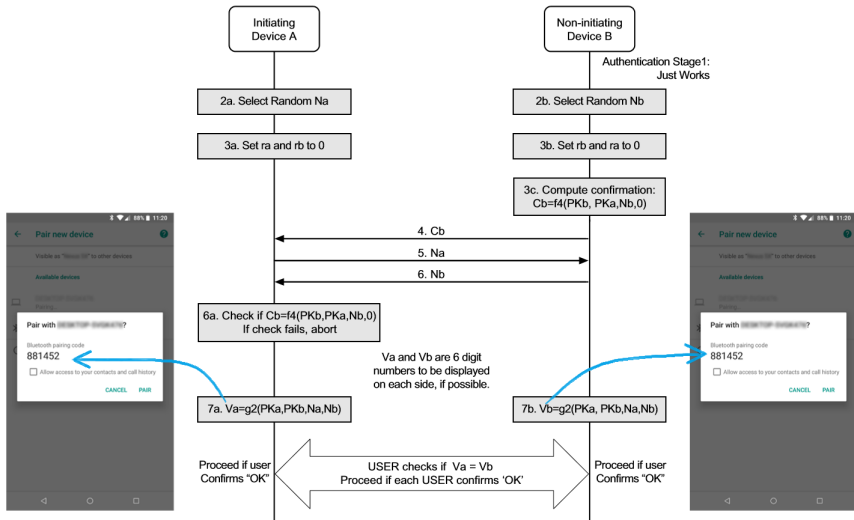
$$f4(U, V, X, Y) = \text{AES-CMAC}_X(U \parallel V \parallel Y)$$

## Function g2 – User Confirm Value Generation Function

The six least decimal digits of the following function:  
 $g2(U, V, X, Y) = \text{AES-CMAC}_X(U \parallel V \parallel Y) \pmod{2^{32}}$

# Bluetooth LE SC Phase 3 – Authentication

Note that unintuitively  $PKa$  and  $PKb$  in this diagram refers to the **x-coordinate** of each public-key, later in the specification defined as  $PKax$  and  $PKbx$ .



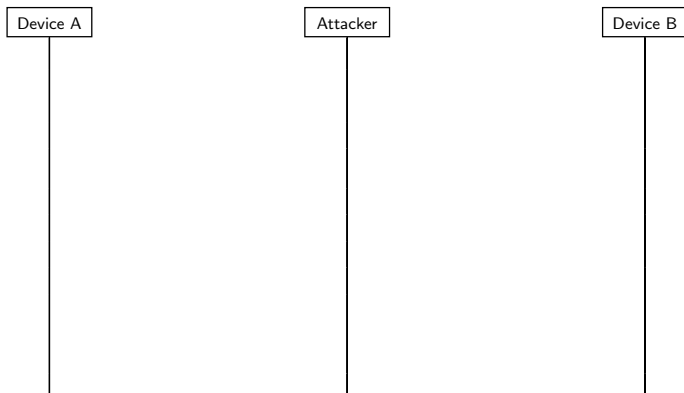
# Our Fixed Coordinate Invalid Curve Attack

- The Fixed Coordinate Invalid Curve Attack is a new variant of the Invalid Curve Attack in which we exploit the ability to forge low order ECDH public keys that preserve the x-coordinate of the original public-keys.
- It is based on the following observations:
  - Only the x-coordinate of each party is authenticated during the Bluetooth pairing protocol.
  - The protocol does not require its implementations to validate whether a given public-key satisfies the curve equation.
- We describe two versions of our attack:
  - Semi-Passive.
  - Fully-Active.



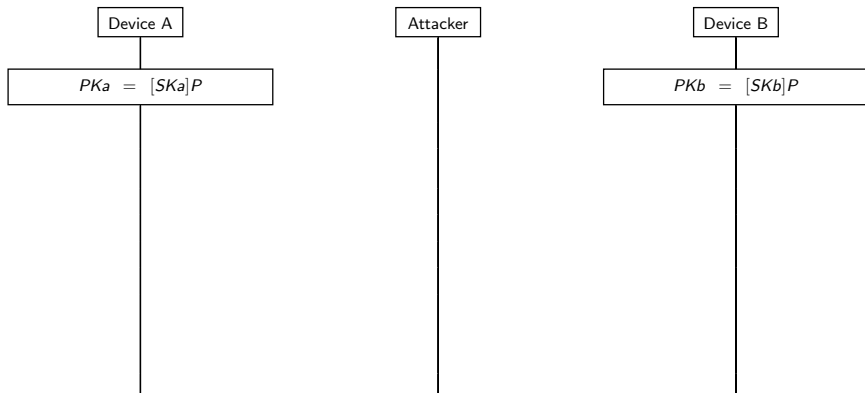
# The Semi-Passive Attack

- The Semi-Passive attack requires a message interception during the second phase of the pairing.
- It replaces the  $y$ -coordinate of each public key with 0.



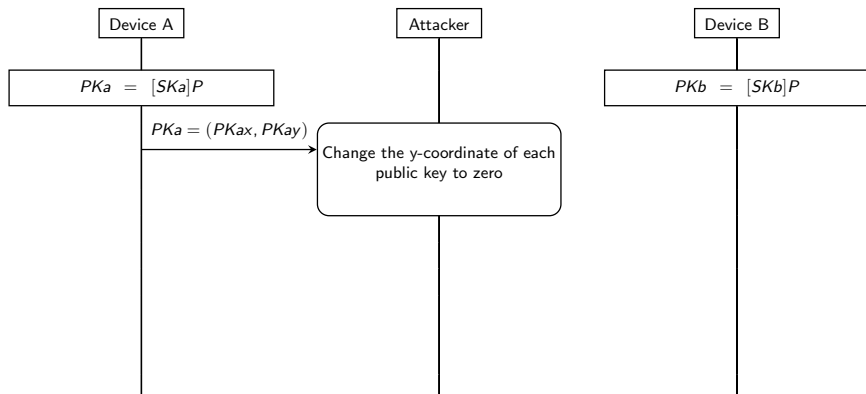
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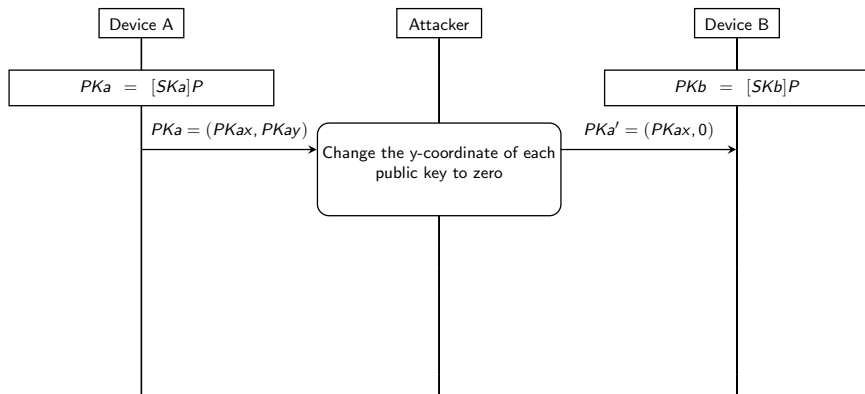
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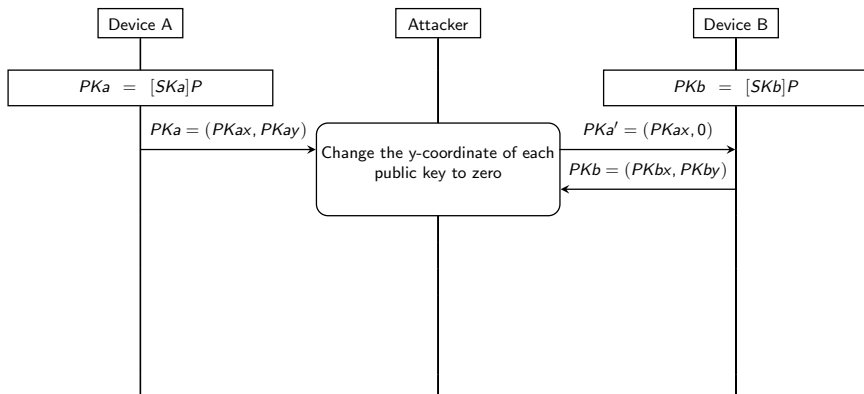
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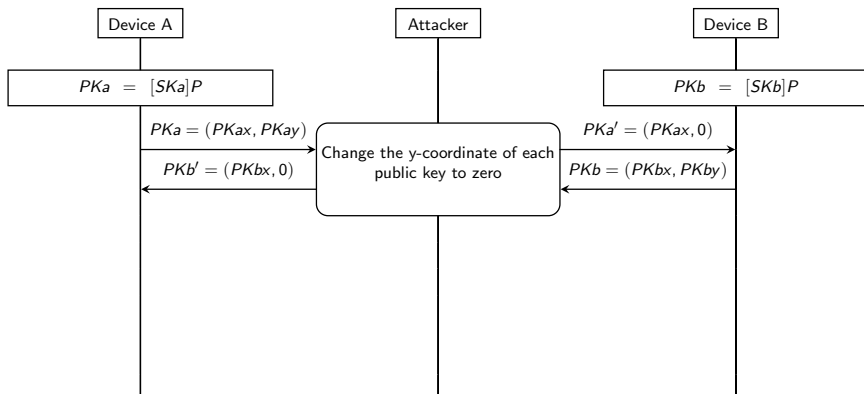
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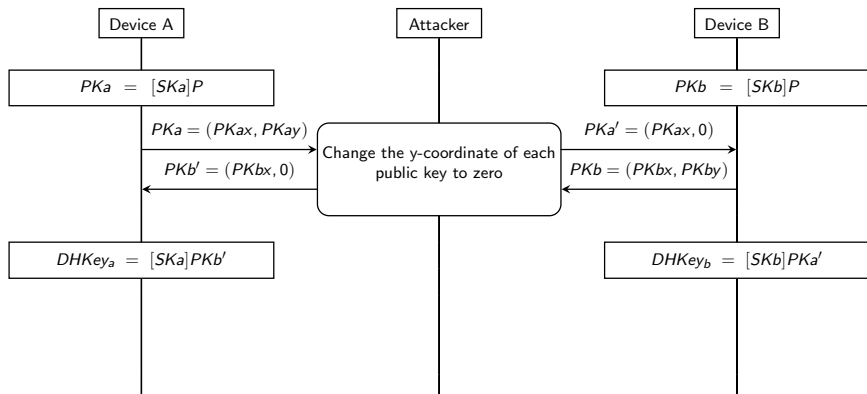
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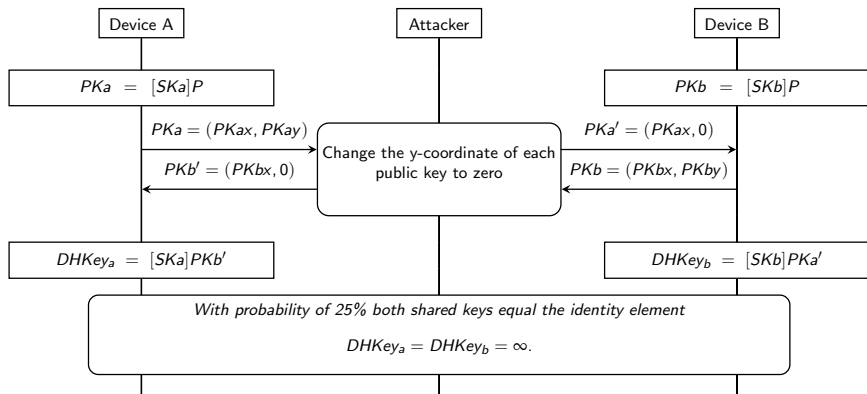
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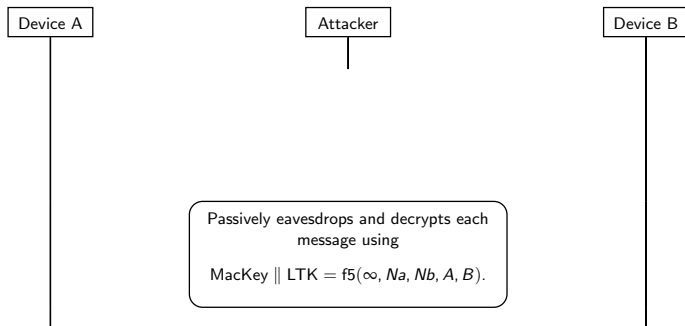
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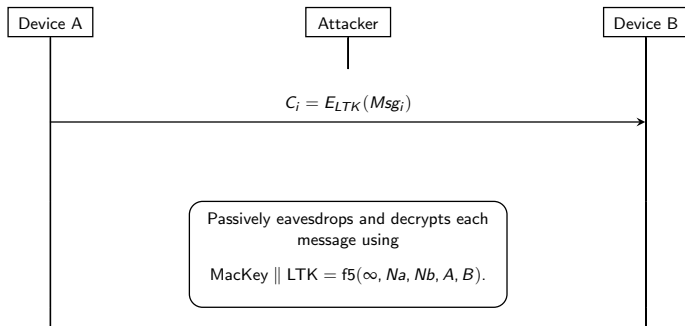
# The Semi-Passive Attack – Passive Message Eavesdropping

- In case both shared keys equal the identity element
  - the attack is undetected,
  - the attacker knows the shared key, and
  - the rest of the communication can be passively eavesdropped.



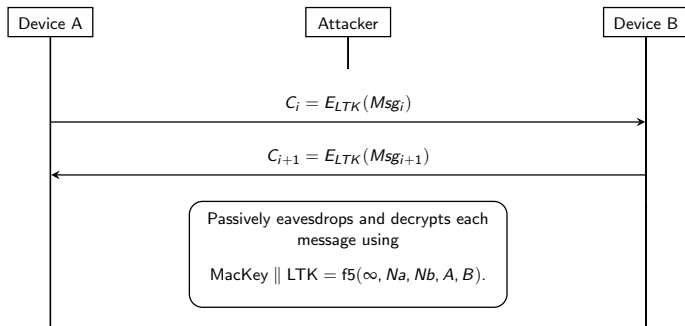
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## Function f5 – Key Derivation Function

$SALT = 0x6C888391AAF5A53860370BDB5A6083BE$

$T = AES-CMAC_{SALT}(DHKey)$

$f5(DHKey, N1, N2, A1, A2) =$

$AES-CMAC_T(0 \parallel 'btle' \parallel N1 \parallel N2 \parallel A1 \parallel A2 \parallel 256) \parallel$

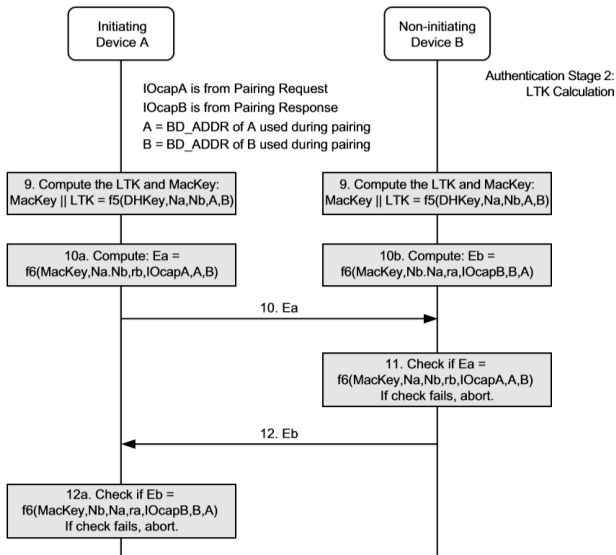
$AES-CMAC_T(1 \parallel 'btle' \parallel N1 \parallel N2 \parallel A1 \parallel A2 \parallel 256)$

## Function f6 – Check Value Generation Function

$f6(W, N1, N2, R, IOcap, A1, A2) =$

$AES-CMAC_W(N1 \parallel N2 \parallel R \parallel IOcap \parallel A1 \parallel A2)$

# Bluetooth LE SC Phase 4 – Key Derivation



# The Fully-Active Attack

- By also intercepting messages sent during the fourth phase we can further improve the attack success probability to 50%.
- $DHKey_b$  never equals  $PKb'$   
 $\implies$  the Semi-Passive attack fails when  $DHKey_a = PKb'$ .

$DHKey_a$	$DHKey_b$
$\infty$	$\infty$
$\infty$	$PKa'$
$PKb'$	$\infty$
$PKb'$	$PKa'$

# The Fully-Active Attack

- In the beginning of the fourth phase Device A commits to the mutual key by transmitting  $Ea$ .
- The attacker can use the value of  $Ea$  in order to determine the value of  $DHKey_a \in \{PKb', \infty\}$ .
- If  $DHKey_a = \infty$  the attacker continues as described in the Semi-Passive Attack without further interception.

# The Fully-Active Attack – Phase 4

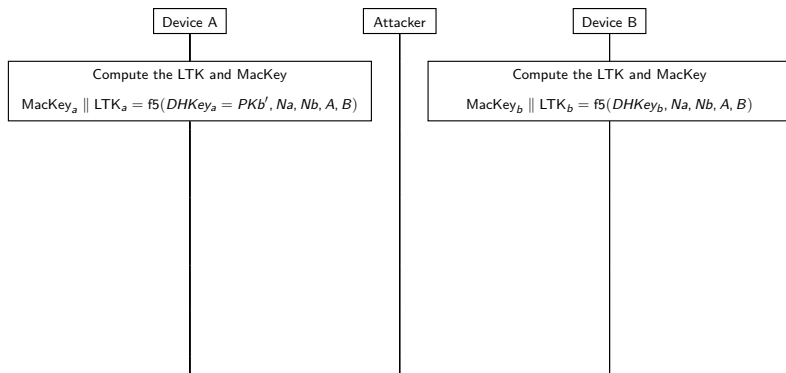
- The following diagram describes the attack considering  $DHKey_a = PKb'$ .





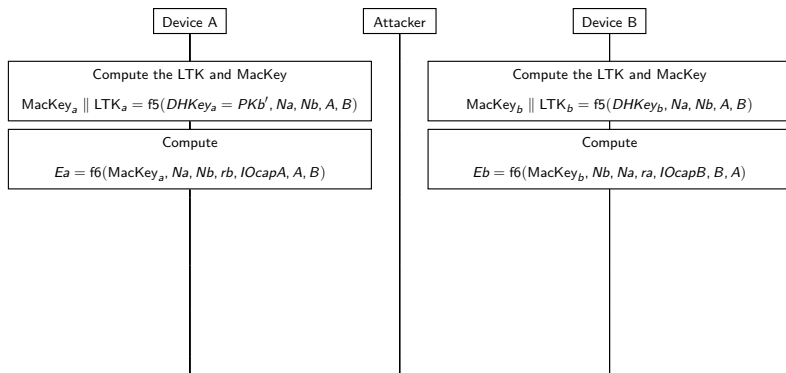
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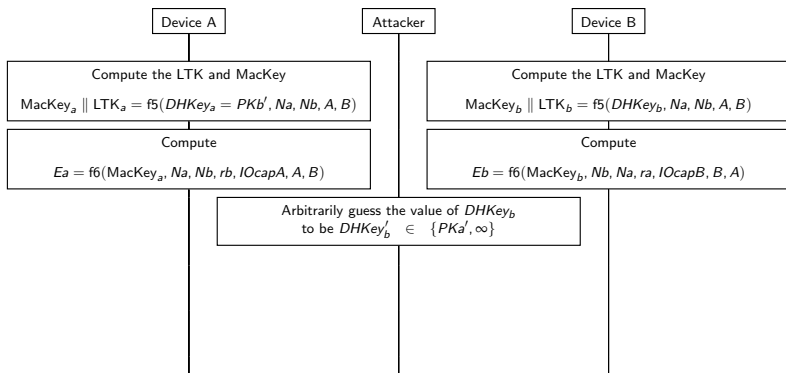
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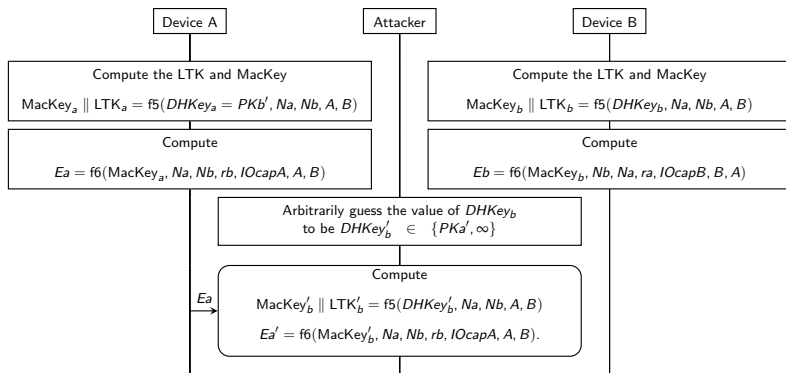
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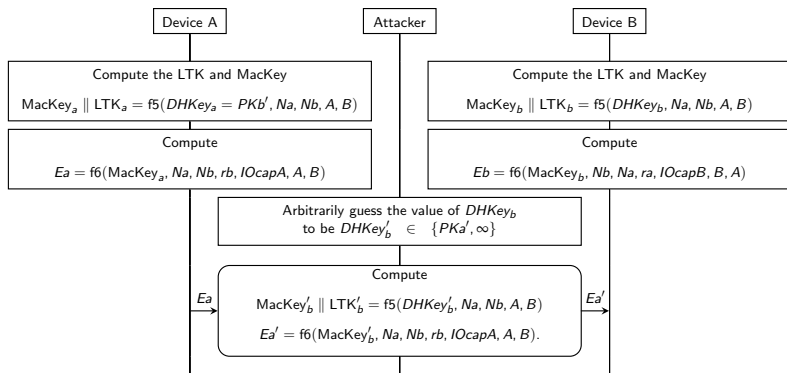
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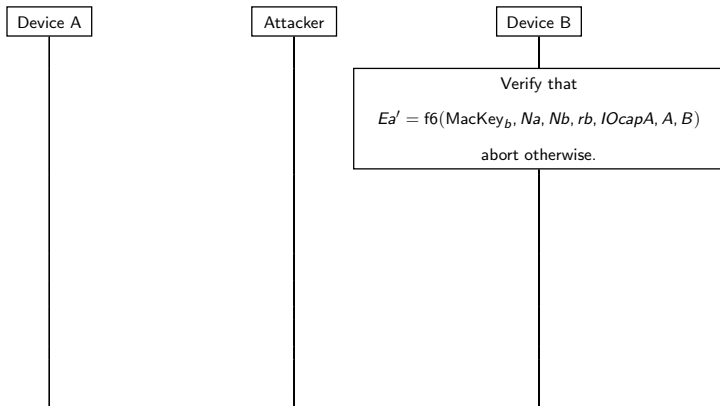


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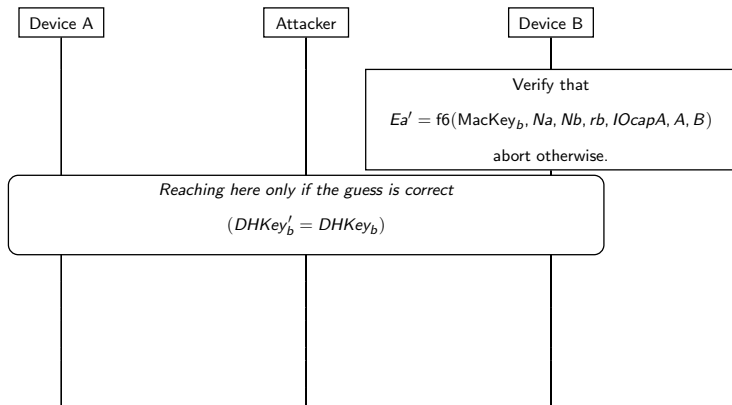
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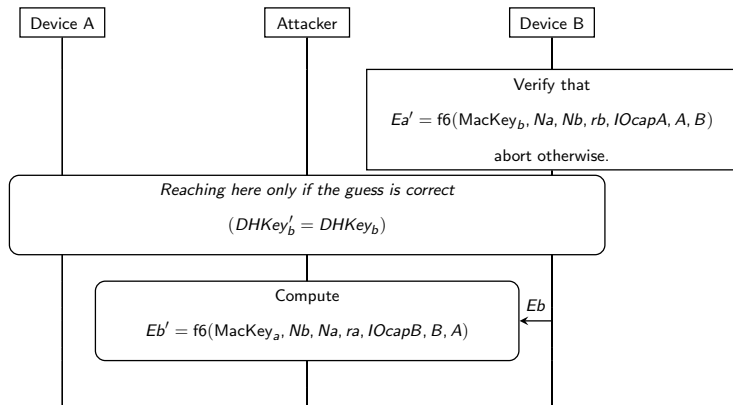
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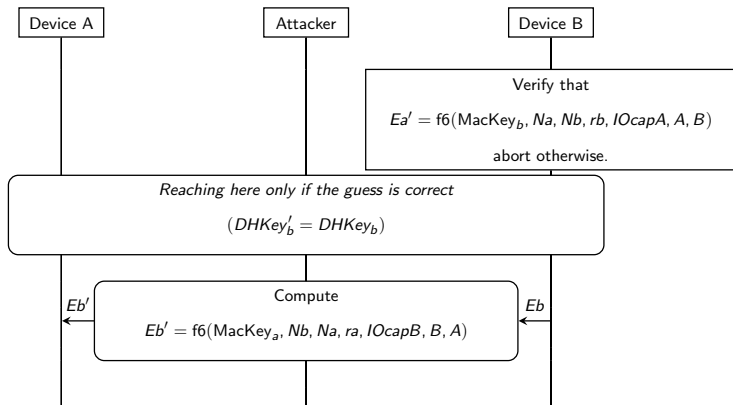


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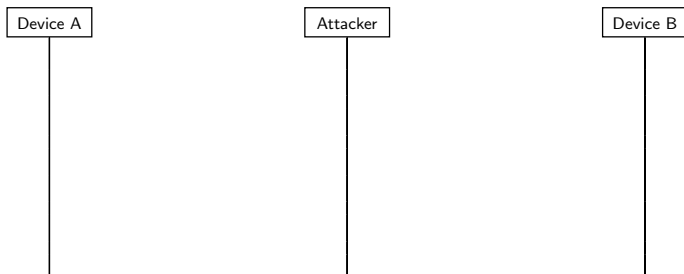




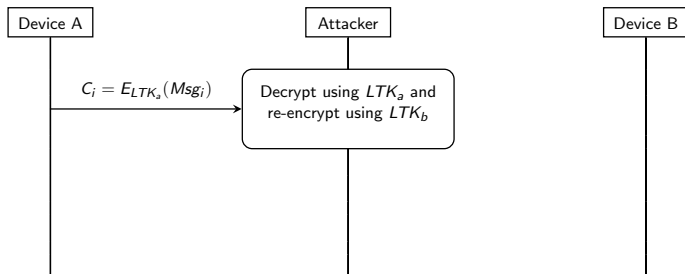
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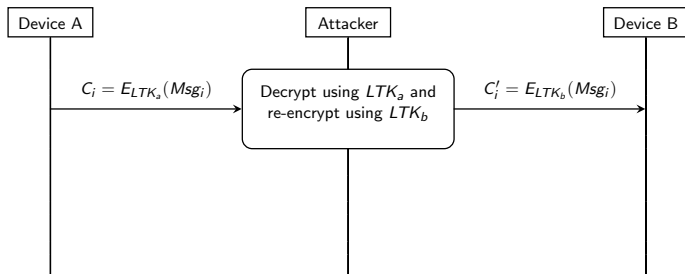
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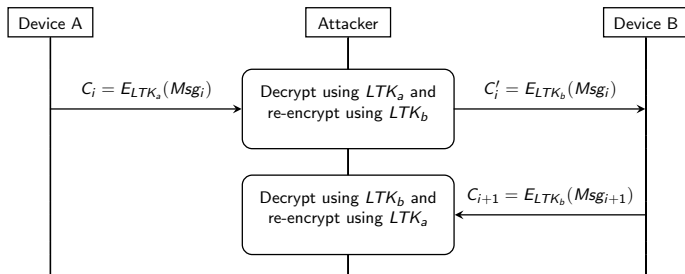
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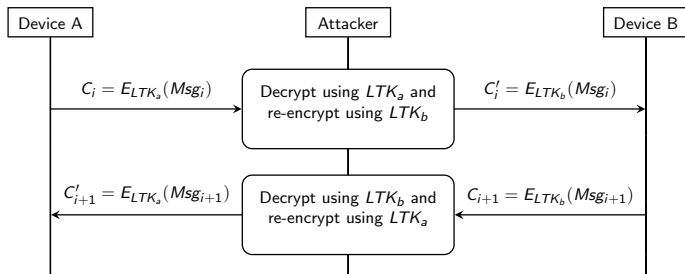
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# Success Rate of Our Attack

## Success Rate – Semi-Passive Attack

$DHKey_a \backslash DHKey_b$	$\infty$	$PKa'$
$\infty$	Success	Failure
$PKb'$	Failure	Failure

Total Semi-Passive Attack: **25%**

## Success Rate – Fully-Active Attack (when guessing $DHKey'_b = \infty$ )

$DHKey_a \backslash DHKey_b$	$\infty$	$PKa'$
$\infty$	Success	Failure
$PKb'$	Success	Failure

Total Fully-Active Attack: **50%**

# Success Rate of Our Attack

## Success Rate – Semi-Passive Attack

$DHKey_a \backslash DHKey_b$	$\infty$	$PKa'$
$\infty$	Success	Failure
$PKb'$	Failure	Failure

Total Semi-Passive Attack: **25%**

## Success Rate – Fully-Active Attack (when guessing $DHKey'_b = PKa'$ )

$DHKey_a \backslash DHKey_b$	$\infty$	$PKa'$
$\infty$	Success	Failure
$PKb'$	Failure	Success

Total Fully-Active Attack: **50%**



# Frequency Hopping

- Bluetooth uses frequency hopping.
  - In [R13] it has been shown that the frequency hopping of Bluetooth Low Energy could be predicted easily and thus it does not provide any security.
  - More sophisticated equipment can listen/transmit to all of the channels used by Bluetooth thus avoiding this issue entirely.

# Over the Air Packet Manipulation

- MitM attacks requires over the air packets manipulation.
  - There are several projects that provide over the air packet manipulation capability on Bluetooth, such as GATTack.
  - Unfortunately, all of the solutions we found are limited to Bluetooth 4.0 and do not support Bluetooth 4.2 (with LE SC) due to its larger packet size.
  - It is safe to assume that products supporting Bluetooth 4.2 packet manipulation will be released in the near future as it becomes more popular.
- At the moment, only Bluetooth LE equipment is available for these attacks, since it is far simpler than Bluetooth BR/EDR.

# Design Flaws

- Both the  $x$ -coordinate and the  $y$ -coordinate are sent during the public key exchange.
  - ⇒ This is unnecessary and highly inadvisable.
- The protocol authenticates only the  $x$ -coordinate.
  - ⇒ The  $y$ -coordinate remains unauthenticated.

# Mitigations

- In order to protect against the classical Invalid Curve Attack the specification suggests refreshing the ECDH key-pair every pairing attempt.  
⇒ Our attack still works when this mitigation is applied.
- The obvious (and recommended) mitigation against our attack is to test whether the given ECDH public-key satisfies the curve equation.

# Vulnerable Platforms

- Our new attack was applicable to most available Bluetooth devices.
- We informed the Bluetooth SIG and the vendors.
- CVE-2018-5383 was assigned to this vulnerability in the Bluetooth protocol.

# Vulnerable Platforms – Bluetooth LE SC

- LE SC pairing is implemented in the host.
- The vulnerability is found in the host's operating system
  - Regardless of the Bluetooth controller.
- The Android Bluetooth stack, “Bluedroid” is vulnerable.
  - Tested on Nexus 5X devices with Android version 8.1.
- Apple iOS and MacOS was found to be vulnerable.
  - This includes all of the latest Apple products (both laptops, phones and tablets).
- At the time of our publication Microsoft Windows did not yet support LE SC.
  - This made all Windows versions vulnerable to the simpler Legacy Pairing Eavesdropping Attack.

# Vulnerable Platforms – Bluetooth BR/EDR SSP

- The key exchange in SSP is performed by the Bluetooth controller.
- The vulnerability depends on the Bluetooth controller's firmware implementation.
  - Independent of the operating-system.
- Controllers of most major vendors are vulnerable:
  - Qualcomm – Tested on Qualcomm's QCA6174A.
  - Broadcom – Tested on Broadcom's BCM4358 and BCM4339.
  - Intel – Tested on Intel 8265.

# Industry Reaction

- Google rated this vulnerability as High-Severity.
  - A patch was released for the Android OS on June 4th 2018.
- Apple released a formal statement explaining the vulnerability to its users.
  - A patch for iOS and MacOS was released on July 23rd 2018.
- Intel rated this vulnerability as High Severity as well.
  - A patch, referred by INTEL-SA-00128, was released to dozens of Intel's products on July 23rd 2018.
- Qualcomm and Broadcom had also released patches to their vendor partners.



- On July 23rd 2018 the Bluetooth SIG released a statement addressing our findings.
  - “To remedy the vulnerability, the Bluetooth SIG has now updated the Bluetooth specification to require products to validate any public key received as part of public key-based security procedures. In addition, the Bluetooth SIG has added testing for this vulnerability within our Bluetooth Qualification Program.”
  - The included specification change, released under the name “Erratum 10734”, implements our recommended mitigation.

# Summary

- We introduced the *Fixed Coordinate Invalid Curve Attack* which provides
  - A new tool for attacking the ECDH protocols.
  - Presented the application of our new attack to the Bluetooth pairing protocol.
- As a result of our attack all of the variants of Bluetooth were proven insecure.
- We discovered multiple design flaws in the Bluetooth specification.
- We found that all of the major vendors are vulnerable.
- The Bluetooth protocol was modified according to our findings.

- Special thanks to the CERT/CC for helping us managing the responsible disclosure to the vendors, and to the vendors for the cooperation on patching their systems.

# The End